

Cross Sections

- **cross section:** $\sigma = \pi R^2$
 $[\sigma] = \text{barn}$ 1 b = 10^{-24} cm^2
 1 mb = 10^{-27} cm^2
 1 fb = 10^{-39} cm^2
 strong interaction: $\sigma(\pi N) \sim 100 \text{ mb}$
- **interaction radius:** $R = \sqrt{\sigma/\pi}$
 $R(\text{strong}) \sim \sqrt{10^{-30} \text{ m}^2} \sim 10^{-15} \text{ m} = 1 \text{ fm} = 1 \text{ fermi}$
- **lifetime:** $\tau = R / c$ = reaction time
 $\tau(\text{strong}) = 1 \text{ fm} / c = 3 \times 10^{-24} \text{ s}$
- **uncertainty relation:** $\hbar = \Gamma \tau$
 $\hbar c = 200 \text{ MeV fm} = \Delta E \Delta R$
- **decay width:** $\Gamma = \hbar / \tau = \hbar c / R$
 energy scale $\Gamma = E$

$\Gamma = 200 \text{ MeV fm} / R$
 $E(\text{strong}) = 200 \text{ MeV}$ $\Gamma(\text{strong: } \Delta, \rho) = 120\text{-}150 \text{ MeV}$
- **coupling constant:** $F = \alpha \hbar c / r^2$ electric force
 $\alpha = e^2 / (4\pi \hbar c)$ dimensionless ($\epsilon_0=1$)

$$E = \Gamma = \hbar/\tau = \hbar c / R = \hbar c \sqrt{\pi/\sigma} \sim \left| \begin{array}{c} \diagup \quad \diagdown \\ \bullet \quad \bullet \\ \diagdown \quad \diagup \end{array} \right|^2 \sim \alpha^2$$