

5. Physik des Z^0 -Bosons

Glashow-Salam-Weinberg-Theorie (GSW)

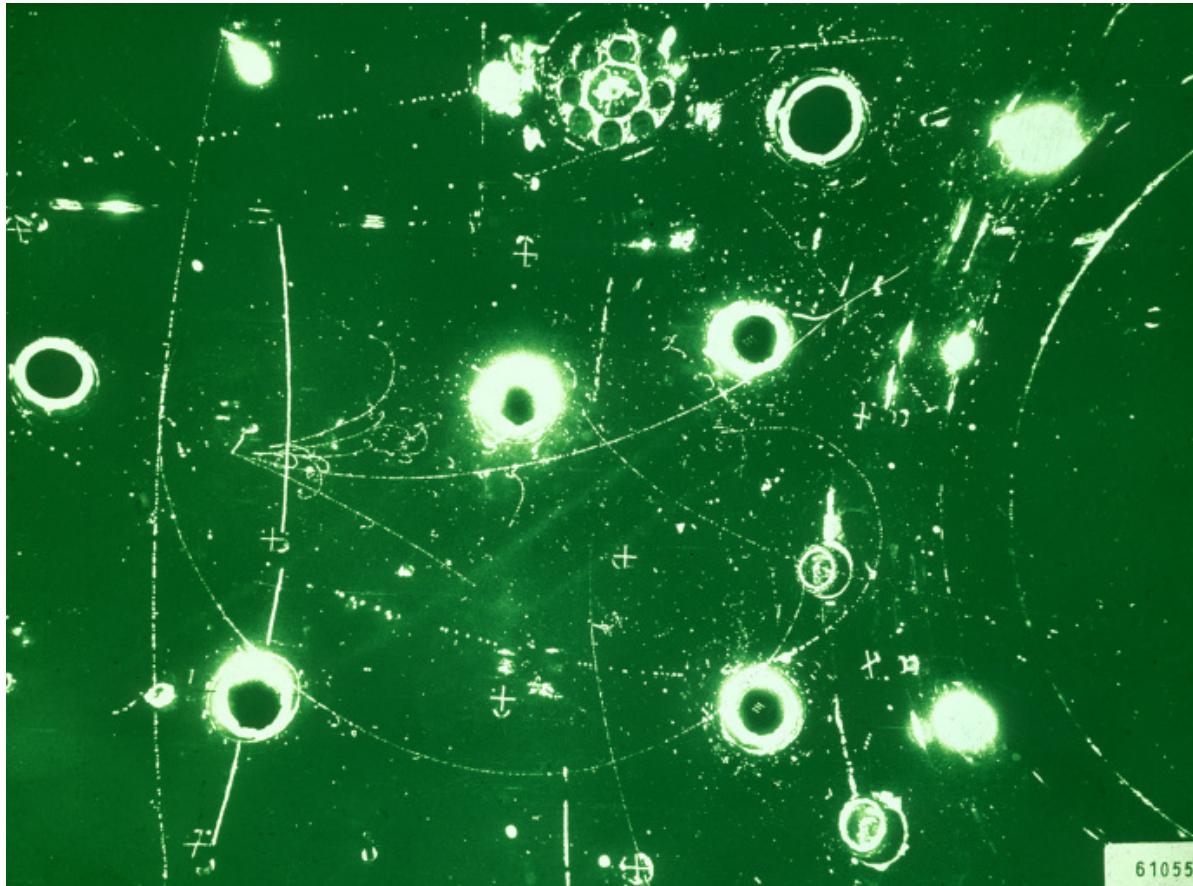
Gruppe	Kopplung	Felder	Generatoren	physikalische Teilchen
SU(2) _L	g	W_μ^1 W_μ^2 W_μ^3	τ_1 τ_2 τ_3	$\left. \right\} W_\mu^\pm = \frac{1}{\sqrt{2}} (W_\mu^1 \pm W_\mu^2)$? Z_μ
U(1) _Y	g'	B_μ	Y ? A_μ

$$\begin{aligned} Z^0 &= W^0 \cdot \cos \theta_W - B^0 \cdot \sin \theta_W \\ \gamma &= W^0 \cdot \sin \theta_W + B^0 \cdot \cos \theta_W \end{aligned}$$

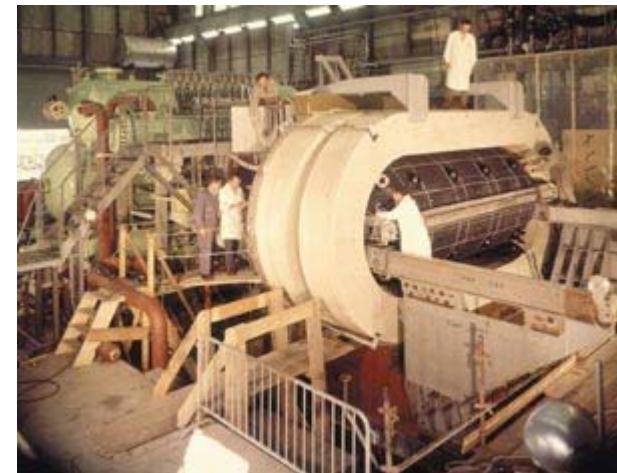
3 unabhängige Parameter

g, g', θ_W	oder	g, M_W, θ_W	oder	G_F, α, θ_W
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5.1 Entdeckung des Neutralen Stroms (NC)



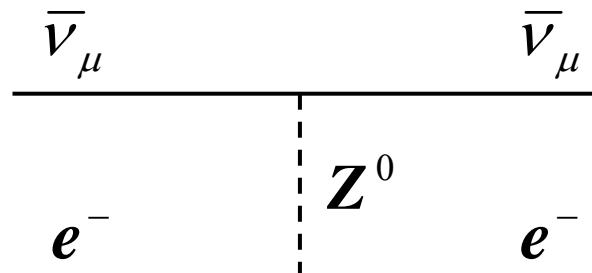
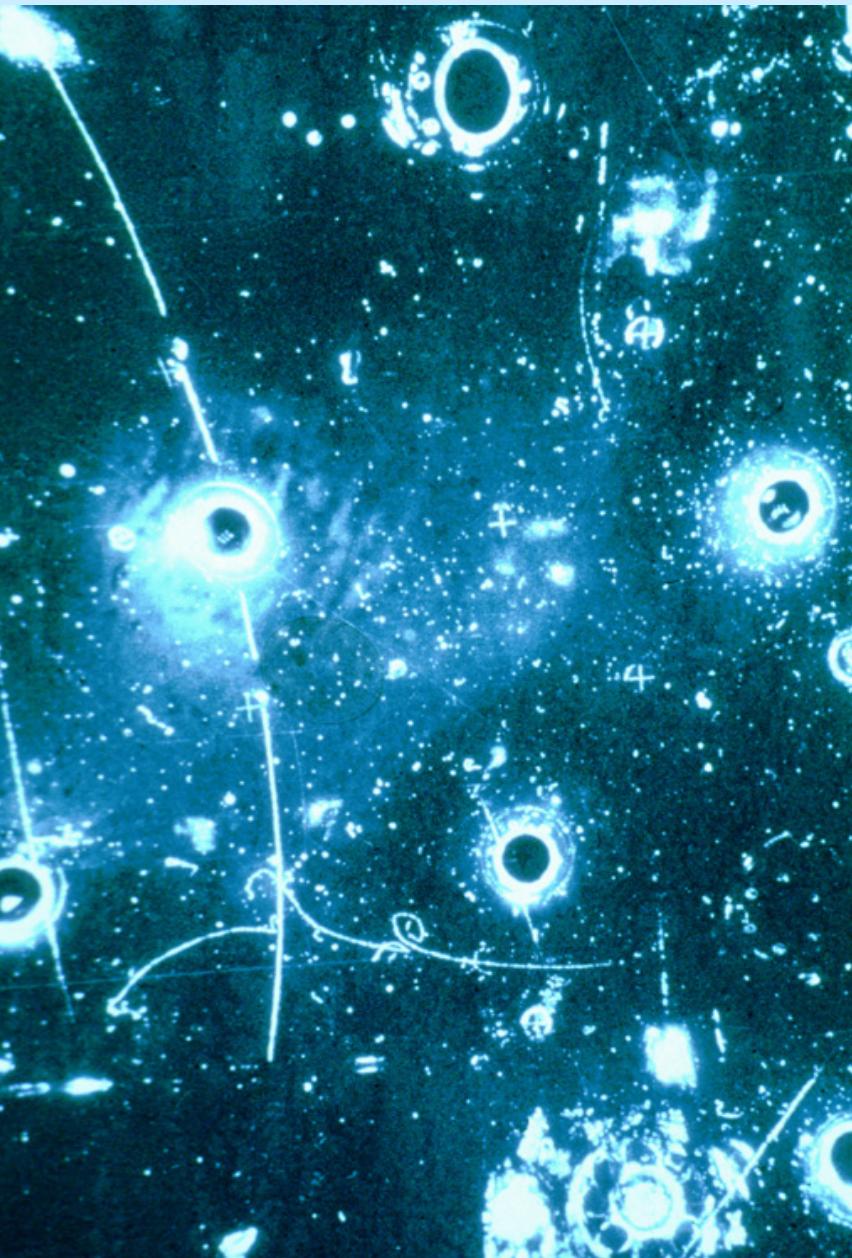
The Gargamelle chamber



Date: Oct 1973

A hadron event - a neutrino interacting with a nucleon and emerging as a neutrino : first observation of "neutral currents" in the Gargamelle heavy liquid bubble chamber.

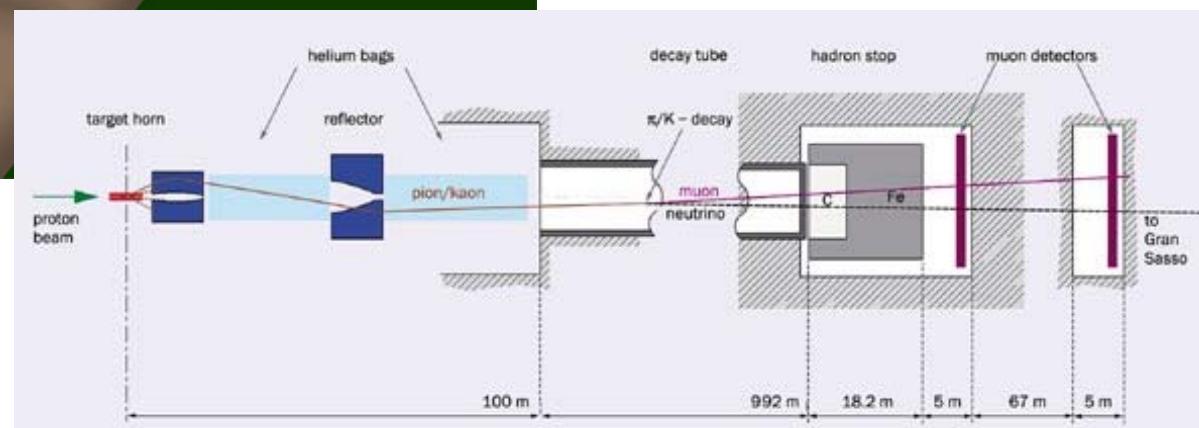
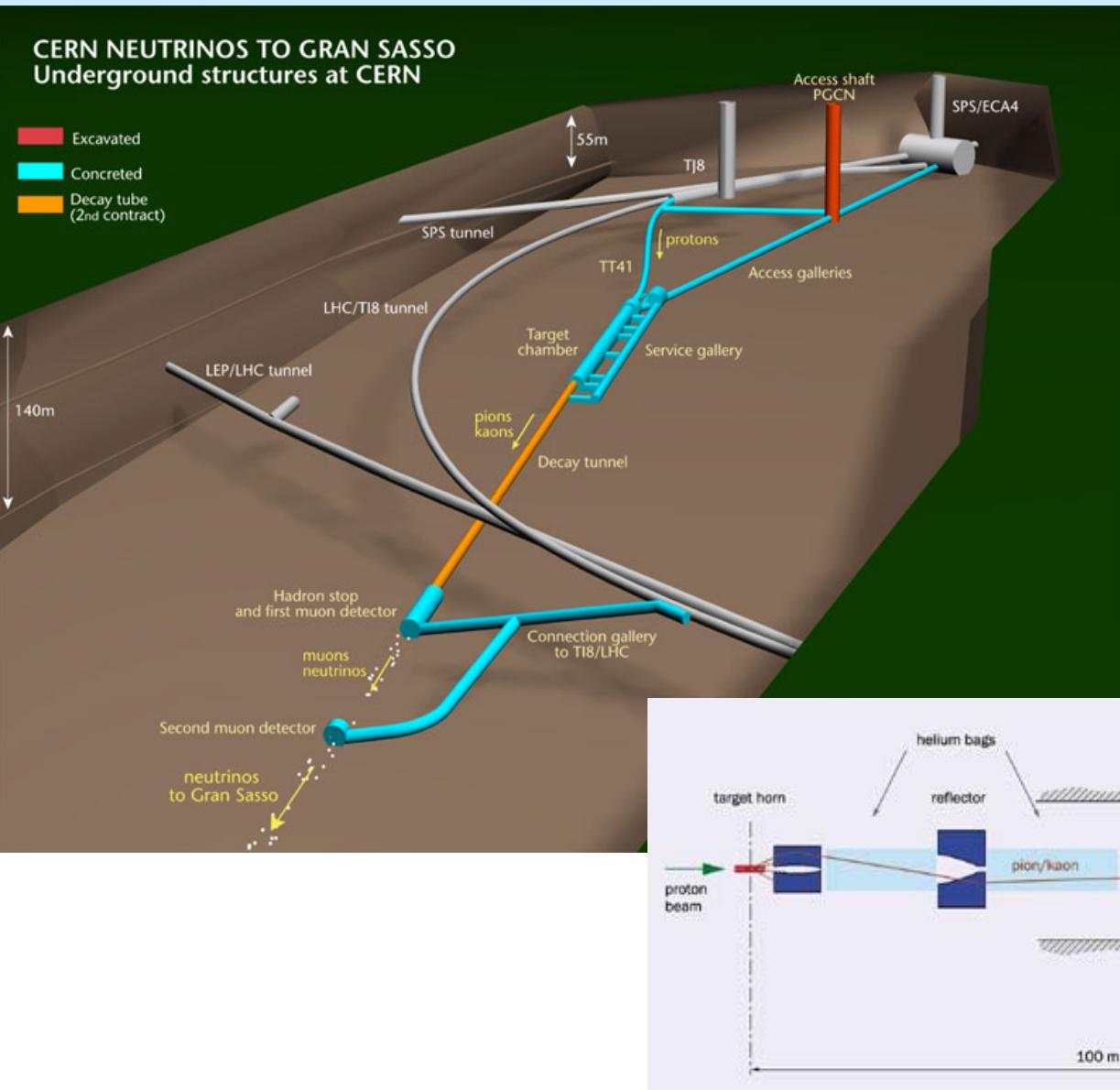
NC: leptonisches Ereignis



Date: 1973

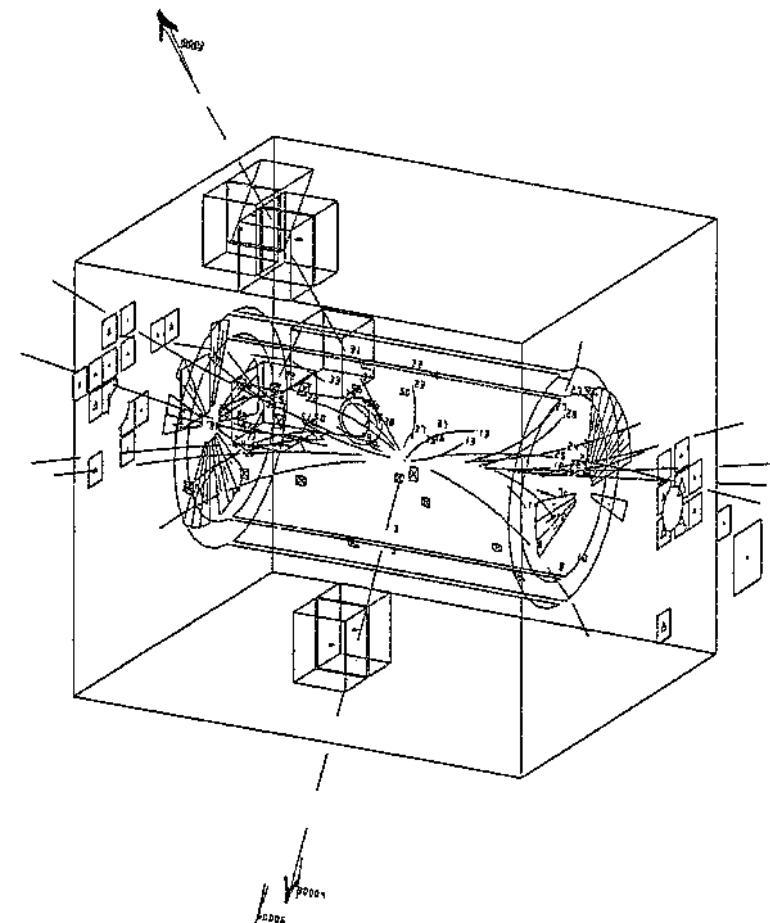
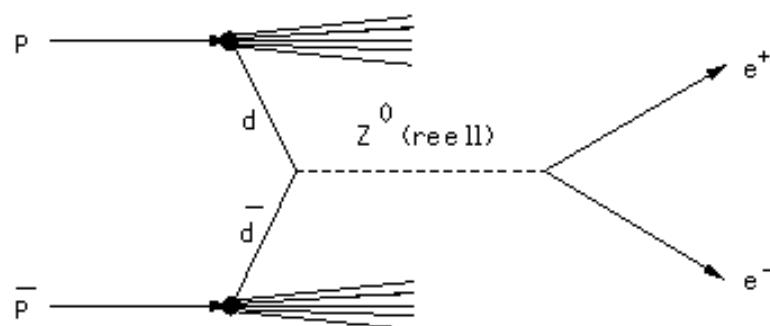
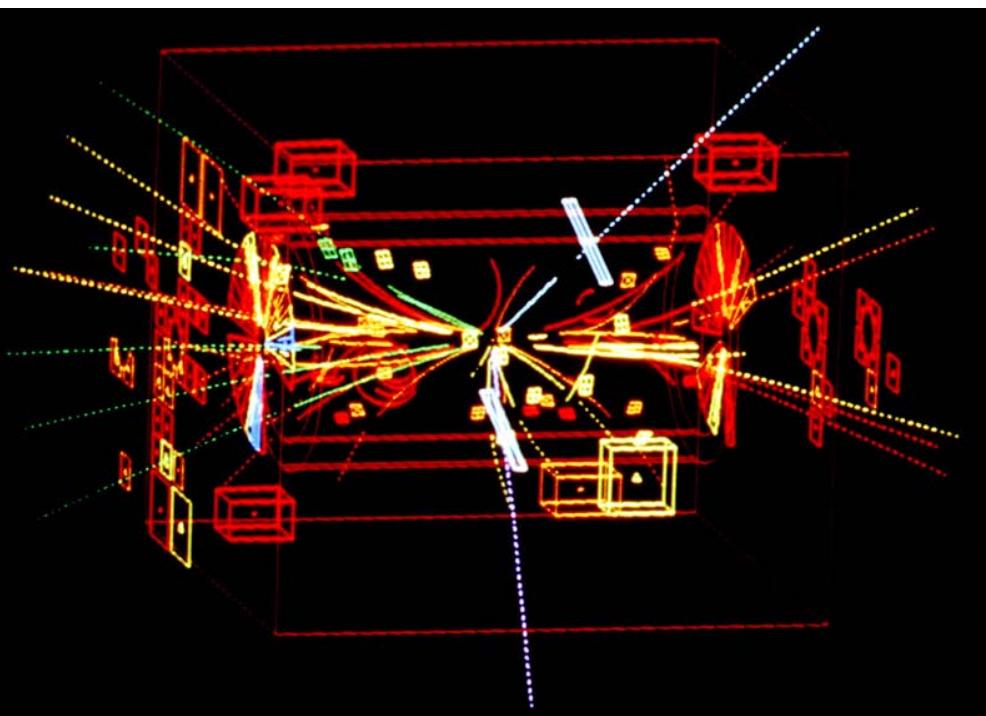
A lepton event - a neutrino interacting with an electron and emerging as a neutrino : first observation of "neutral currents" in the Gargamelle heavy liquid bubble chamber. In the photograph, an unseen neutrino interacts with an electron and emerges as a neutrino instead of changing into a muon - what is seen (horizontally) is the track of the electron. This lepton event offers proof of the existence of neutral currents.

Neutrino-Strahlen (Beispiel CNGS)

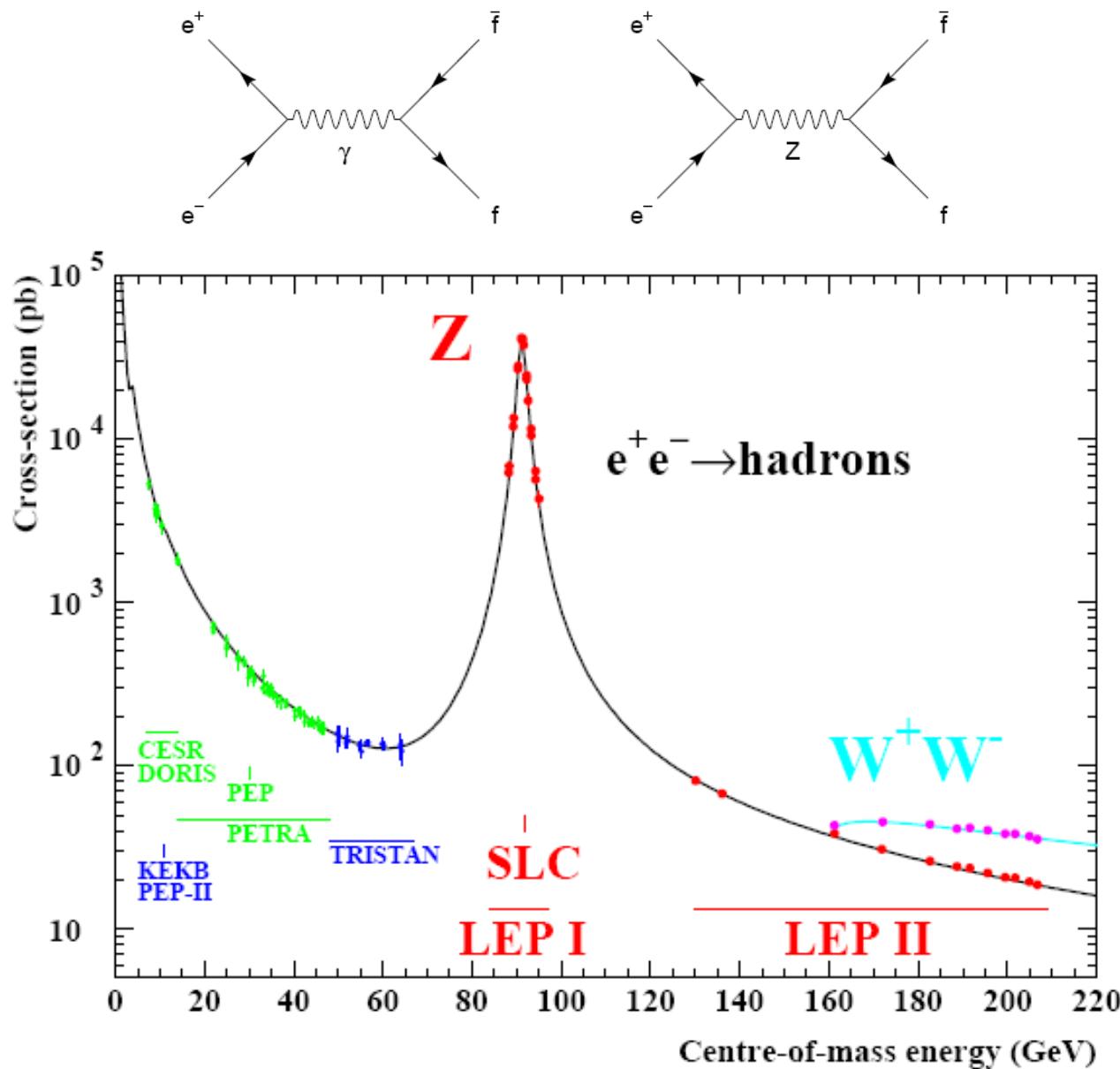


Direkte Erzeugung des Z^0 -Bosons

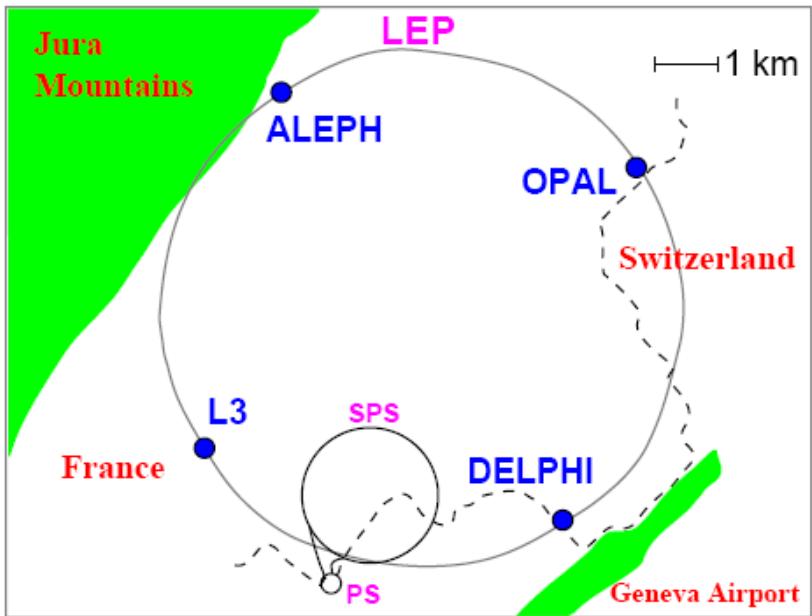
First candidate Z event at UA1, 1983.



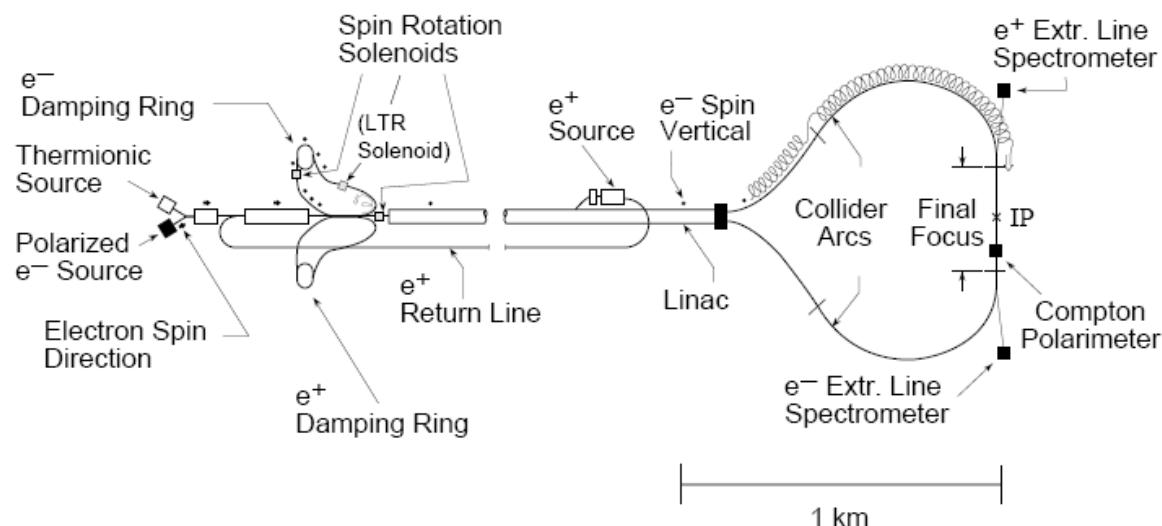
5.2 Resonante Erzeugung des Z^0 -Bosons in e^+e^-



LEP/SLC-Ergebnisse



$$\begin{aligned}
 m_Z &= 91.1875 \pm 0.0021 \text{ GeV} \\
 \Gamma_Z &= 2.4952 \pm 0.0023 \text{ GeV} \\
 \rho_\ell &= 1.0050 \pm 0.0010 \\
 \sin^2 \theta_{\text{eff}}^{\text{lept}} &= 0.23153 \pm 0.00016 .
 \end{aligned}$$



Schwacher Isospin und NC-Kopplungen

Family			T	T_3	Q
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$	1/2	+1/2 -1/2	0 -1
ν_{eR}	$\nu_{\mu R}$	$\nu_{\tau R}$	0	0	0
e_R	μ_R	τ_R	0	0	-1
$\begin{pmatrix} u \\ d \end{pmatrix}_L$	$\begin{pmatrix} c \\ s \end{pmatrix}_L$	$\begin{pmatrix} t \\ b \end{pmatrix}_L$	1/2	+1/2 -1/2	+2/3 -1/3
u_R	c_R	t_R	0	0	+2/3
d_R	s_R	b_R	0	0	-1/3

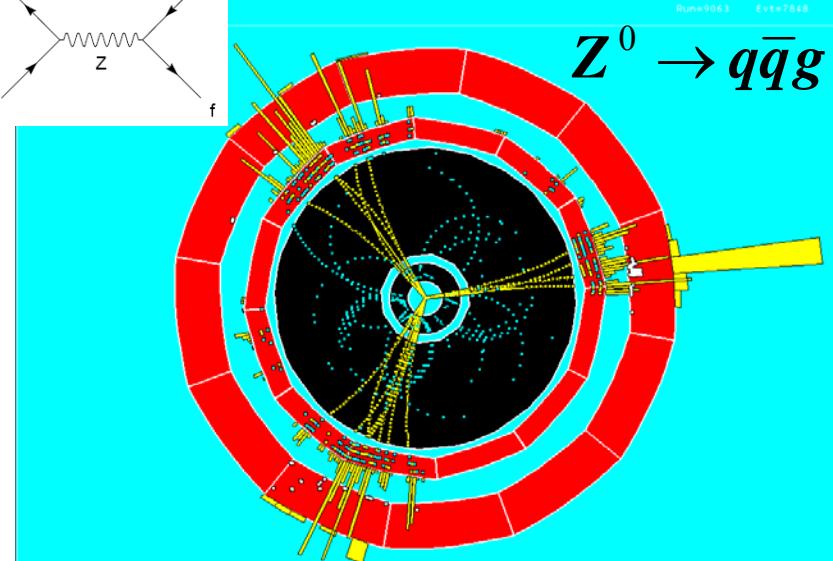
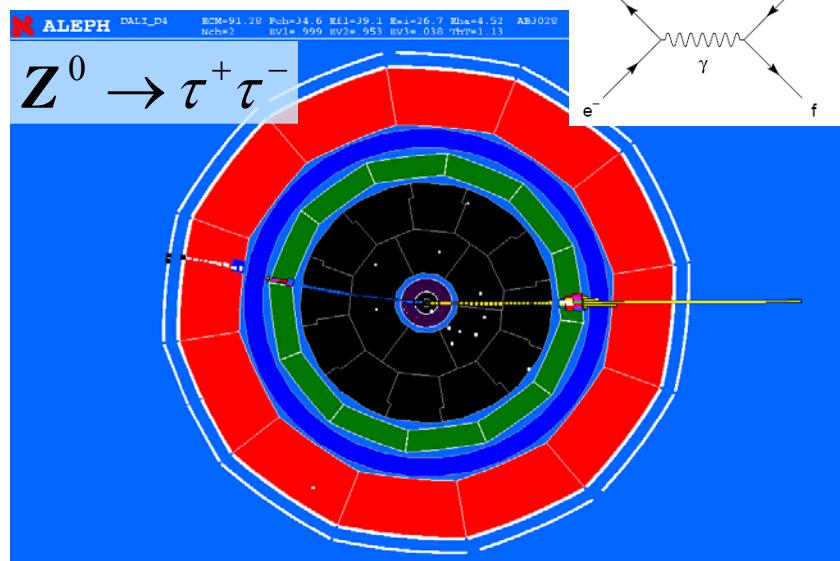
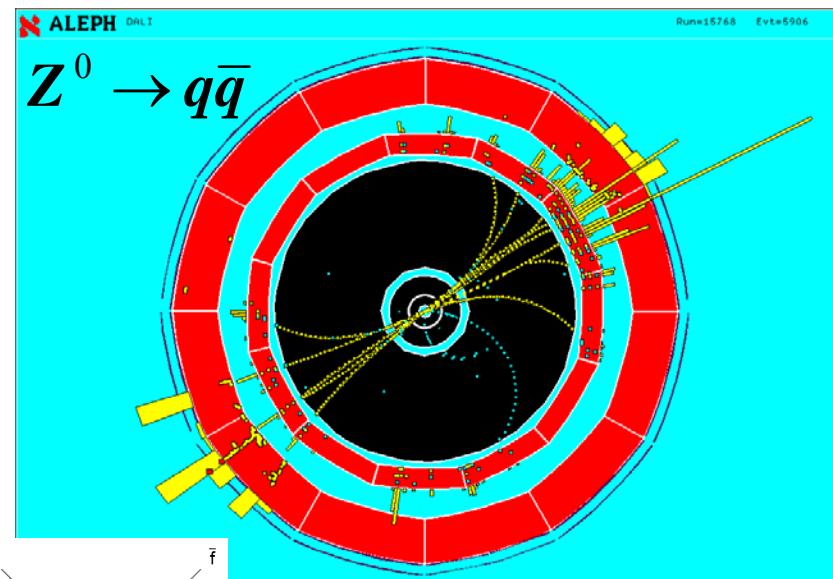
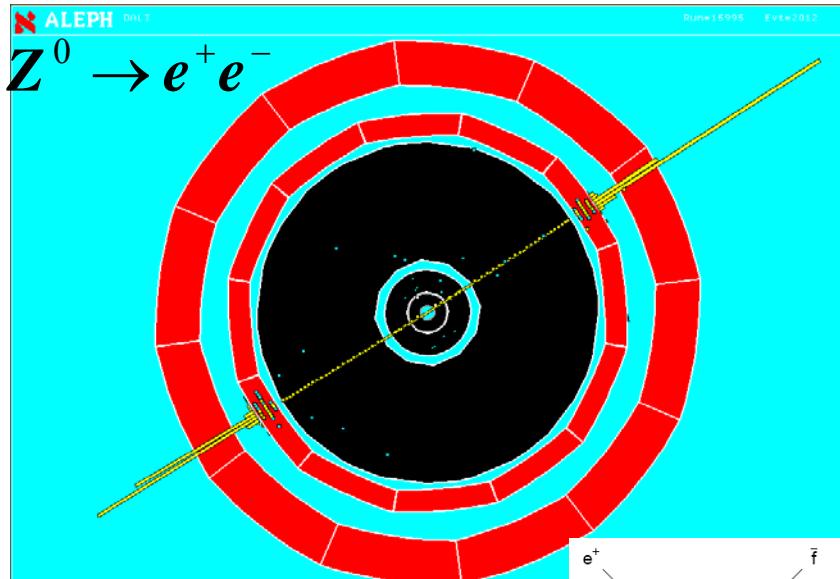
$$g_V = 2 I_3 - 4 Q \sin^2 \theta_W$$

$$g_A = 2 I_3$$

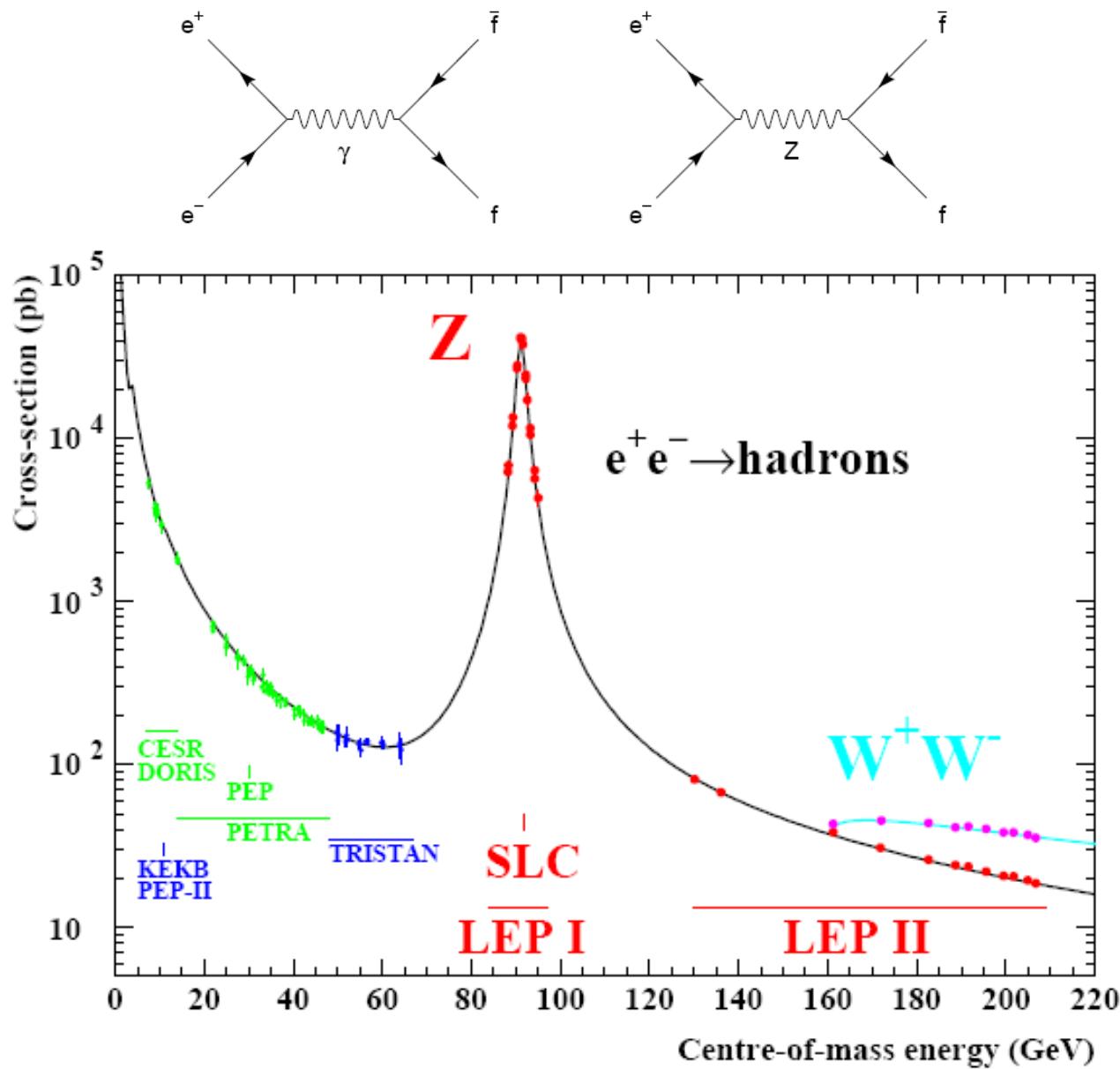
Bei $\sin^2 \theta_W \approx 1/4$ sind die Vorhersagen

	Q	I_3	g_V	g_A
ν	0	+1/2	+1	+1
e	-1	-1/2	0	-1
u, c, t	2/3	+1/2	+1/3	+1
d, s, b	-1/3	-1/2	-2/3	-1

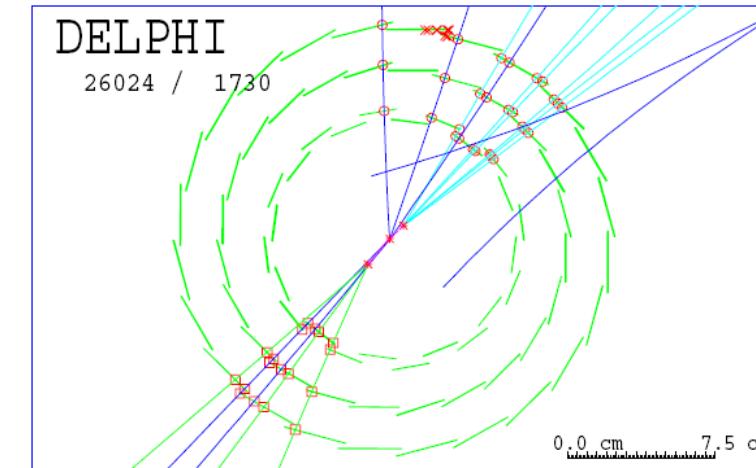
Z^0 -Zerfälle bei LEP



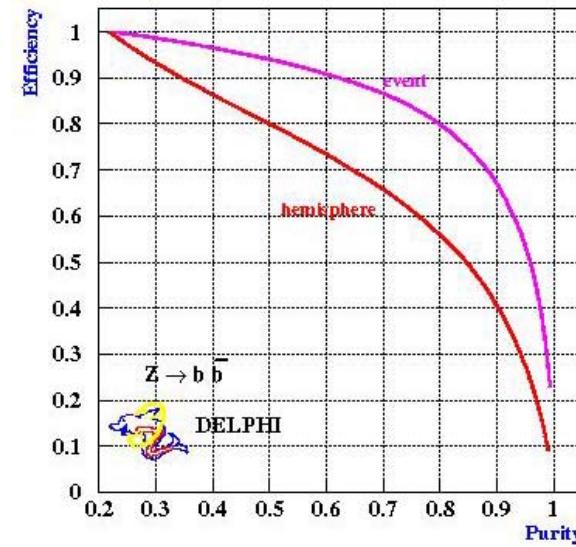
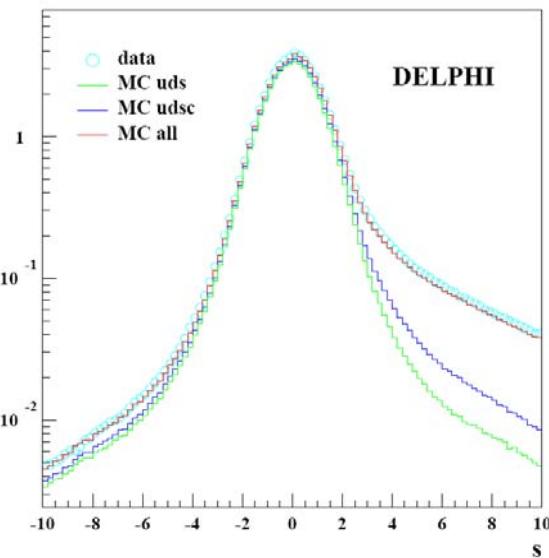
Z^0 -Resonanz



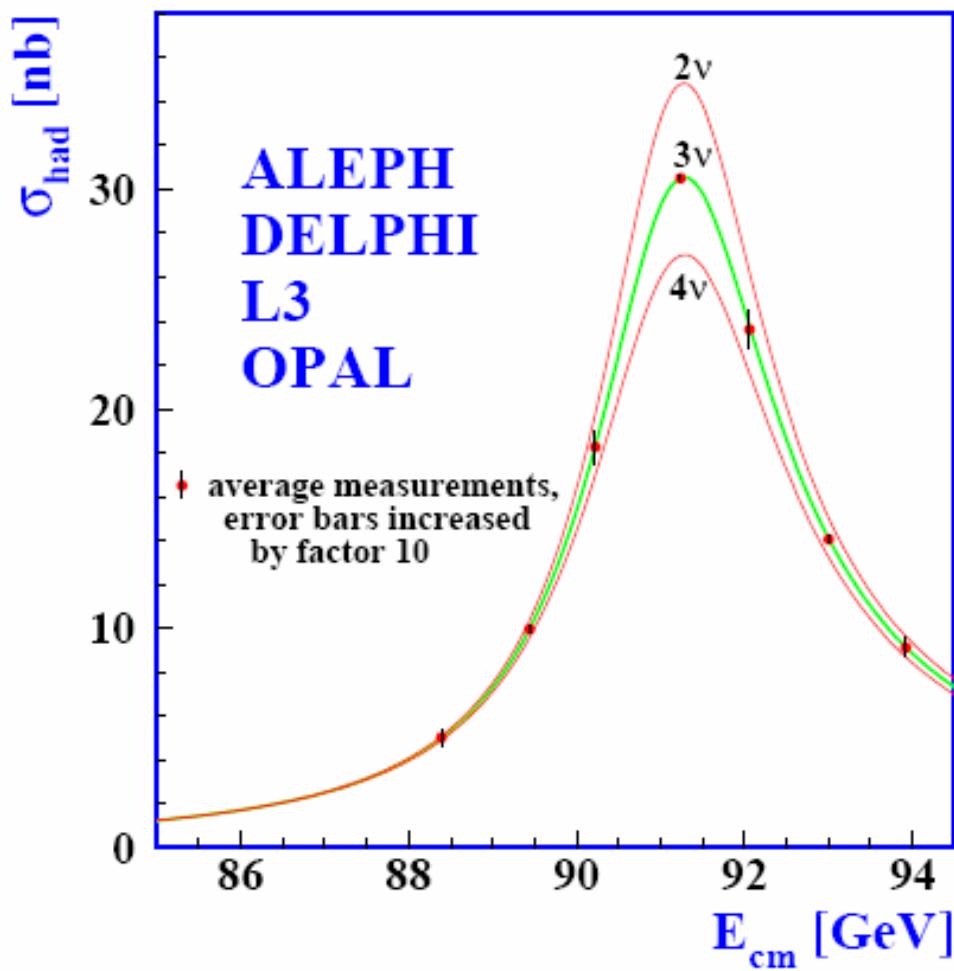
Flavour-Tagging



Impact parameter significance



Anzahl der Neutrinoarten



Partielle Breiten

Parameter $\Gamma_{f\bar{f}}$	Average [MeV]	Correlations						
Without Lepton Universality								
		Γ_{had}	Γ_{ee}	$\Gamma_{\mu\mu}$	$\Gamma_{\tau\tau}$	$\Gamma_{b\bar{b}}$	$\Gamma_{c\bar{c}}$	Γ_{inv}
Γ_{had}	1745.8 \pm 2.7	1.00						
Γ_{ee}	83.92 \pm 0.12	-0.29	1.00					
$\Gamma_{\mu\mu}$	83.99 \pm 0.18	0.66	-0.20	1.00				
$\Gamma_{\tau\tau}$	84.08 \pm 0.22	0.54	-0.17	0.39	1.00			
$\Gamma_{b\bar{b}}$	377.6 \pm 1.3	0.45	-0.13	0.29	0.24	1.00		
$\Gamma_{c\bar{c}}$	300.5 \pm 5.3	0.09	-0.02	0.06	0.05	-0.12	1.00	
Γ_{inv}	497.4 \pm 2.5	-0.67	0.78	-0.45	-0.40	-0.30	-0.06	1.00
With Lepton Universality								
		Γ_{had}	Γ_{ee}	$\Gamma_{b\bar{b}}$	$\Gamma_{c\bar{c}}$	Γ_{inv}		
Γ_{had}	1744.4 \pm 2.0	1.00						
Γ_{ee}	83.985 \pm 0.086	0.39	1.00					
$\Gamma_{b\bar{b}}$	377.3 \pm 1.2	0.35	0.13	1.00				
$\Gamma_{c\bar{c}}$	300.2 \pm 5.2	0.06	0.03	-0.15	1.00			
Γ_{inv}	499.0 \pm 1.5	-0.29	0.49	-0.10	-0.02	1.00		

5.4 Lorentz-Struktur der Z^0 -Kopplung

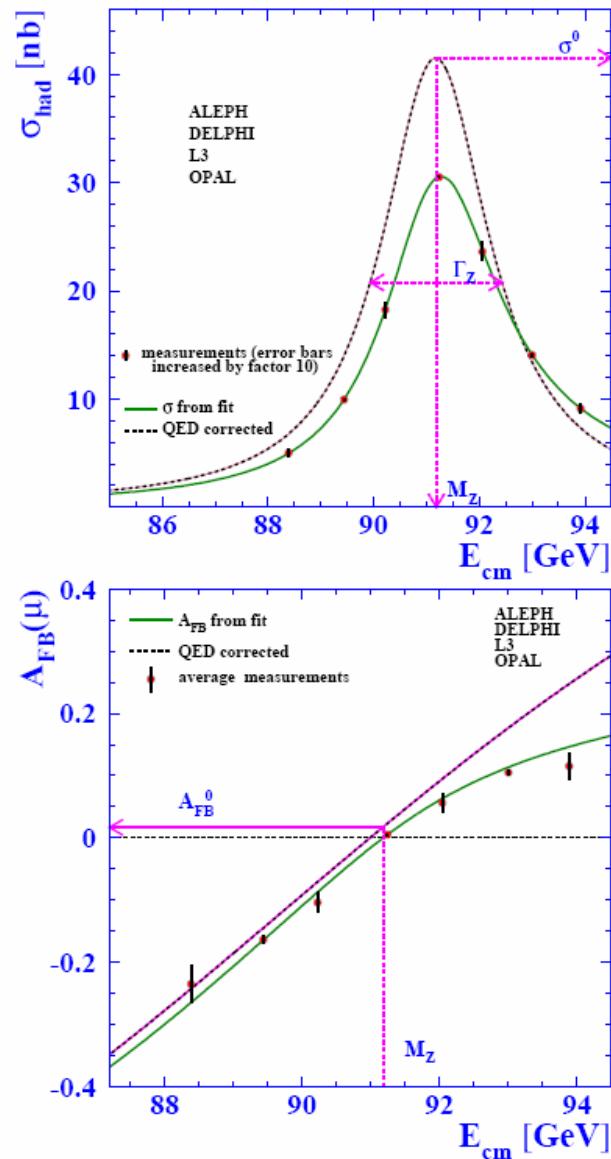
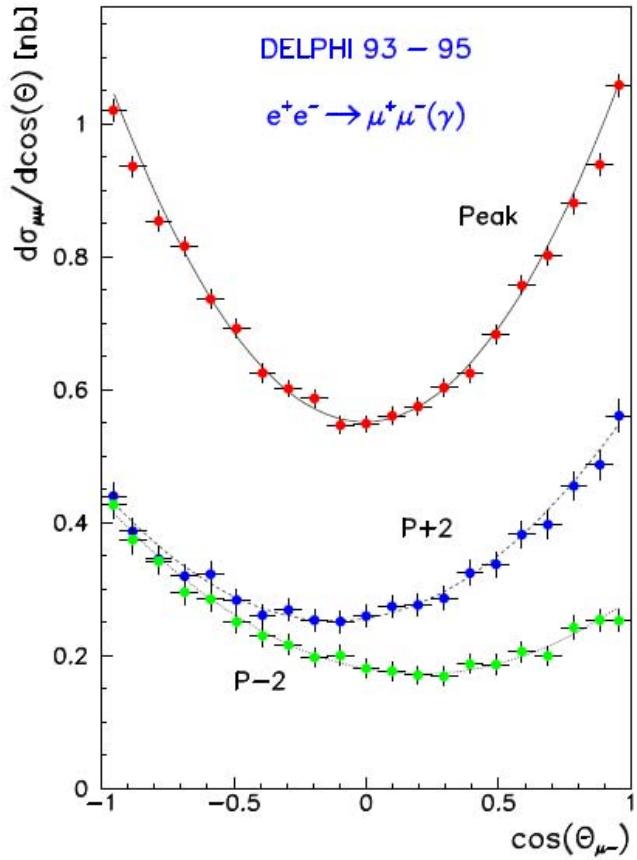
$\cos\theta$ -Verteilung

$$\begin{aligned}
 & \frac{2s}{\pi} \frac{1}{N_c^f} \frac{d\sigma_{ew}}{d\cos\theta} (e^+ e^- \rightarrow f\bar{f}) = \\
 & \underbrace{\left| \alpha(s) Q_f \right|^2 (1 + \cos^2 \theta)}_{\sigma^\gamma} \\
 & \underbrace{- 8 \Re \left\{ \alpha^*(s) Q_f \chi(s) \left[\mathcal{G}_{Ve} \mathcal{G}_{Vf} (1 + \cos^2 \theta) + 2 \mathcal{G}_{Ae} \mathcal{G}_{Af} \cos \theta \right] \right\}}_{\gamma-Z \text{ interference}} \\
 & \underbrace{+ 16 |\chi(s)|^2 [(|\mathcal{G}_{Ve}|^2 + |\mathcal{G}_{Ae}|^2)(|\mathcal{G}_{Vf}|^2 + |\mathcal{G}_{Af}|^2)(1 + \cos^2 \theta) \\
 & \quad + 8 \Re \{ \mathcal{G}_{Ve} \mathcal{G}_{Ae}^* \} \Re \{ \mathcal{G}_{Vf} \mathcal{G}_{Af}^* \} \cos \theta] }_{\sigma^Z}
 \end{aligned}$$

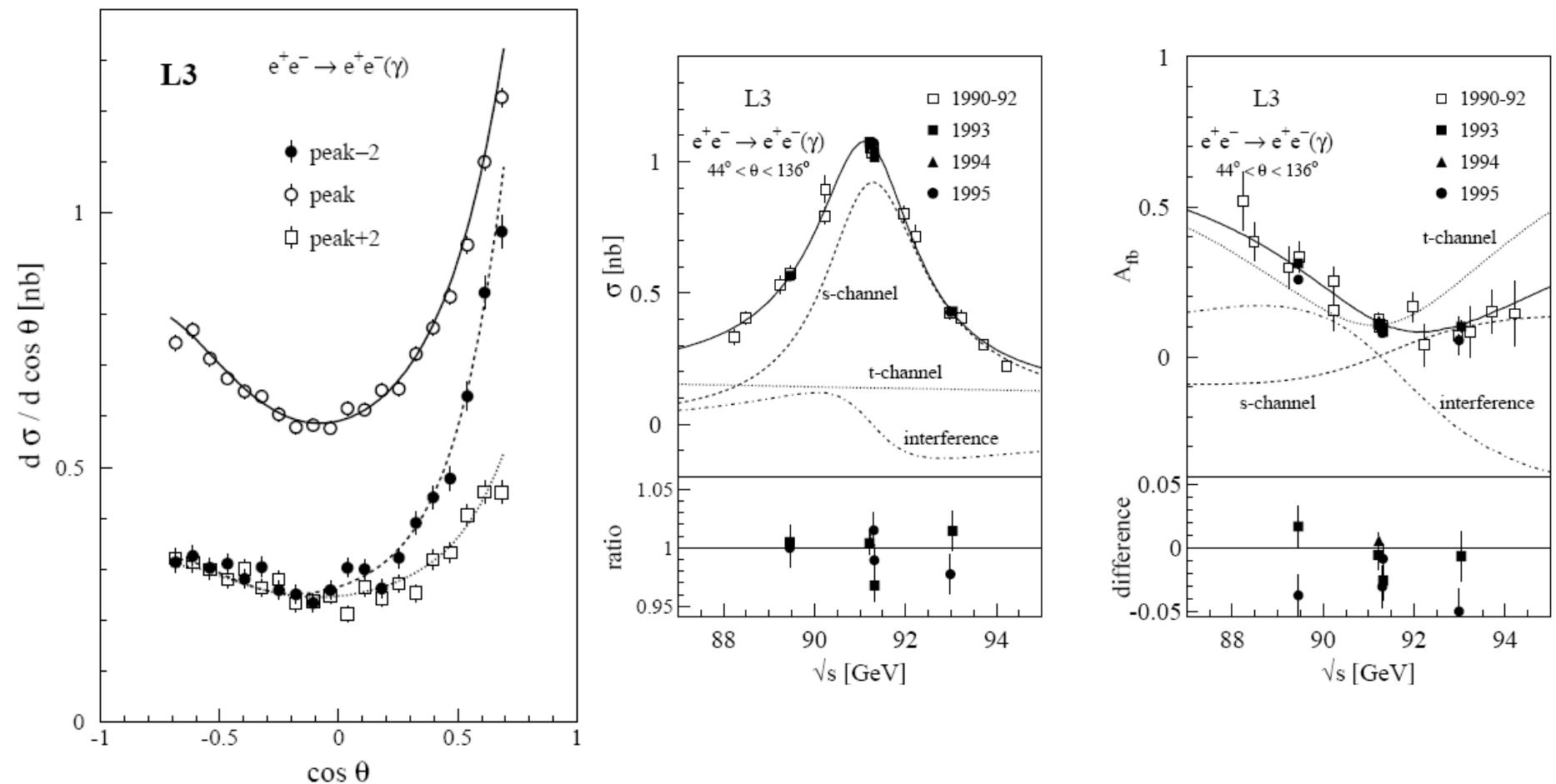
with:

$$\chi(s) = \frac{G_F m_Z^2}{8\pi\sqrt{2}} \frac{s}{s - m_Z^2 + i s \Gamma_Z / m_Z},$$

FB-Asymmetrien

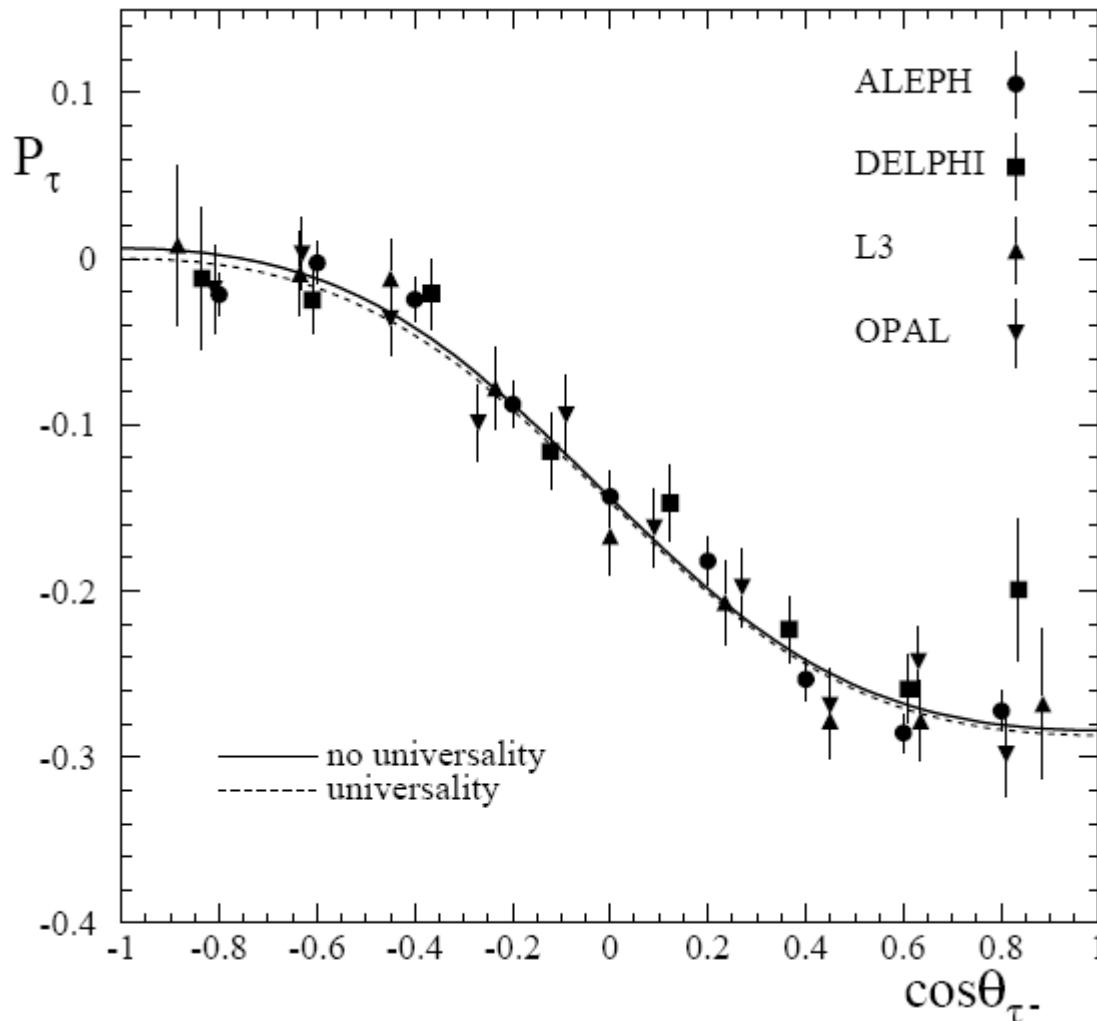


FB-Asymmetrien

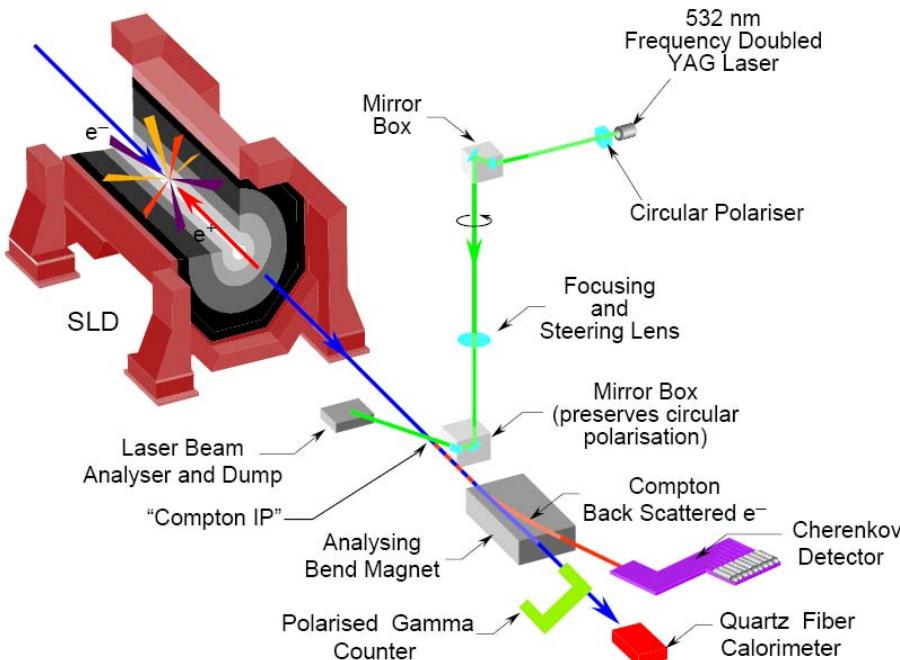


τ -Polarisation

$$\mathcal{P}_f(\cos \theta) = -\frac{\mathcal{A}_f(1 + \cos^2 \theta) + 2\mathcal{A}_e \cos \theta}{(1 + \cos^2 \theta) + 2\mathcal{A}_f \mathcal{A}_e \cos \theta}$$

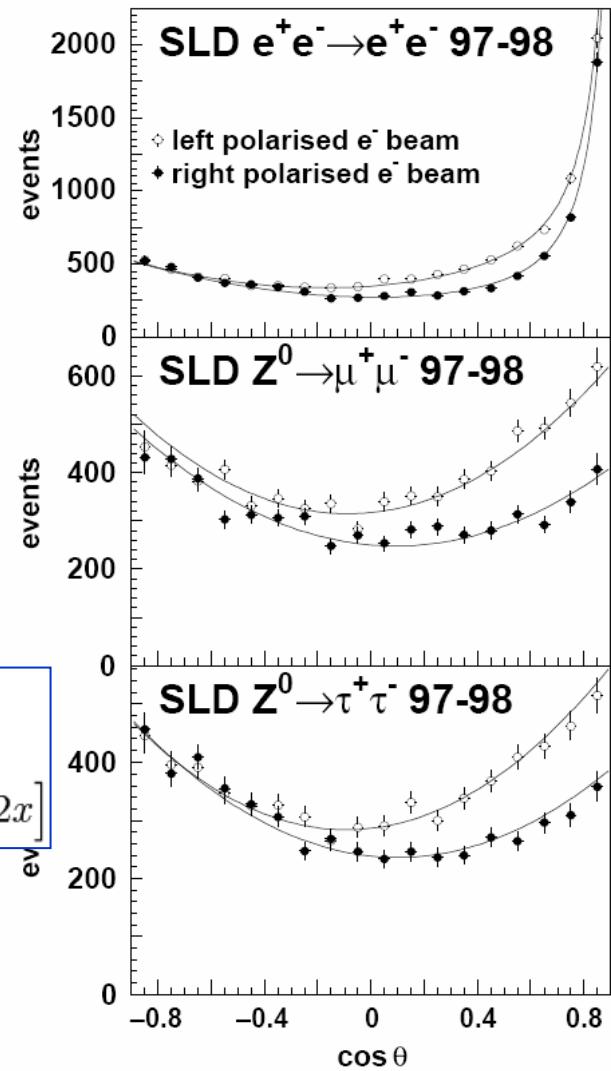


LR-Asymmetrien (SLC)



$$\begin{aligned} \frac{d}{dx}\sigma_Z(x, s, \mathcal{P}_e; \mathcal{A}_e, \mathcal{A}_\ell) &\equiv f_Z(s)\Omega_Z(x, \mathcal{P}_e; \mathcal{A}_e, \mathcal{A}_\ell) \\ &= f_Z(s) [(1 - \mathcal{P}_e \mathcal{A}_e)(1 + x^2) + (\mathcal{A}_e - \mathcal{P}_e) \mathcal{A}_\ell 2x] \end{aligned}$$

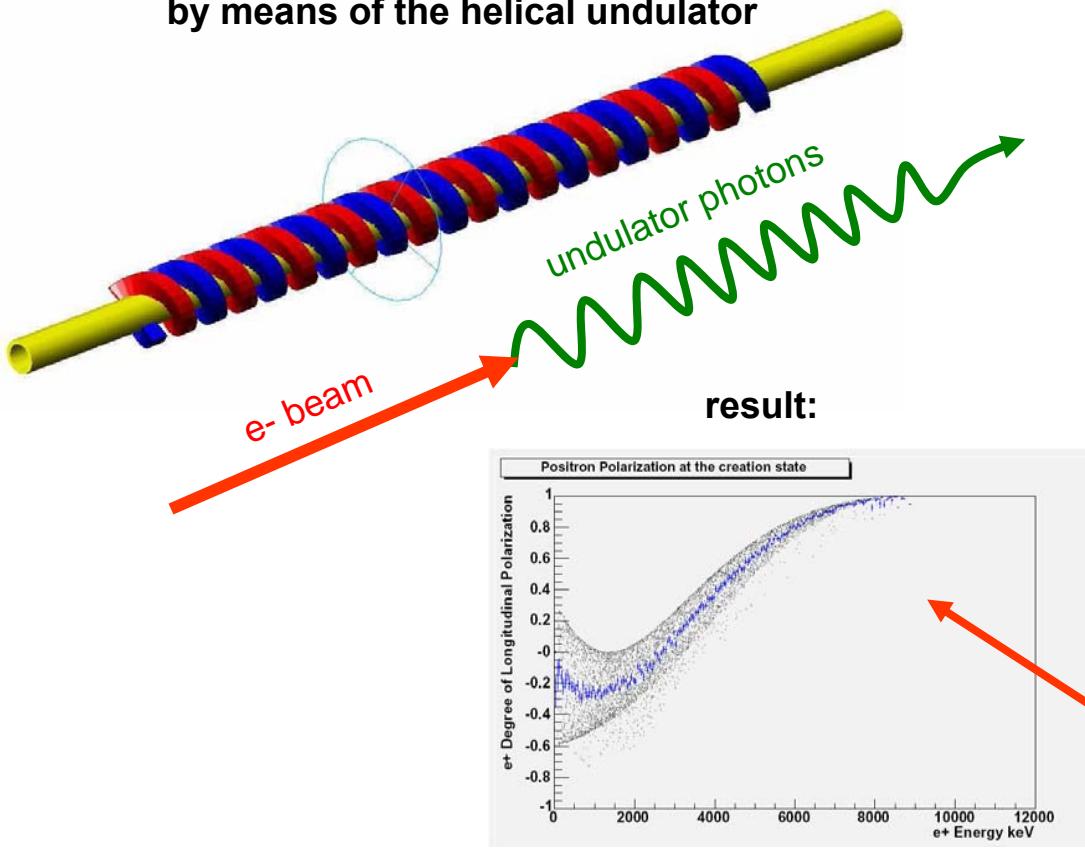
Parameter	Average	Correlations		
		\mathcal{A}_e	\mathcal{A}_μ	\mathcal{A}_τ
\mathcal{A}_e	0.1516 ± 0.0021	1.000		
\mathcal{A}_μ	0.142 ± 0.015	0.038	1.000	
\mathcal{A}_τ	0.136 ± 0.015	0.033	0.007	1.000



polarized positrons

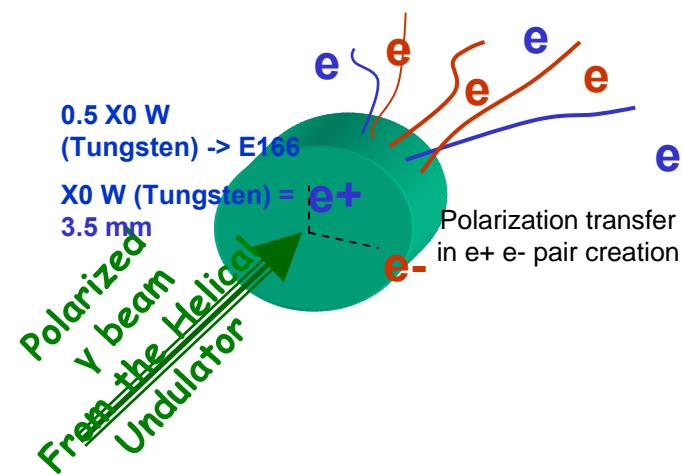
- **polarized positrons:** production and measurement of polarization before the main linac, i.e. at low energies

A: production of polarized photons by means of the helical undulator



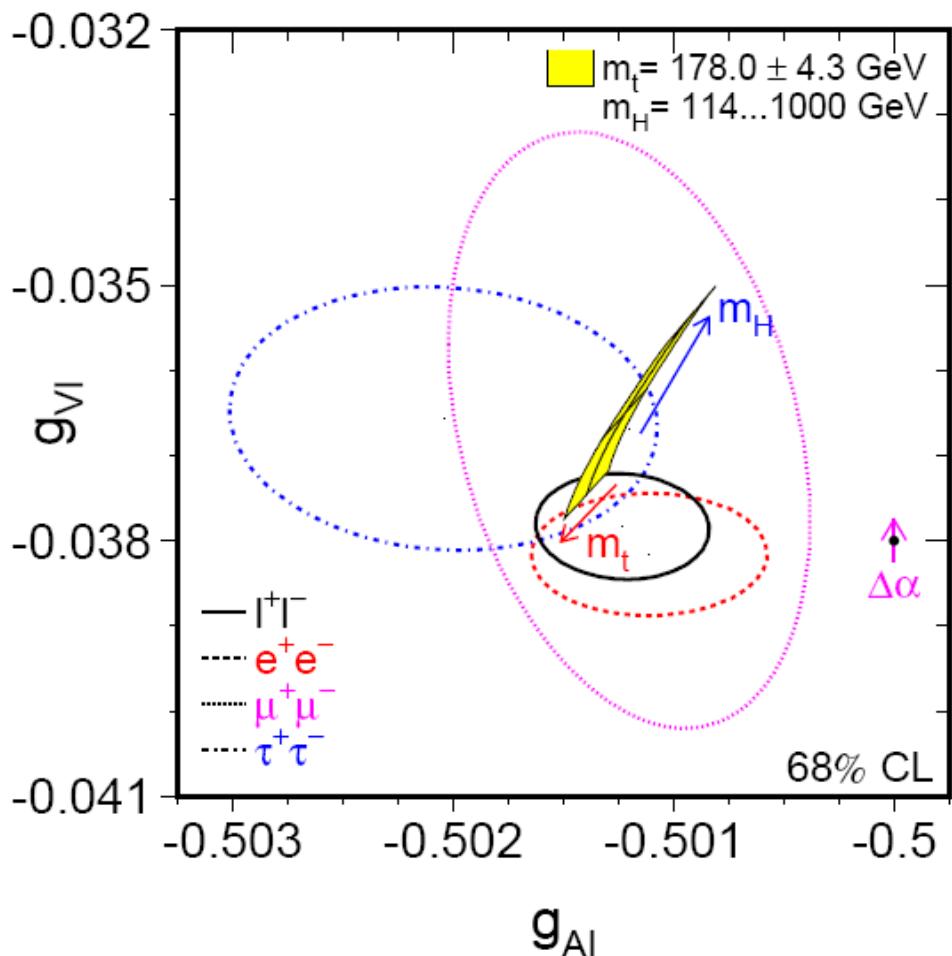
Positron Polarization profile created by the undulator photons

B: production of polarized positrons by polarized photons



C: measure the polarization degree at different energies

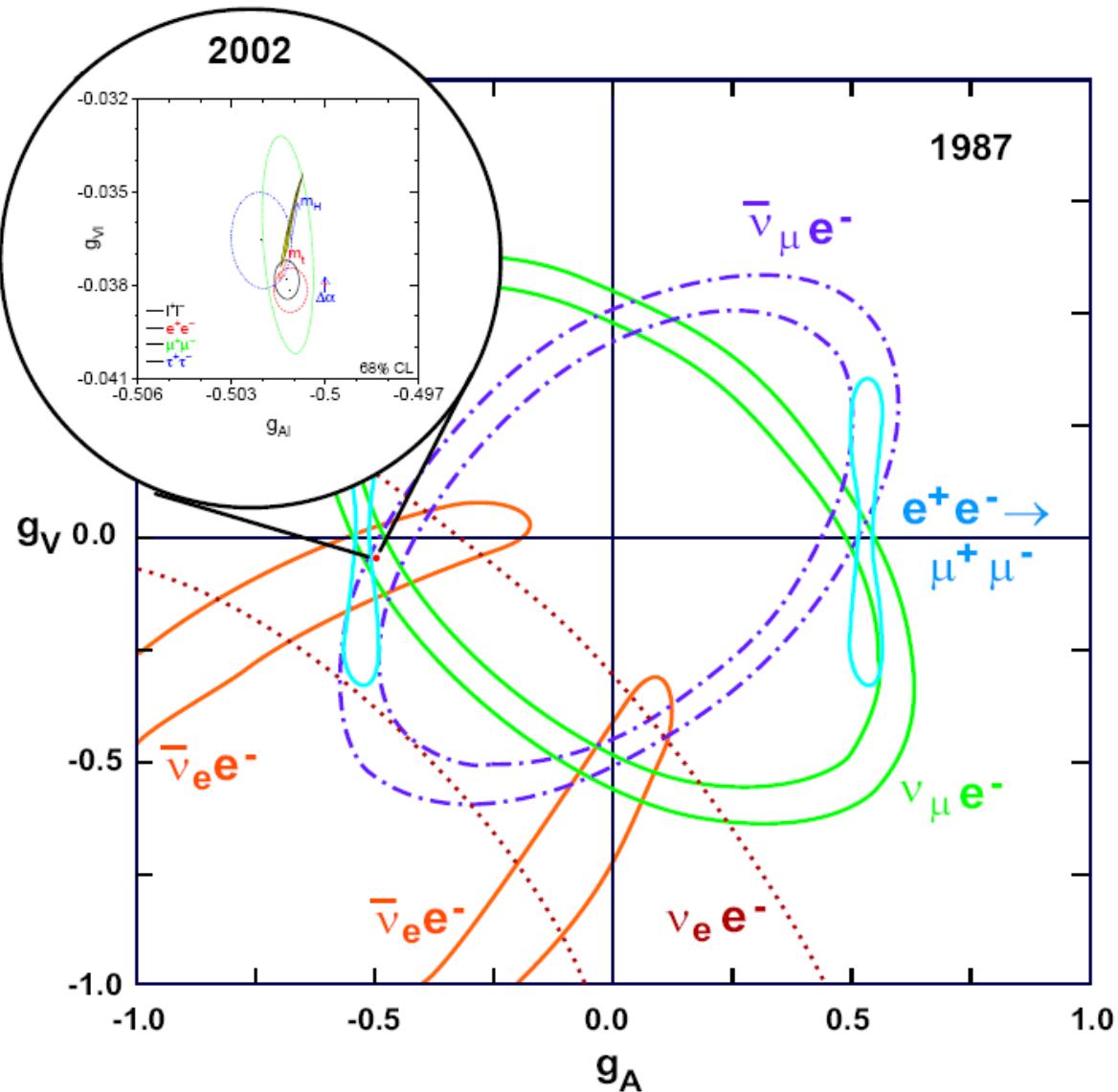
g_V, g_A Messungen



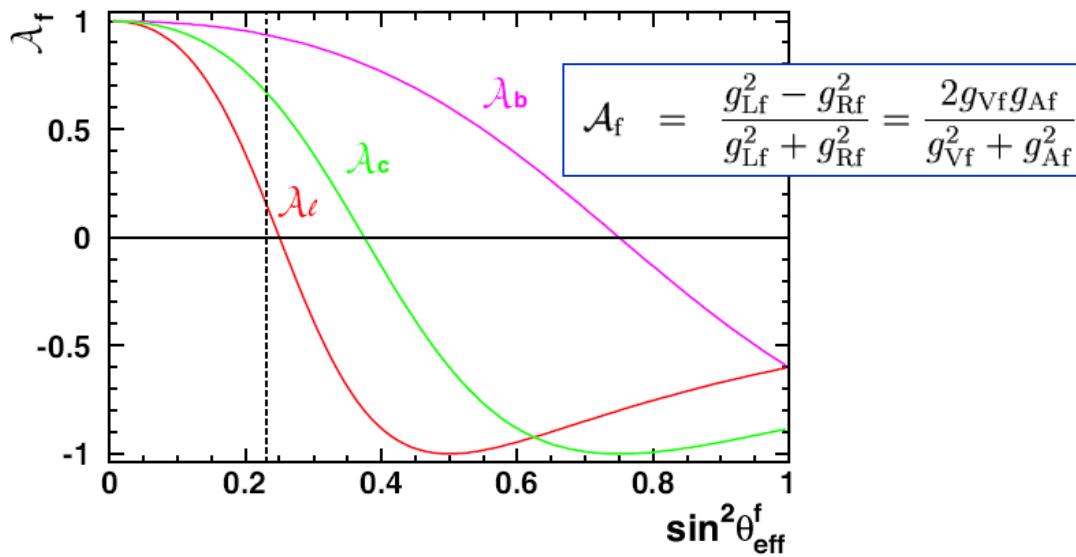
Parameter	Average	Correlations		
		g_ν	$g_{A\ell}$	$g_{V\ell}$
$g_{A\nu} \equiv g_{V\nu}$	$+0.50076 \pm 0.00076$	1.00		
$g_{A\ell}$	-0.50123 ± 0.00026	-0.48	1.00	
$g_{V\ell}$	-0.03783 ± 0.00041	-0.03	-0.06	1.00

Parameter	Average	Correlations		
		$g_{L\nu}$	$g_{L\ell}$	$g_{R\ell}$
$g_{L\nu}$	$+0.50076 \pm 0.00076$	1.00		
$g_{L\ell}$	-0.26953 ± 0.00024	-0.29	1.00	
$g_{R\ell}$	$+0.23170 \pm 0.00025$	0.22	0.43	1.00

g_V, g_A Messungen vor und nach LEP



Sensitivität der Asymmetrien auf $\sin^2 \theta_W$

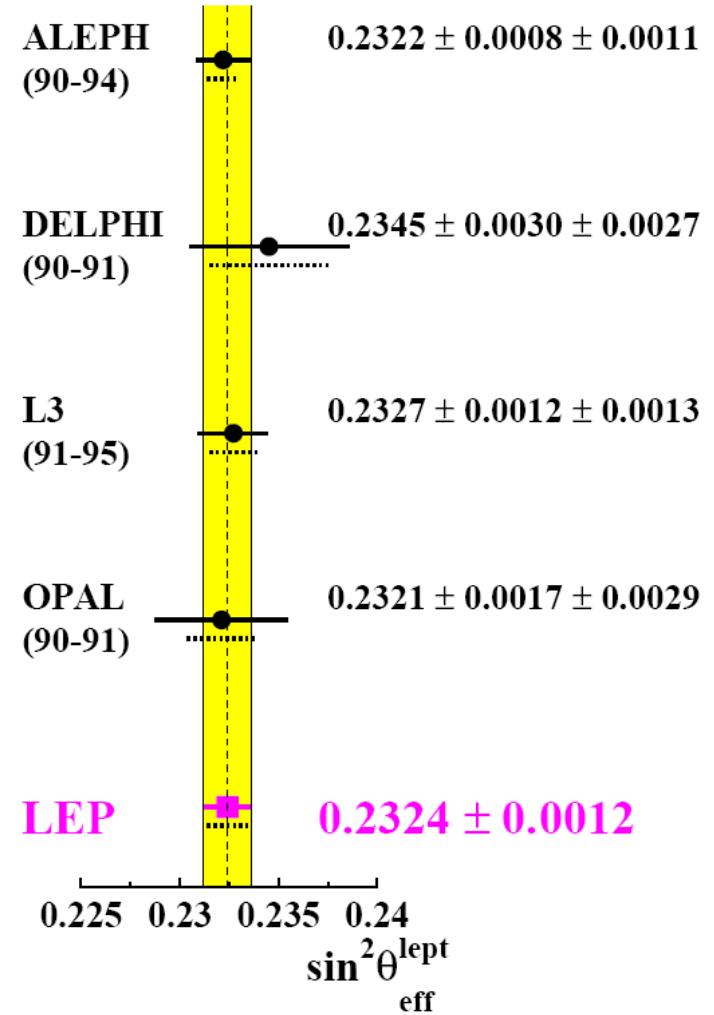


$$g_V = 2I_3 - 4Q \sin^2 \theta_W$$

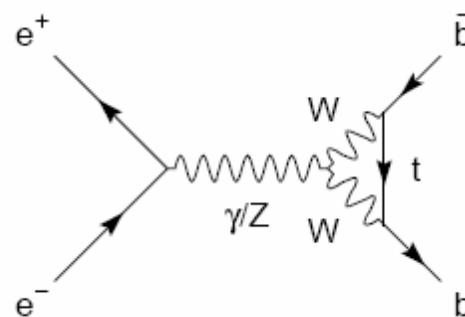
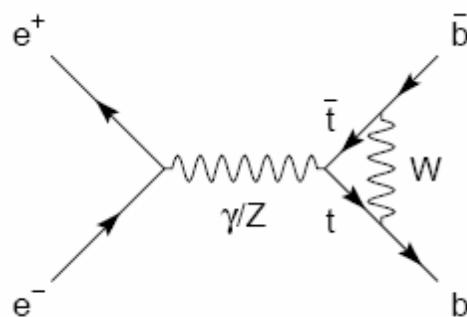
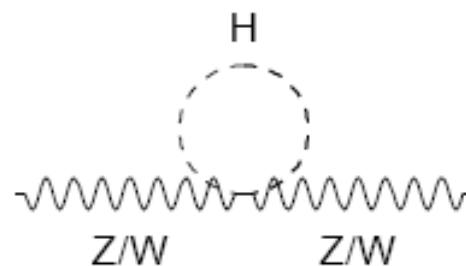
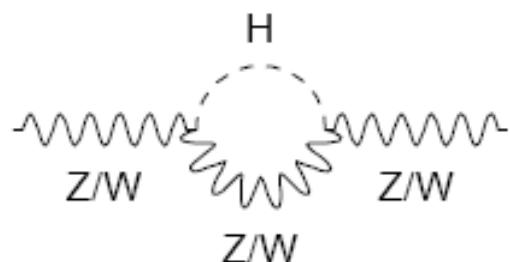
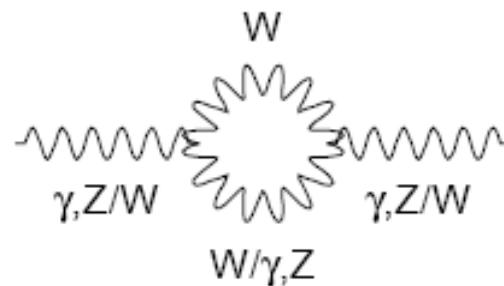
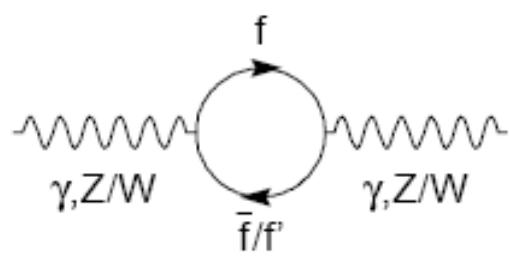
$$g_A = 2I_3$$

$\sin^2 \theta_W \approx 1/4$ sind die Vorhersagen

	Q	I_3	g_V	g_A
ν	0	+1/2	+1	+1
e	-1	-1/2	0	-1
u, c, t	2/3	+1/2	+1/3	+1
d, s, b	-1/3	-1/2	-2/3	-1



Strahlungskorrekturen: Präzisionstests

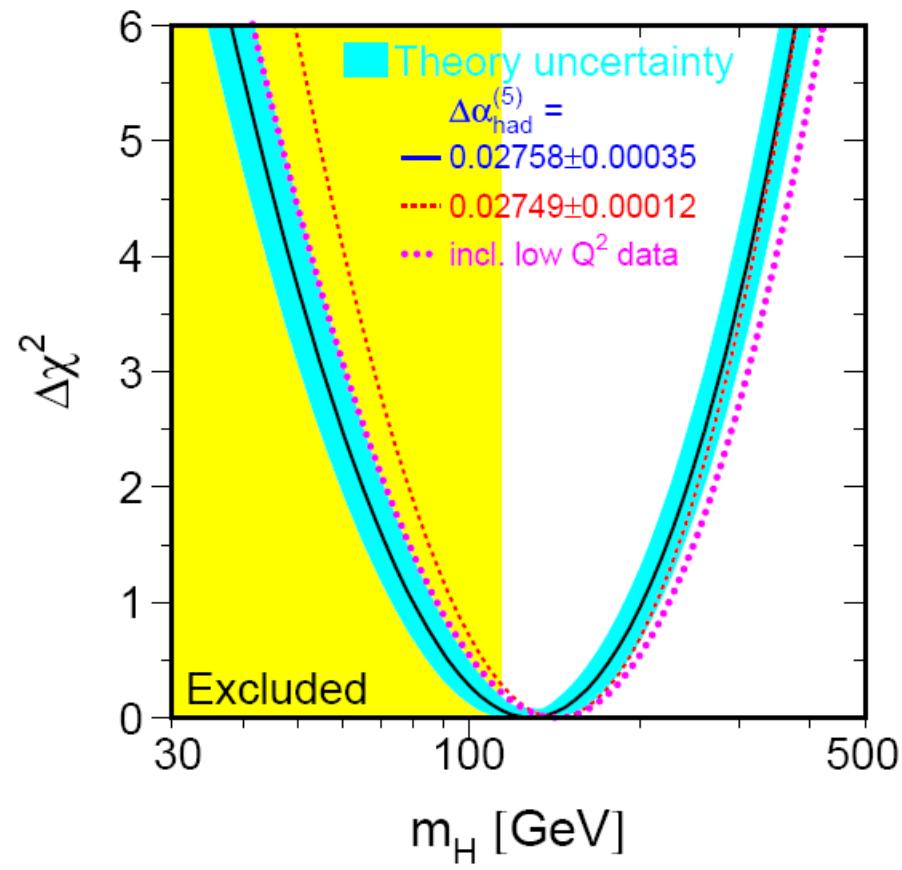
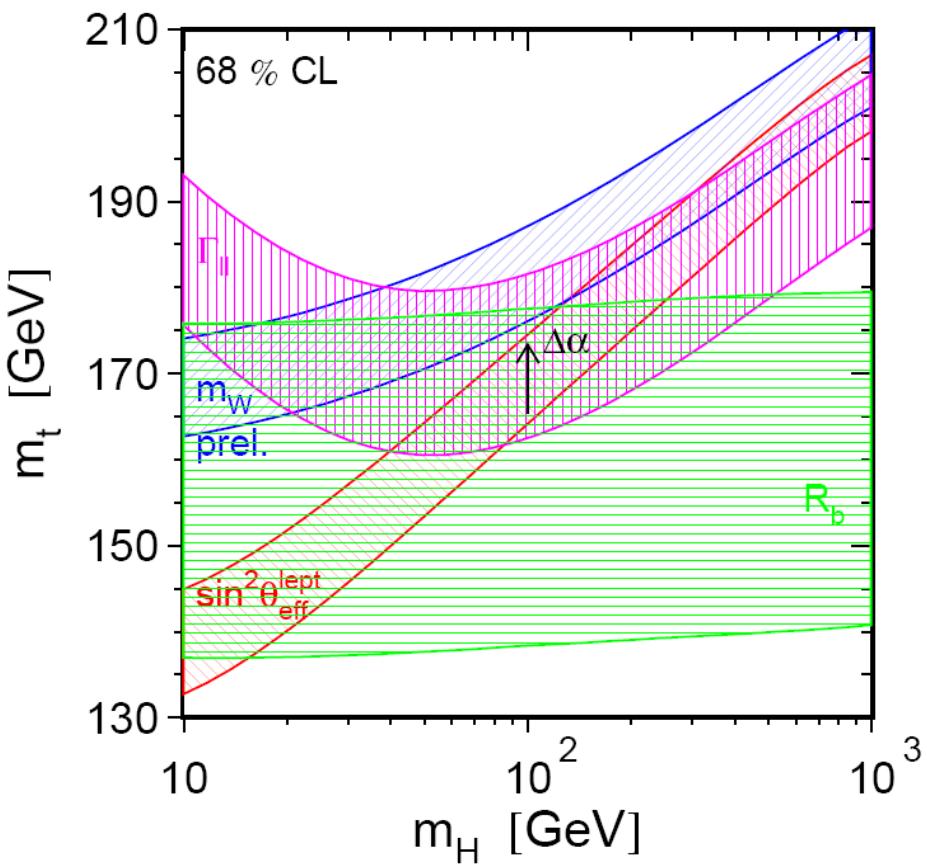


The Standard Model
is a non-trivial
structure with a few
constants showing up
in many places:
Many opportunities
to check !

In perturbation theory
all these parameters
tend to get connected
and influenced by the
mass scale they
are considered at

$$\begin{aligned}
\mathcal{L}_{\text{SM}} = & -\frac{1}{2} \partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\mu^a g_\mu^b g_\nu^c - \frac{1}{4} g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \frac{1}{2} i g_s^2 (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c \\
& - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - M^2 W_\mu^+ W_\mu^- - \frac{1}{2} \partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2 c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2} \partial_\mu A_\nu \partial_\nu A_\mu - \frac{1}{2} \partial_\mu H \partial_\mu H - \frac{1}{2} m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- \\
& - M^2 \phi^+ \phi^- - \frac{1}{2} \partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2 c_w^2} M \phi^0 \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2} \alpha_h \\
& - i g c_w \left[\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+) \right] \\
& - i g s_w \left[\partial_\nu A_\mu (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+) \right] \\
& - \frac{1}{2} g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2} g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 \left(Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\mu^+ W_\nu^- \right) + g^2 s_w^2 \left(A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^- \right) \\
& + g^2 s_w c_w \left[A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - 2A_\mu Z_\mu^0 W_\nu^+ W_\nu^- \right] - g \alpha \left[H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^- \right] \\
& - \frac{1}{8} g^2 \alpha_h \left[H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2 \right] - g M W_\mu^+ W_\mu^- H - \frac{1}{2} g \frac{M}{c_w^2} Z_\mu^0 Z_\mu^0 H \\
& - \frac{1}{2} i g \left[W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0) \right] + \frac{1}{2} g \left[W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) - W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H) \right] \\
& + \frac{1}{2} g \frac{1}{c_w} Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - i g \frac{s_w}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + i g s_w M A_\mu (W_\mu^+ \phi^- - W_\mu^- \phi^+) - i g \frac{1 - 2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- \\
& - \phi^- \partial_\mu \phi^+) + i g s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W_\mu^+ W_\mu^- \left[H^2 + (\phi^0)^2 + 2\phi^+ \phi^- \right] - \frac{1}{4} g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 [H^2 + (\phi^0)^2 \\
& + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2} g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2} i g^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2} g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) \\
& + \frac{1}{2} i g^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - e^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{v}^\lambda \gamma \partial v^\lambda \\
& - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + i g s_w A_\mu [-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3} (\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3} (\bar{d}_j^\lambda \gamma^\mu d_j^\lambda)] \\
& + \frac{i g}{4 c_w} Z_\mu^0 \left[(\bar{v}^\lambda \gamma^\mu (1 + \gamma^5) v^\lambda) + (\bar{e}^\lambda \gamma^\mu (4 s_w^2 - 1 - \gamma^5) e^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (\frac{4}{3} s_w^2 - 1 - \gamma^5) u_j^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (1 - \frac{8}{3} s_w^2 - \gamma^5) d_j^\lambda) \right] \\
& + \frac{i g}{2\sqrt{2}} W_\mu^+ \left[(\bar{v}^\lambda \gamma^\mu (1 + \gamma^5) v^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa) \right] + \frac{i g}{2\sqrt{2}} W_\mu^- \left[(\bar{e}^\lambda \gamma^\mu (1 + \gamma^5) e^\lambda) + (\bar{d}_j^\kappa C_{\lambda\kappa}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda) \right] \\
& + \frac{i g}{2\sqrt{2}} \frac{m_e^\lambda}{M} \left[-\phi^+ (\bar{v}^\lambda (1 - \gamma^5) v^\lambda) + \phi^- (\bar{e}^\lambda (1 + \gamma^5) e^\lambda) \right] - \frac{g}{2} \frac{m_e^\lambda}{M} \left[H (\bar{e}^\lambda e^\lambda) + i \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) \right] \\
& + \frac{i g}{2M\sqrt{2}} \phi^+ \left[-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) \right] + \frac{i g}{2M\sqrt{2}} \phi^- \left[m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) \right] \\
& - \frac{g}{2} \frac{m_e^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \frac{i g}{2} \frac{m_u^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{i g}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- \\
& + \bar{X}^0 \left(\partial^2 - \frac{M^2}{c_w^2} \right) X^0 + \bar{Y} \partial^2 Y + i g c_w W_\mu^+ (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + i g s_w W_\mu^+ (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ Y) + i g c_w W_\mu^- (\partial_\mu \bar{X}^- X^0 - \partial_\mu \bar{X}^0 X^-) \\
& + i g s_w W_\mu^- (\partial_\mu \bar{X}^- Y - \partial_\mu \bar{Y} X^+) + i g c_w Z_\mu^0 (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) + i g s_w A_\mu (\partial_\mu \bar{X}^+ X^+ - \partial_\mu \bar{X}^- X^-) - \frac{1}{2} g M |\bar{X}^+ X^+ H + \bar{X}^- X^- H| \\
& + \frac{1}{c_w^2} \bar{X}^0 X^0 H + \frac{1 - 2c_w^2}{2c_w} i g M |\bar{X}^+ X^0 \phi^+ - \bar{X}^- X^0 \phi^-| + \frac{1}{2c_w} i g M |\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-| + i g M s_w |\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-| \\
& + \frac{1}{2} i g M |\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0|
\end{aligned}$$

Einschränkungen für die Higgs-Masse



Übereinstimmung mit dem SM

