

DIS: The Status of Parton Densities and Λ_{QCD}

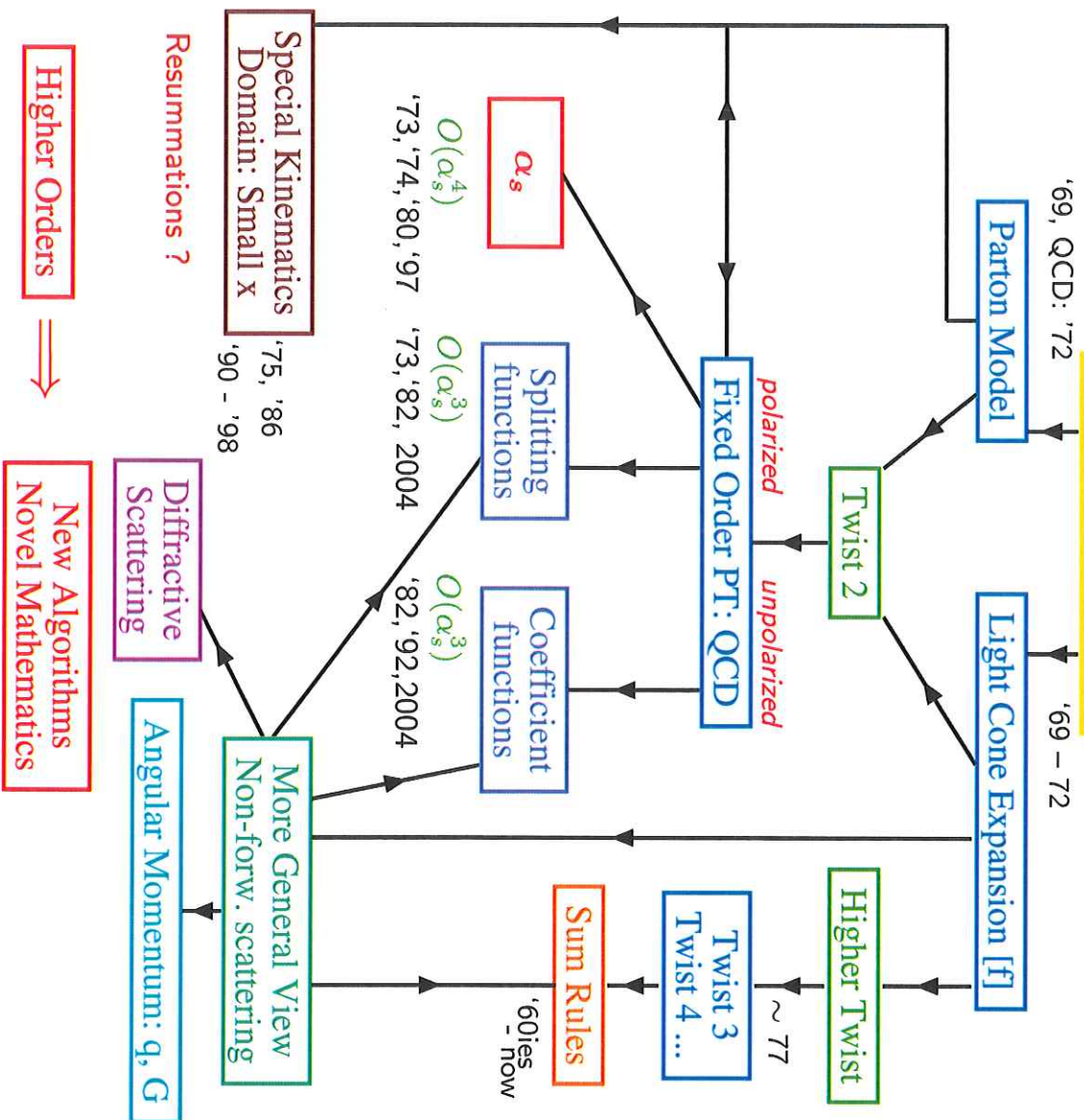
Johannes Blümlein
DESY



- Unpolarized Deeply Inelastic Scattering
- Polarized Deeply Inelastic Scattering
- Λ_{QCD} and $\alpha_s(M_Z^2)$
- Future Avenues

Dedicated to the memory of Jiro Kodaira.

Theory of DIS



Highest order corrections of HO QCD

- Running α_s : $O(\alpha_s^4)$ Larin, van Ritbergen, Vermaseren 1997
- Unpol. anomalous dimensions and Wilson coefficients: $O(\alpha_s^3)$
Moch, Vermaseren, Vogt 2004/05
- Unpol. NS anomalous dimension 2nd Moment: $O(\alpha_s^4)$ Baikov, Chetyrkin 2006
- Pol. anomalous dimension: $O(\alpha_s^2)$; ΔP_{NS}^{qq} , ΔP_{qG} : $O(\alpha_s^3)$ Mertig, van Neerven, 1995; Vogelsang 1995; Moch, Vermaseren, Vogt
- Pol. Wilson coefficients: $O(\alpha_s^2)$; ΔC_{NS}^{qq} , ΔC_{qG} : van Neerven, Zijlstra 1994 $O(\alpha_s^3)$ to come
- Transversity: $O(\alpha_s^2)$, some moments anom. dim.: $O(\alpha_s^3)$, Hayashigaki, Kanazawa, Koike; Kumano, Miyama; Vogelsang: 1997; Gracey 2006
- Unpol. Heavy Flavor Wilson Coefficients: $O(\alpha_s^2)$ Laenen, van Neerven, Riemersma, Smith, 1993
- Pol. Heavy Flavor Wilson Coefficients: $O(\alpha_s^1)$, Watson 1982
- $Q^2 \gg m^2$ Pol. Heavy Flavor Wilson Coefficient : $O(\alpha_s^2)$ van Neerven, Smith et al. 1996
- $Q^2 \gg m^2$ Unpol. Heavy Flavor Wilson Coefficient F_L : $O(\alpha_s^3)$

Blümlein, De Freitas, van Neerven, S. Klein 2005

The Basic Functions of massless QCD to $w=5$: \equiv 3 Loops

Representative : $S_1(N) = \psi(N+1) + \gamma_E$ and its derivatives.

Weight $w=3$:

$$F_1(N) = \mathbf{M} \left[\frac{\ln(1+x)}{1+x} \right] (N)$$

$$F_2(N) = \mathbf{M} \left[\frac{Li_2(x)}{1+x} \right] (N), \quad F_3(N) = \mathbf{M} \left[\left(\frac{Li_2(x)}{1-x} \right)_+ \right] (N)$$

Yndurain et al., 1981: $F_2(N)$

Weight $w=4$:

$$F_4(N) = \mathbf{M} \left[\frac{S_{1,2}(x)}{1+x} \right] (N), \quad F_5(N) := \mathbf{M} \left[\left(\frac{S_{1,2}(x)}{1-x} \right)_+ \right] (N)$$

$F_3(N) - F_5(N)$: J.B., S. Moch, 2003; J.B., V. Ravindran, 2004

Weight w=5 :

$$F_{6,7}(N) = \mathbf{M} \left[\left(\frac{\text{Li}_4(x)}{1 \pm x} \right)_{(+)} \right] (N), \quad F_8(N) = \mathbf{M} \left[\frac{S_{1,3}(x)}{1+x} \right] (N),$$

$$F_{9,10}(N) = \mathbf{M} \left[\left(\frac{S_{2,2}(x)}{1 \pm x} \right)_{(+)} \right] (N), \quad F_{11}(N) = \mathbf{M} \left[\frac{\text{Li}_2^2(x)}{1+x} \right] (N),$$

$$F_{12,13}(N) := \mathbf{M} \left[\left(\frac{S_{2,2}(-x) - \text{Li}_2^2(-x)/2}{1 \pm x} \right)_{(+)} \right] (N)$$

$F_6(N) - F_{13}(N)$: J.B., S. Moch, 2004.

Massless QCD to 3 Loops depends on 14 Functions.

DIS: Microscopy of the Nucleon

- determination of all quark densities and the gluon distribution
- determination of all polarized parton densities

DIS: Fundamental Tests of QCD

- precision measurement of Λ_{QCD} and $\alpha_s(M_Z^2)$
- Thorough verification of the prediction of the light cone expansion: to higher twist
- Test of linear and non-linear resummations

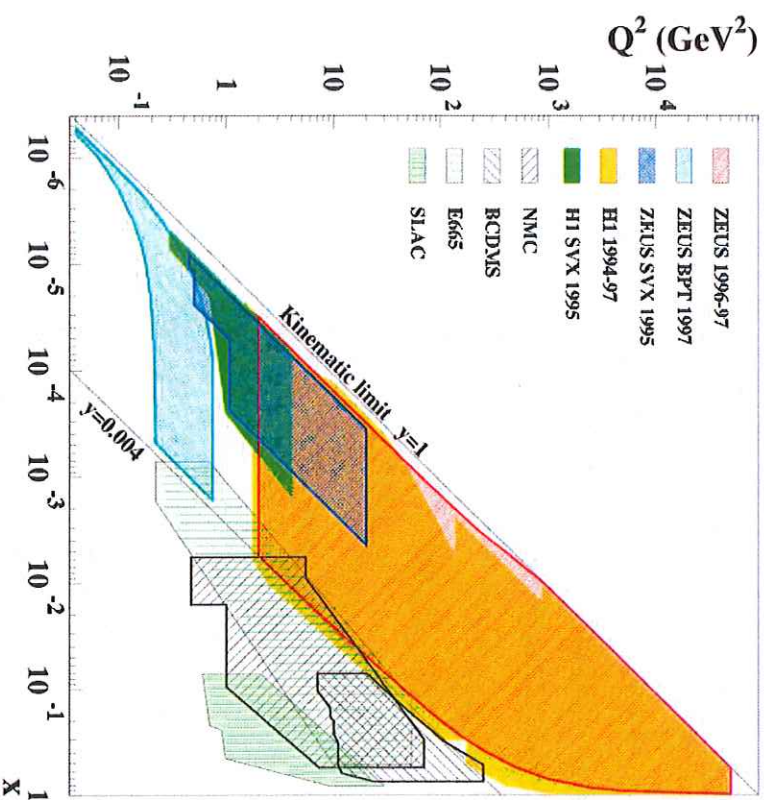
Challenges for Theory: perturbative and non-perturbative

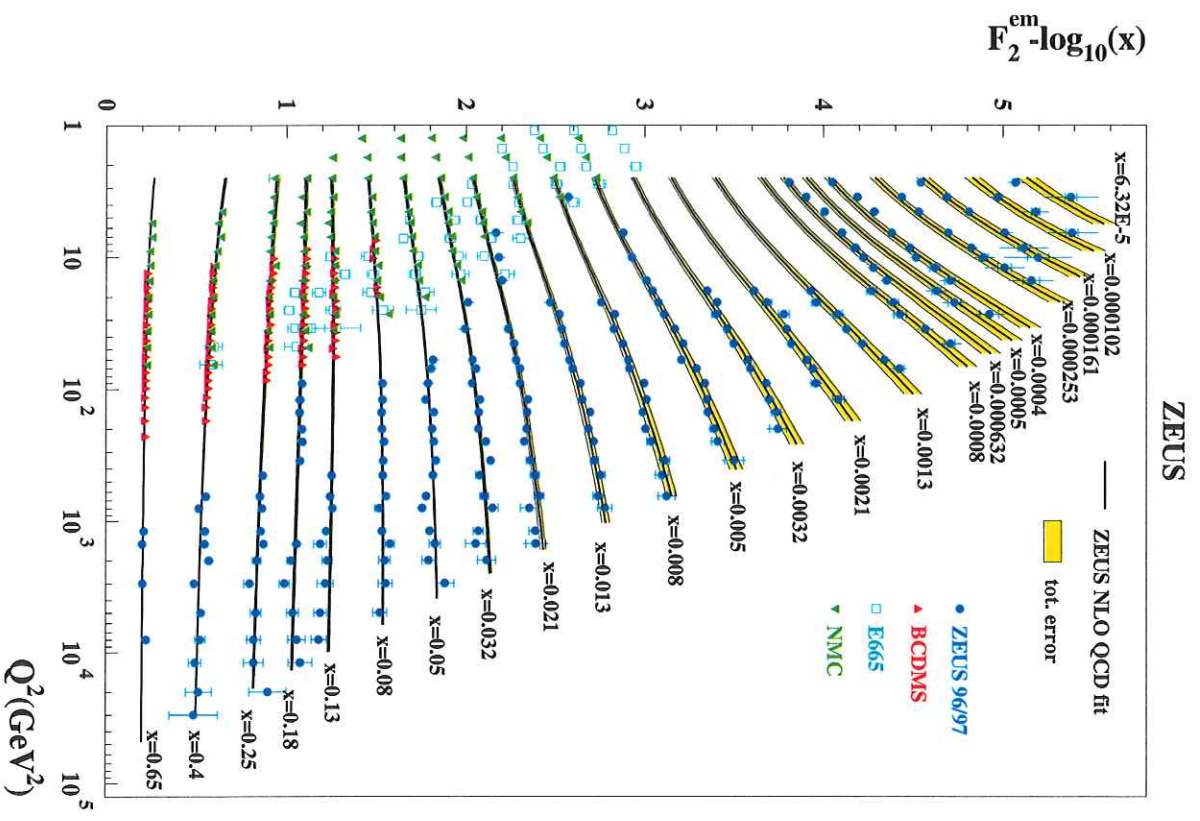
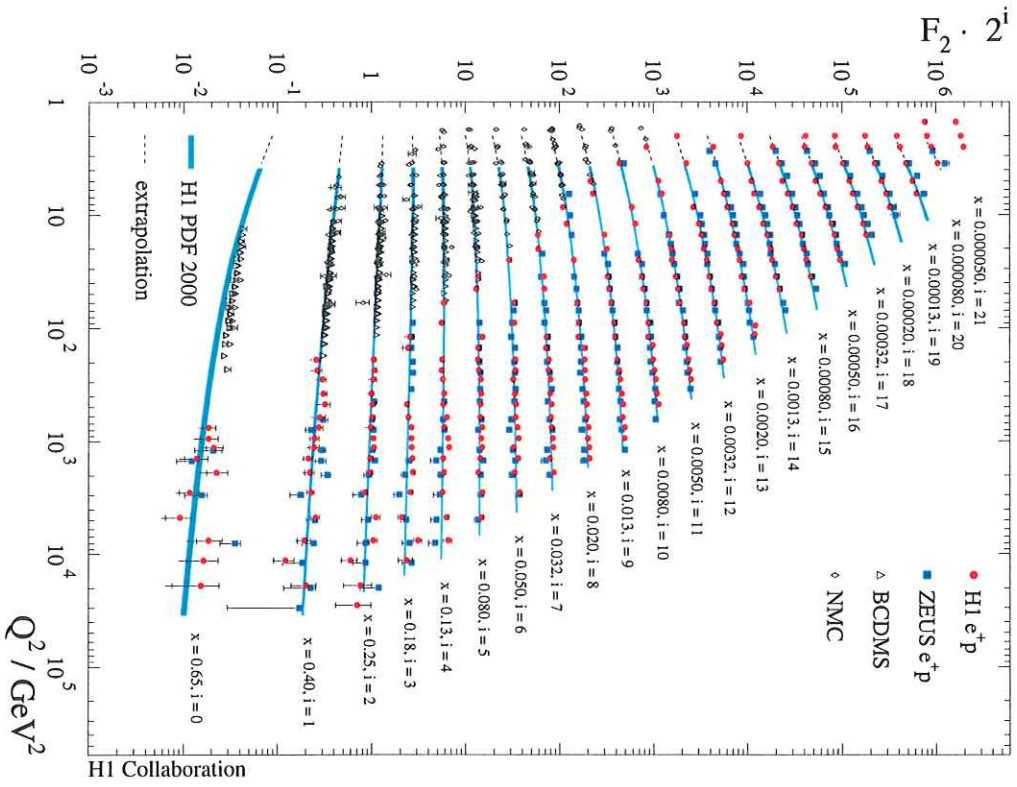
- higher order precision calculations and data analysis
- Lattice gauge theory results for hadronic matrix elements

1. Unpolarized Parton Distributions

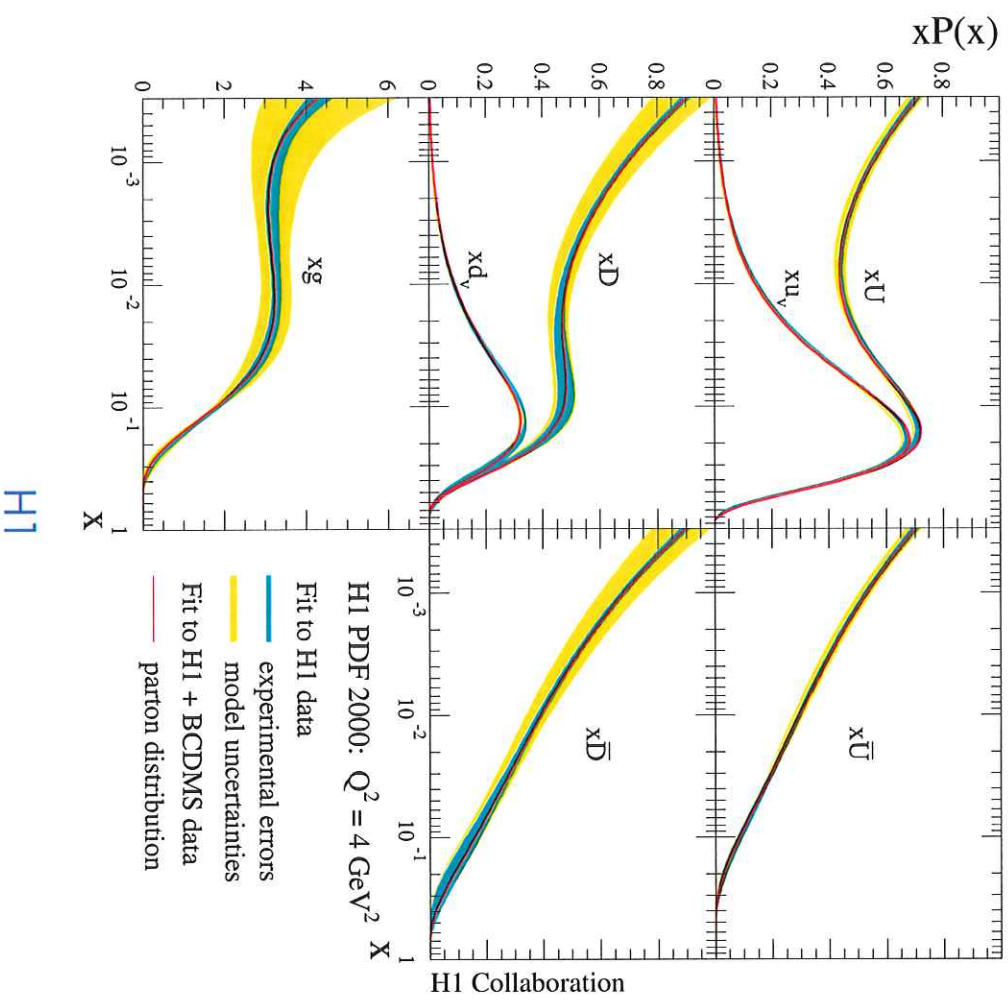
DIS range
Nucleon structure:

$$10^{-5} < x < 0.9, \\ 1 < Q^2 < 50.000 \text{ GeV}^2$$

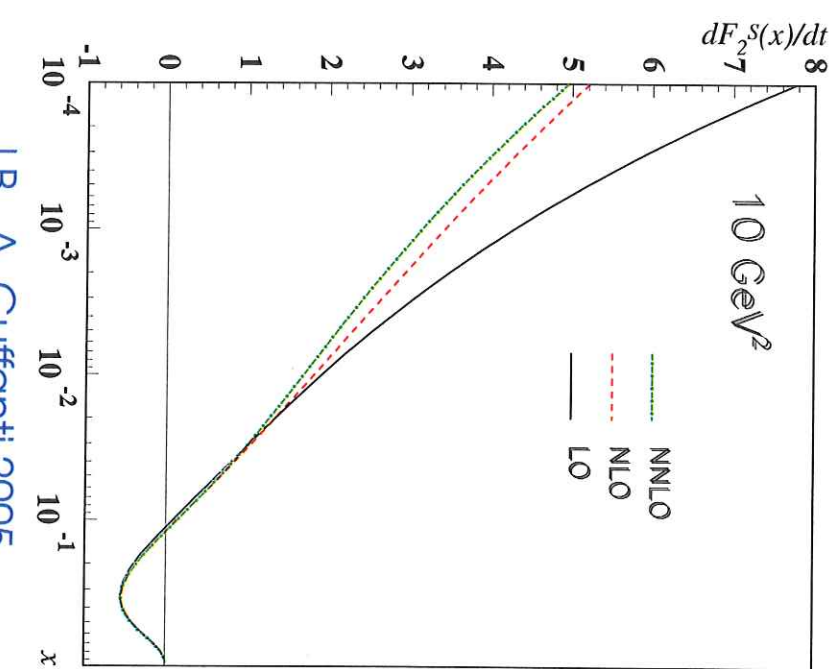
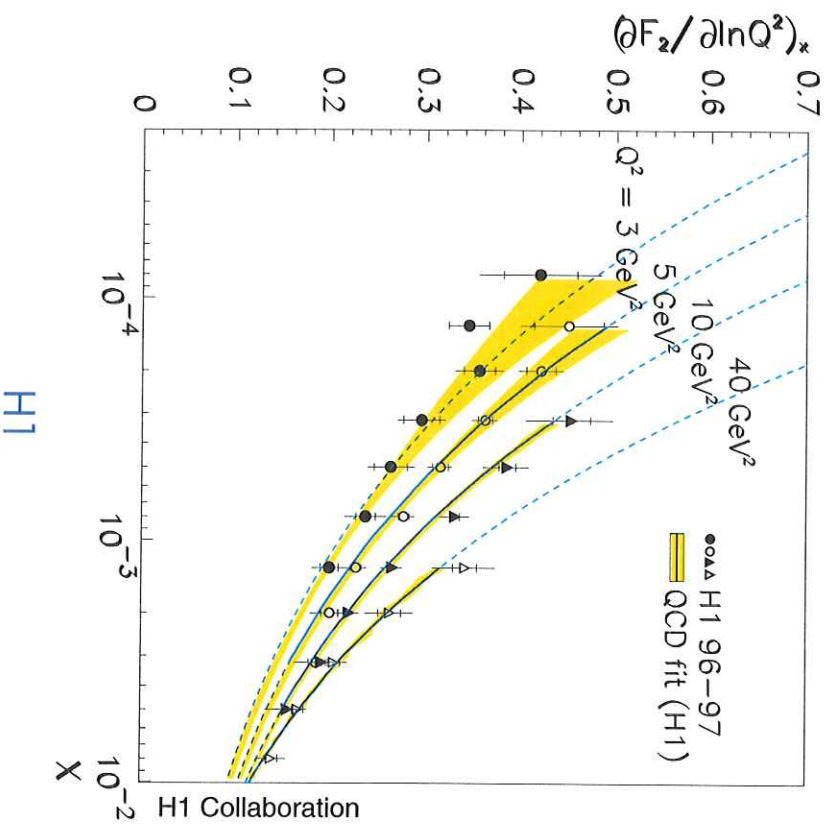




Parton Distributions: Overview



Slope of F_2 at low x

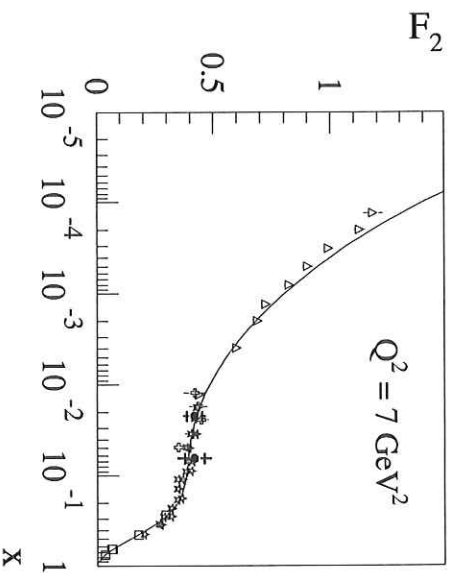
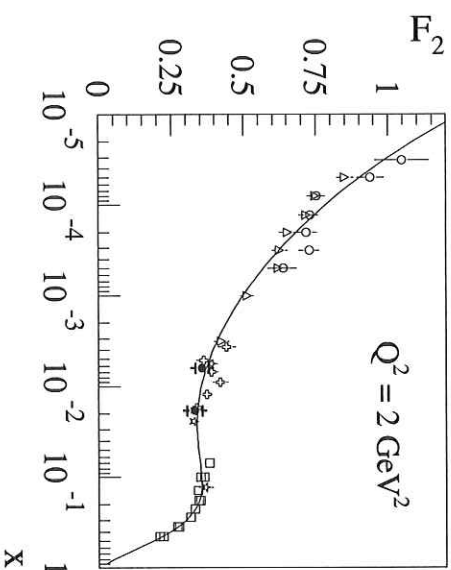
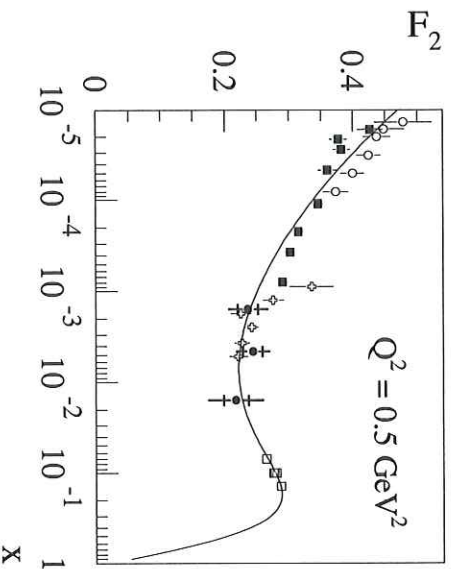


J.B., A. Guffanti 2005

Very likely, that the $\overline{\text{MS}}$ -gluon is remains positive!

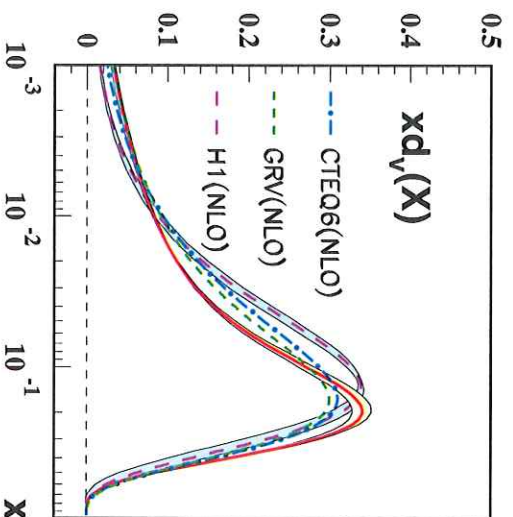
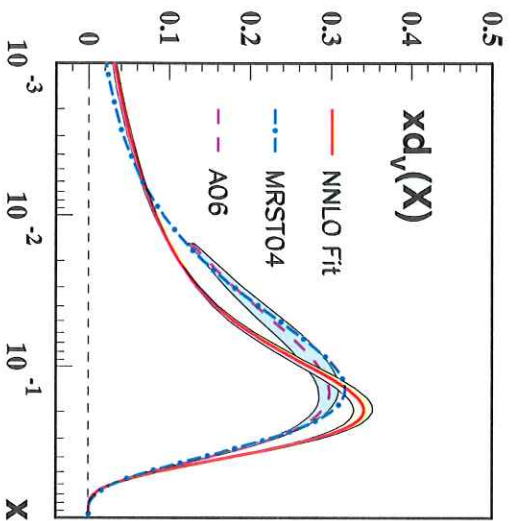
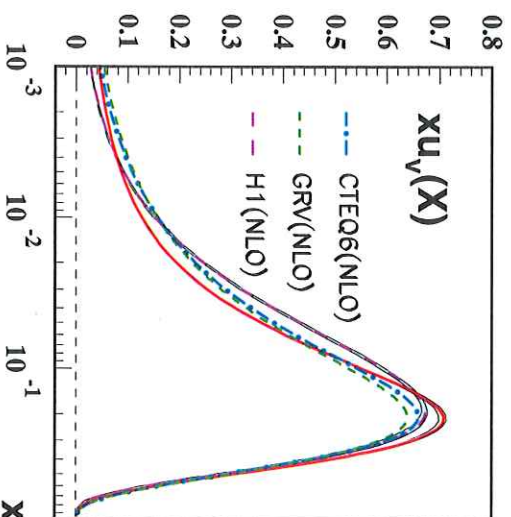
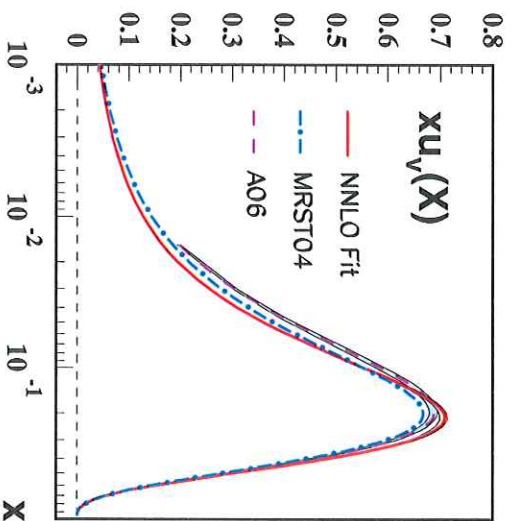
H1

Perturbative or non-perturbative growth?



- H1 QEDC 1997 ◊ E665
- △ H1 1997 * NMC
- H1 SV 1995 □ SLAC
- ZEUS BPT — ALLM97

Valence Distributions



World data:
NS-analysis

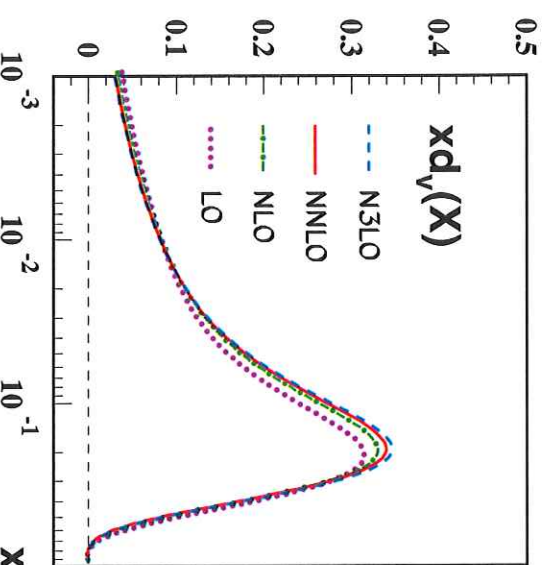
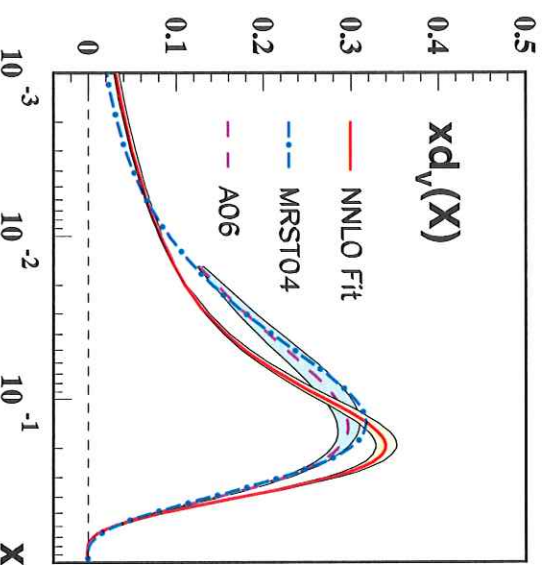
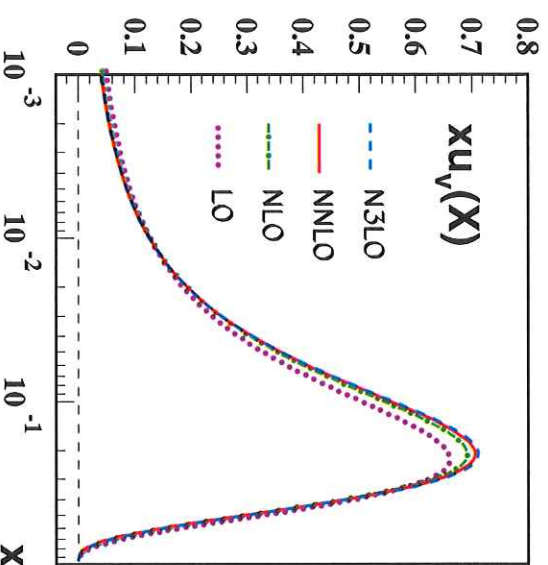
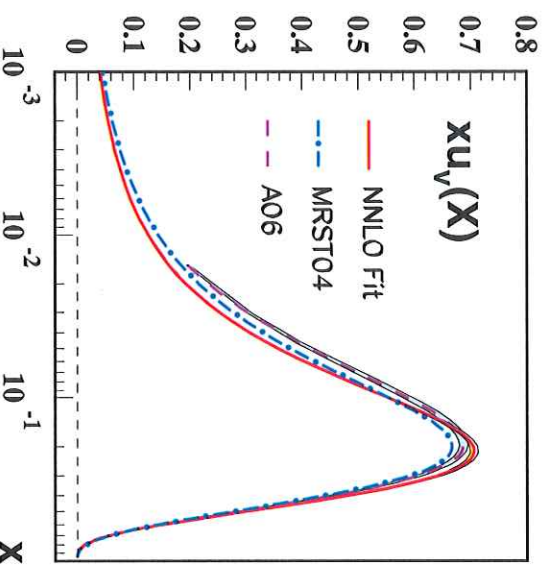
$W^2 > 12.5 \text{ GeV}^2, Q^2 > 4 \text{ GeV}^2$

$N^3\text{LO} :$

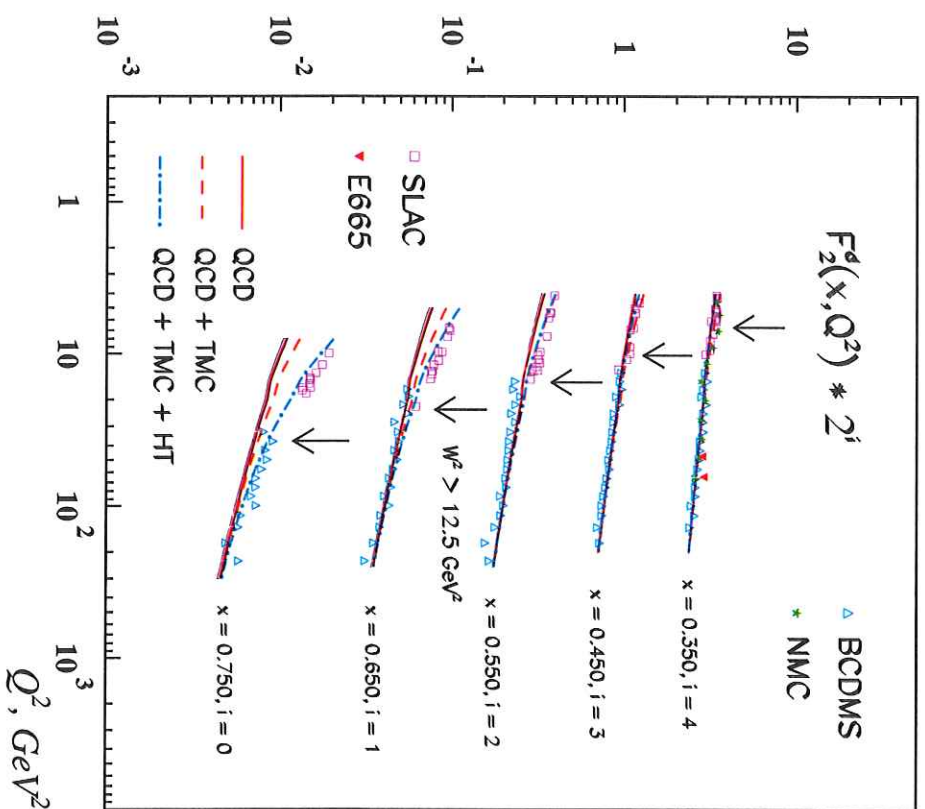
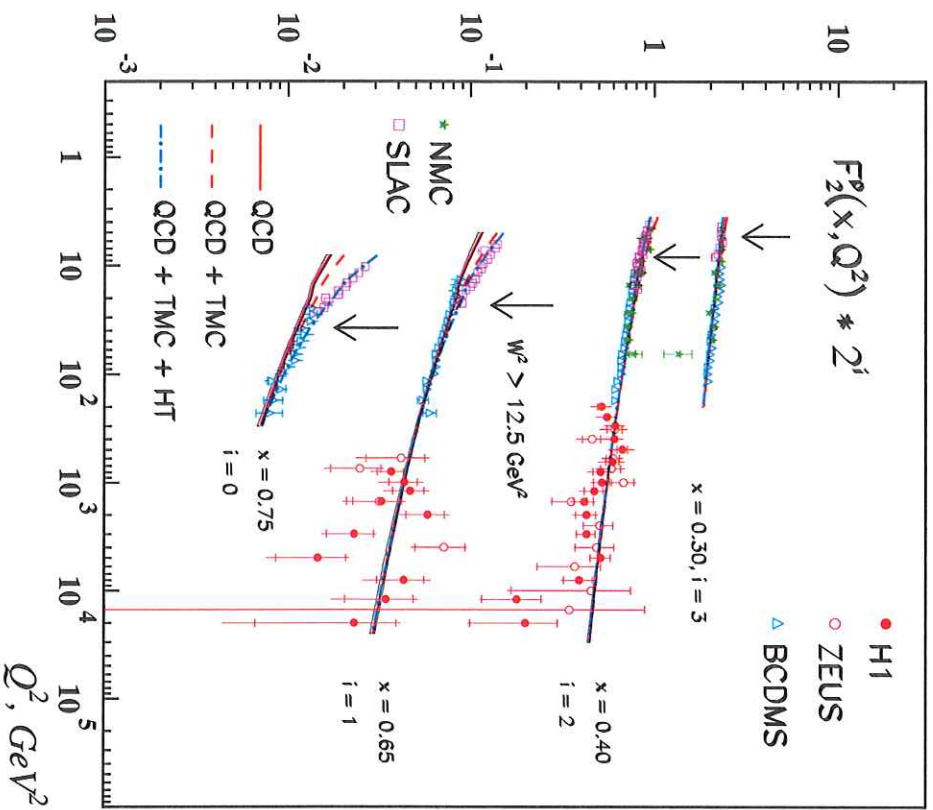
$$\alpha_s(M_Z^2) = 0.1141^{+0.0020}_{-0.0022}$$

J.B., H. Böttcher,
A. Guffanti,
(hep-ph/0607200)

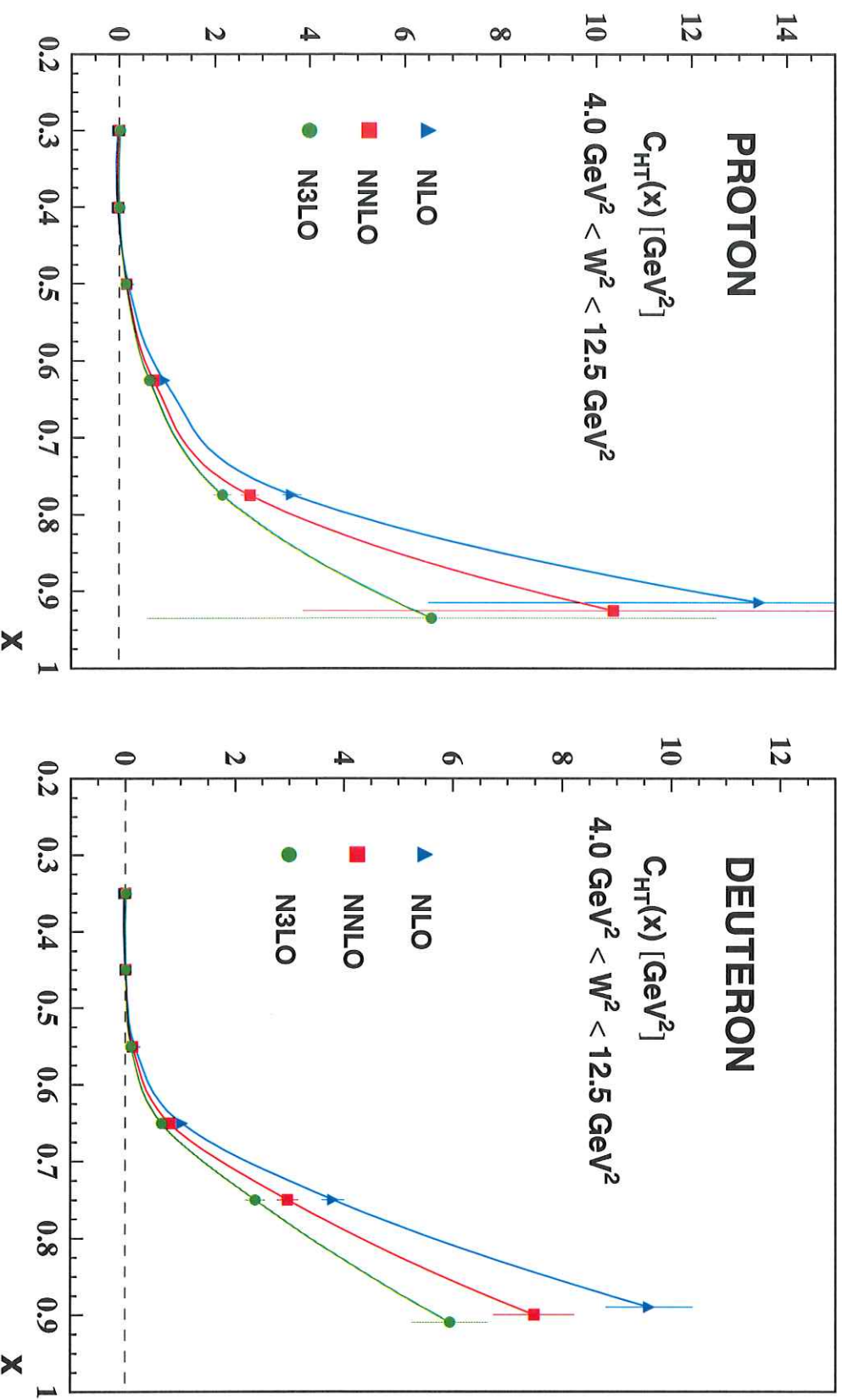
Valence Distributions



Valence Distributions

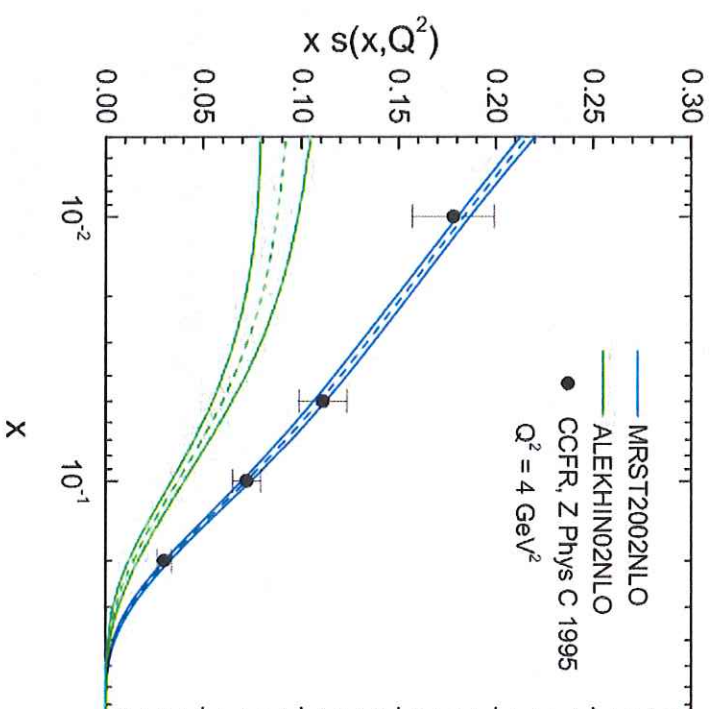
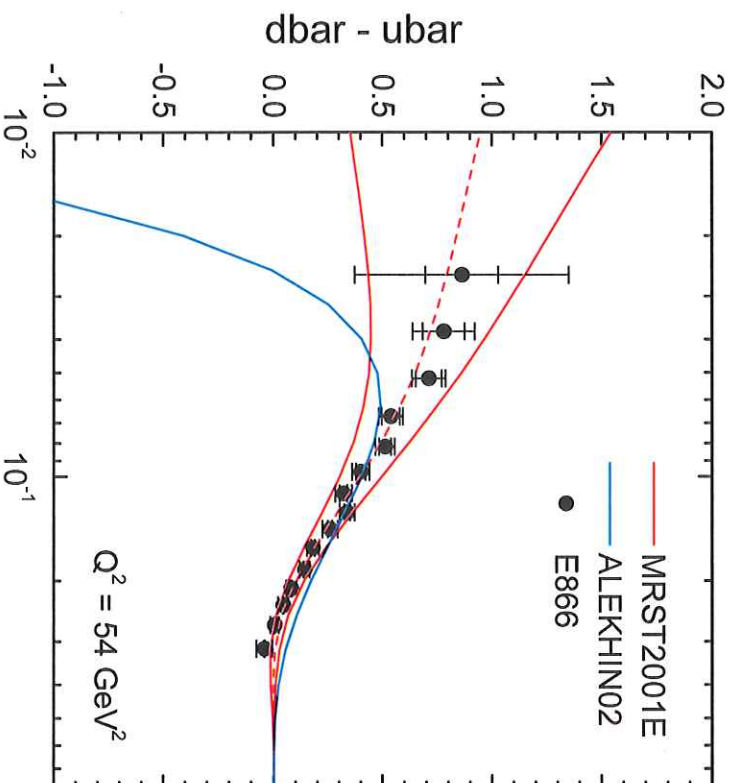


Valence Distributions: higher twist



- agreement between p and d analysis
- LGT determination of interest

Flavor distributions: light quarks

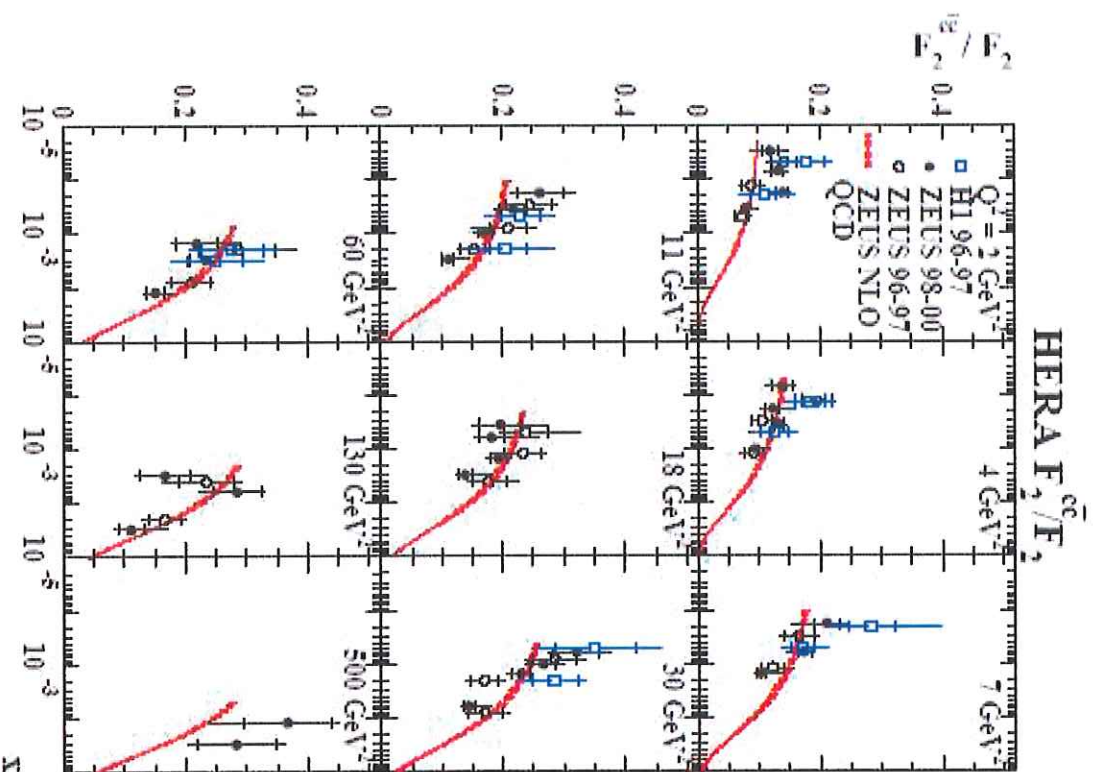


J. Stirling, 2004

More work needed.

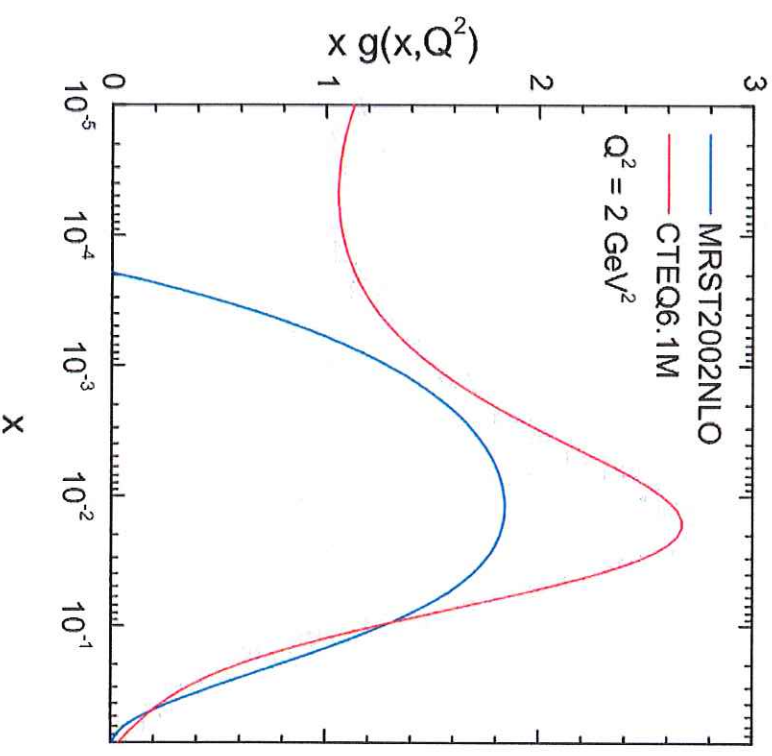
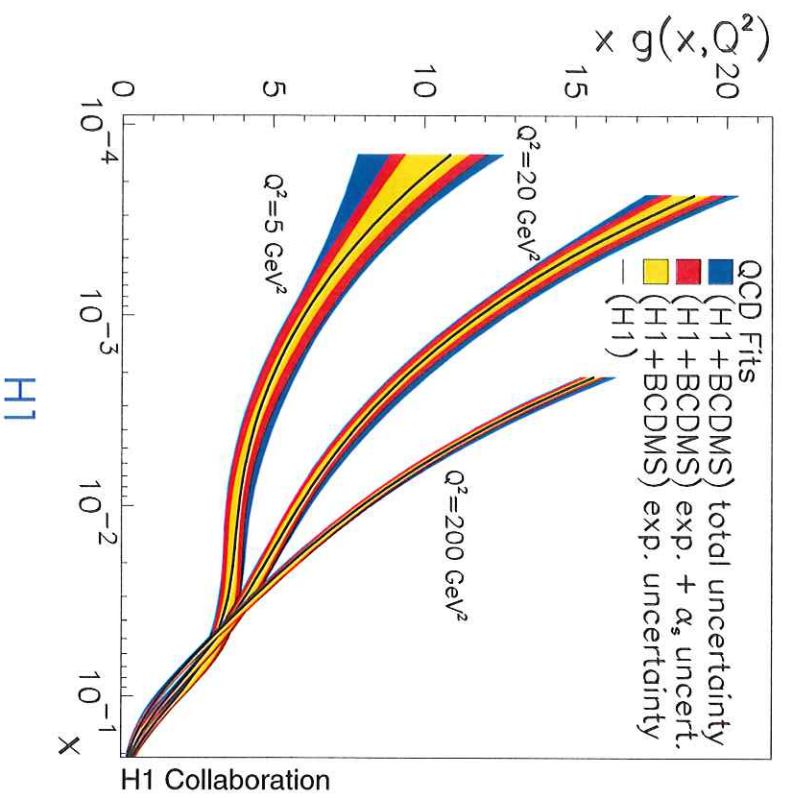
HERMES probably could measure $s(x, Q^2)$ in an independent way.

Charm



$F_2^{cc}(x, Q^2)$ will be very well measured at HERA.

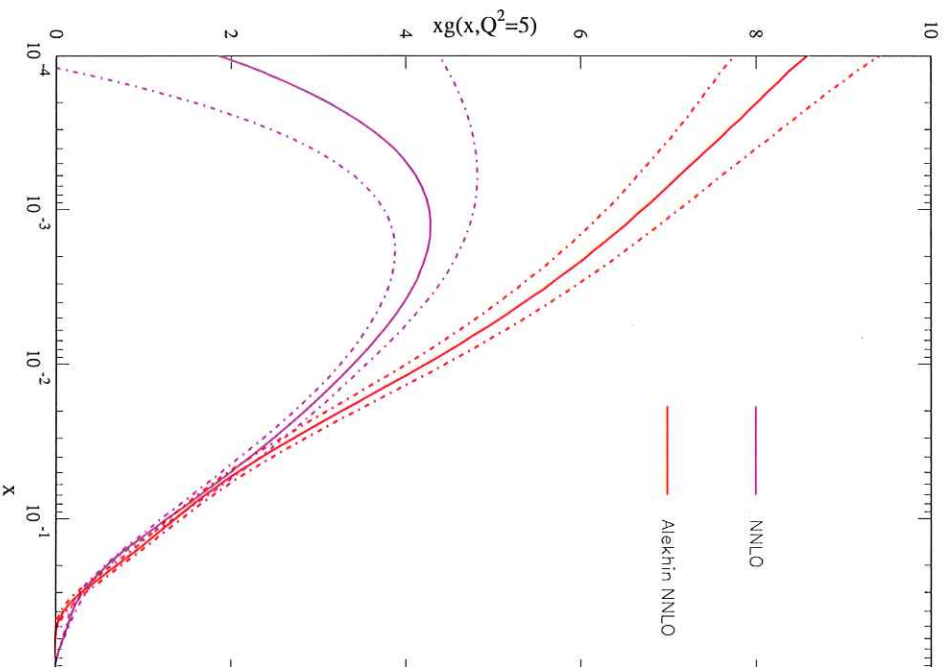
Gluon Density



More work needed; \overline{MS} - vs scheme-invariant evolution.

$F_L(x, Q^2)$ could be decisive.

Gluon Density



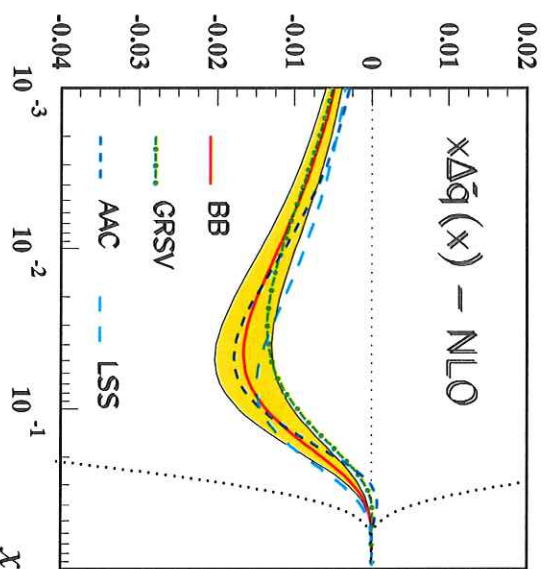
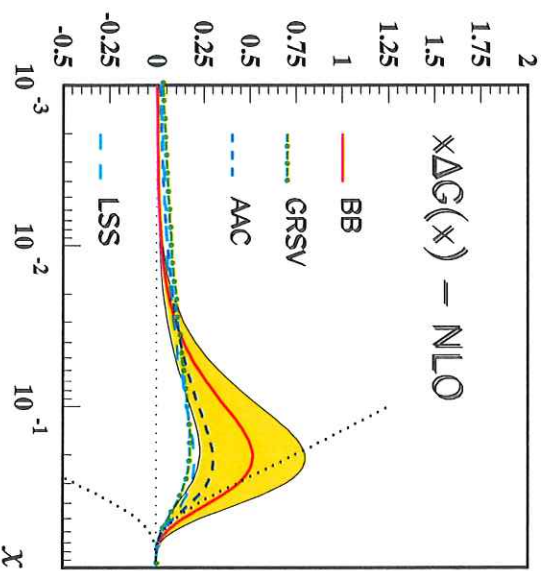
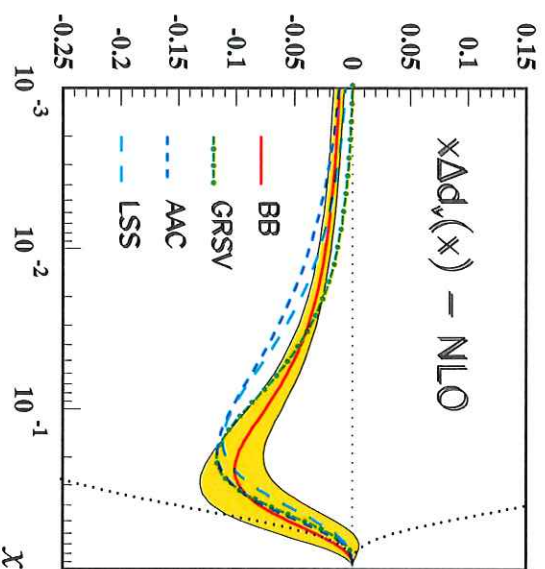
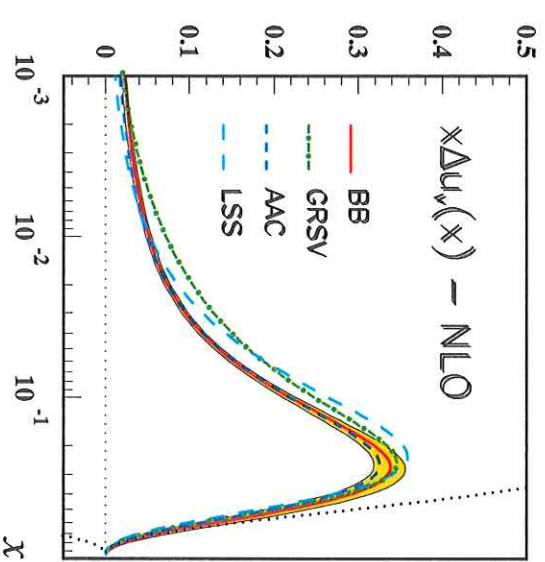
Not both distributions can be correct.

$F_L(x, Q^2)$ could be decisive.

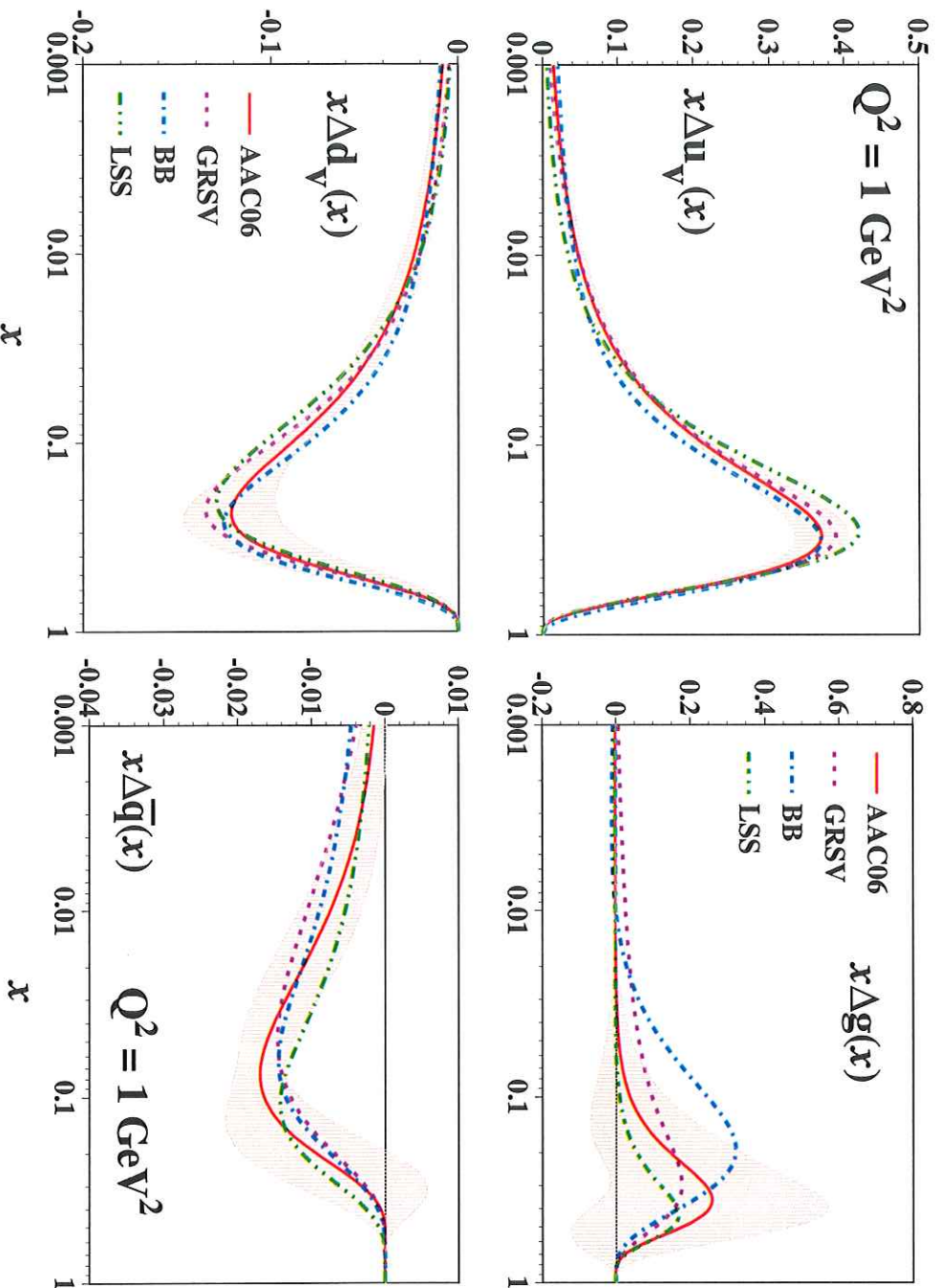
MRST06 vs Alekhin: 2006

More work needed ! BFG Analysis in progress.

2. Polarized Parton Densities



Polarized Parton Densities

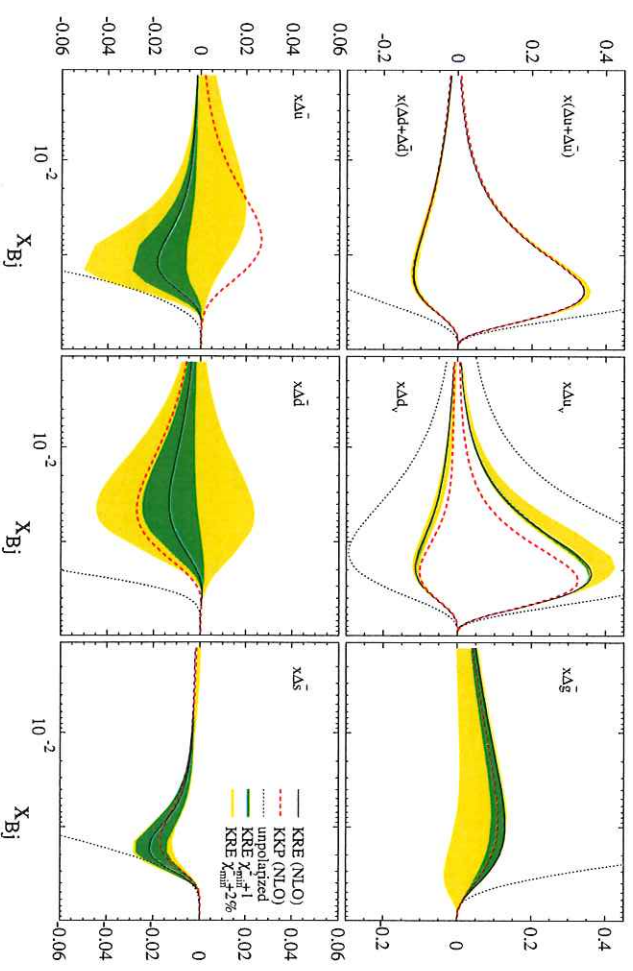
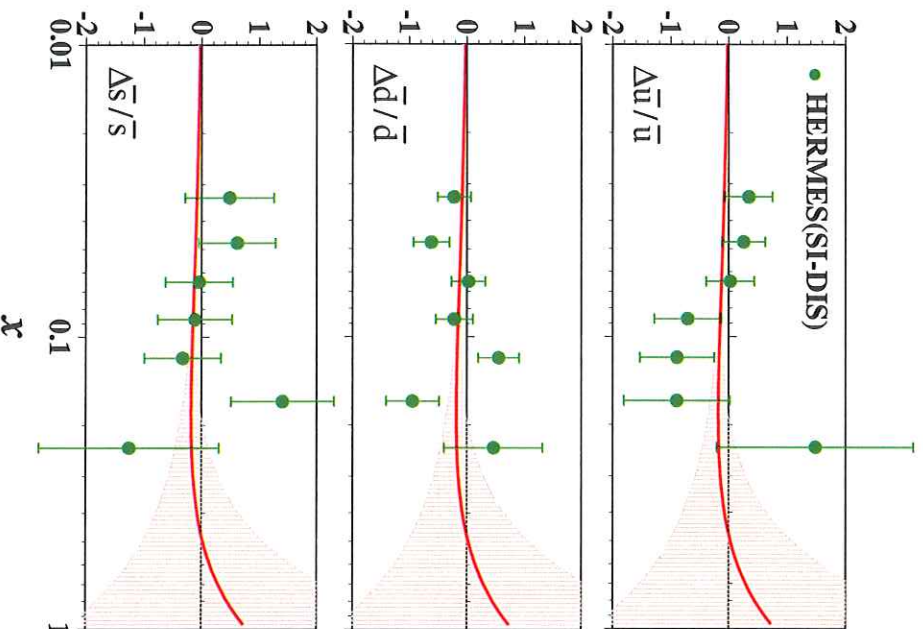


AAC 2006

this workshop: see also A. Khorrarnian & S. Therani;

Neural Networks: L. Del Debbio & A. Guffanti

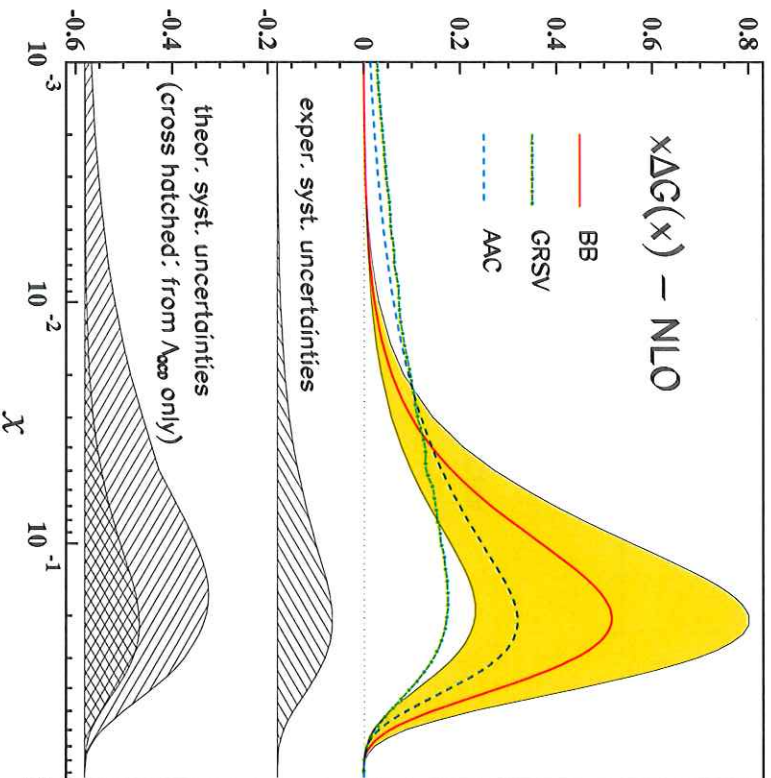
Polarized Parton Densities: Flavor Separation



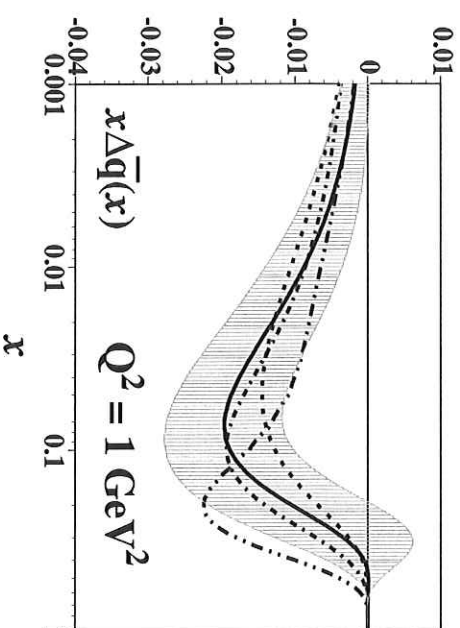
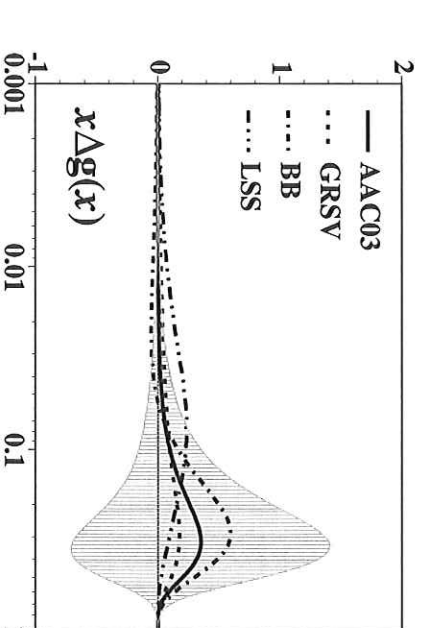
De Florian & Sassot, 2005
 $\delta\Delta_s$ too small ?

HERMES & AAC
 cf. also: Y. Imazu, T. Shibata, Y. Miyachi, this workshop.

Polarized Gluon Density



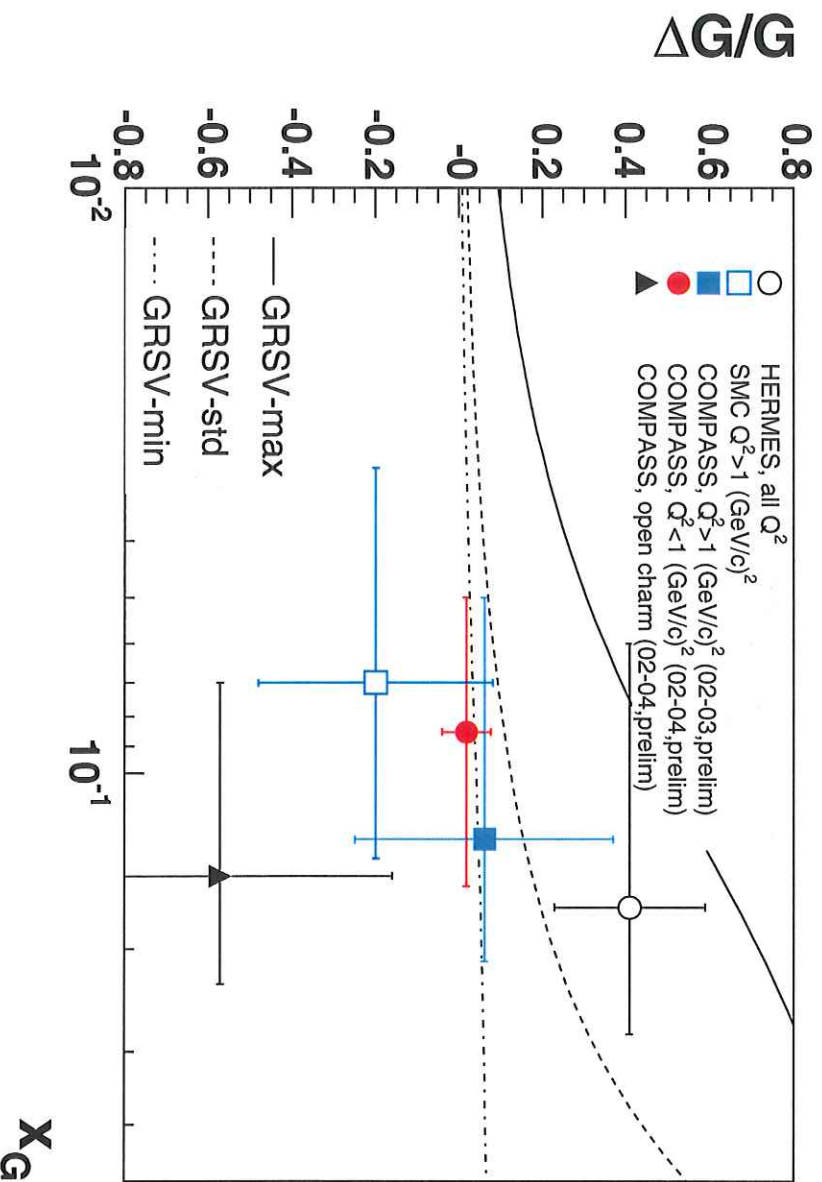
J.B., H. Böttcher, 2002



AAC

⇒ Currently slight move towards lower values.

Polarized Gluon Density



COMPASS 2006 compared to other measurements

⇒ Rather low Q^2 ; cf. G. Mallot and also P. Liebing (HERMES) this workshop.

Moments of PDF's: PT + data

f	n	This Fit	MRST04	A02	Δu_v	Moment	BB, NLO
		N ³ L0	NNLO	NNLO			
u_v	2	0.3006 ± 0.0031	0.285	0.304	Δu_v	0	0.926
	3	0.0877 ± 0.0012	0.082	0.087		1	0.163 ± 0.014
	4	0.0335 ± 0.0006	0.032	0.033	Δd_v	2	0.055 ± 0.006
						0	-0.341
d_v	2	0.1252 ± 0.0027	0.115	0.120	Δd_v	0	-0.047 ± 0.021
	3	0.0318 ± 0.0009	0.028	0.028		1	-0.015 ± 0.009
	4	0.0106 ± 0.0004	0.009	0.010	$\Delta u_v - \Delta d_v$	2	1.267
						0	0.210 ± 0.025
$u_v - d_v$	2	0.1754 ± 0.0041	0.171	0.184	$\Delta u_v - \Delta d_v$	0	0.070 ± 0.011
	3	0.0559 ± 0.0015	0.055	0.059		1	
	4	0.0229 ± 0.0007	0.022	0.024	$\Delta u_v - \Delta d_v$	2	
						0	

J.B., H. Böttcher, A. Guffanti, 2004

J.B., H. Böttcher, 2002

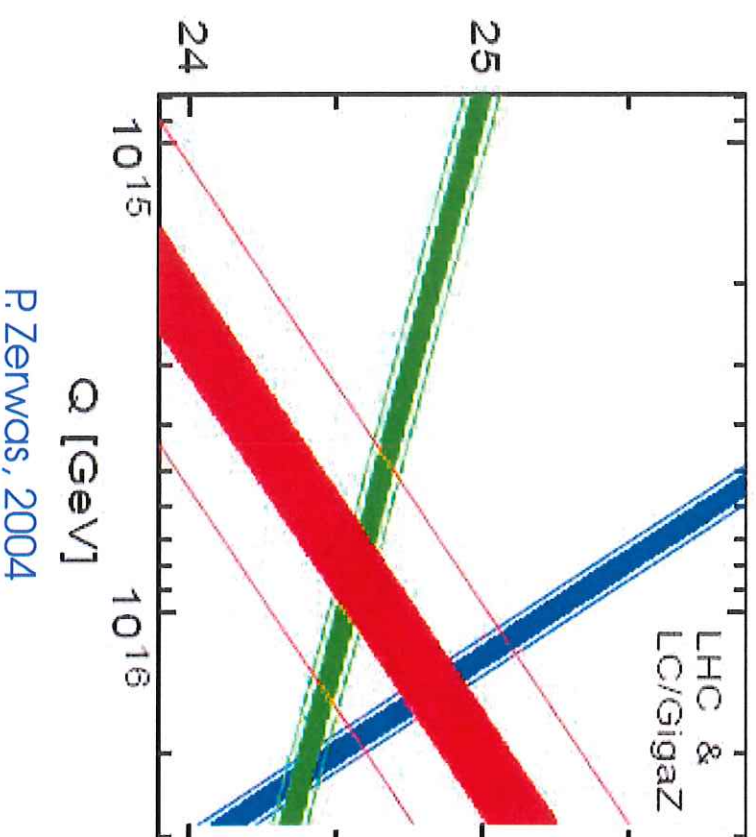
Lattice Results : different fermion-types studied.
Low values of m_π crucial; values approach 270 MeV now.

3. Λ_{QCD} and $\alpha_s(M_Z^2)$

$$\frac{\delta\alpha_{em}(0)}{\alpha_{em}(0)} \sim 3 \cdot 10^{-11}$$

$$\frac{\delta\alpha_{weak}}{\alpha_{weak}} \sim 7 \cdot 10^{-4}$$

$$\frac{\delta\alpha_s(M_Z^2)}{\alpha_s(M_Z^2)} > 2 \cdot 10^{-2}$$



P.Zerwas, 2004

$\alpha_s(M_Z^2)$

NLO	$\alpha_s(M_Z^2)$	expt	theory	Ref.
CTEQ6	0.1165	± 0.0065		[1]
MRST03	0.1165	± 0.0020	± 0.0030	[2]
A02	0.1171	± 0.0015	± 0.0033	[3]
ZEUS	0.1166	± 0.0049		[4]
H1	0.1150	± 0.0017	± 0.0050	[5]
BCDMS	0.110	± 0.006		[6]
GRS	0.112			[10]
BBG	0.1148	± 0.0019		[9]
BB (pol)	0.113	± 0.004	$+0.009$ -0.006	[7]

NLO

BBG: $N_f = 4$: non-singlet data-analysis at $O(\alpha_s^4)$: $\Lambda = 234 \pm 26 \text{ MeV}$
 I. Savin: pol. $O(\alpha_s^2)$ this workshop.

Lattice results :

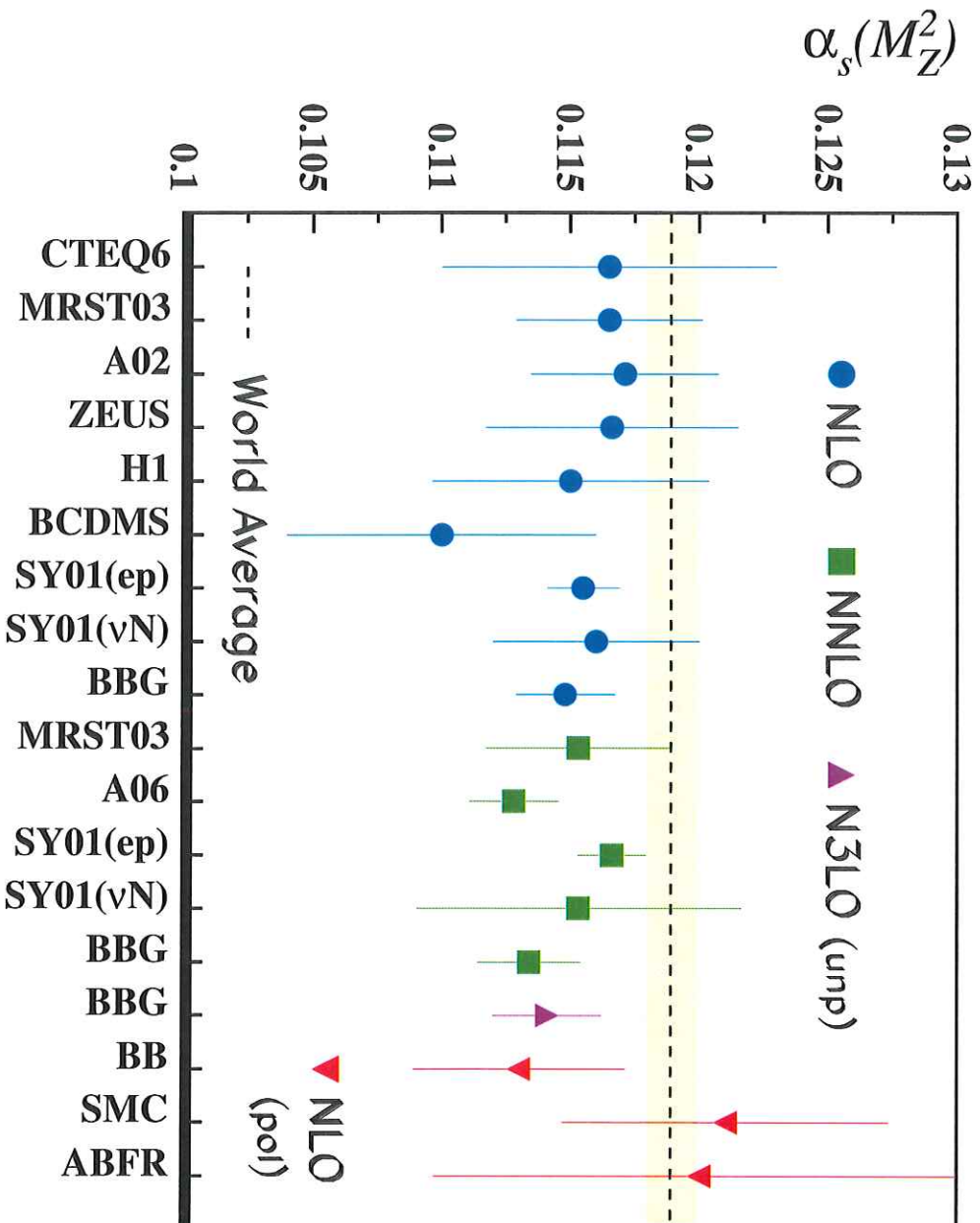
Alpha Collab: $N_f = 2$ Lattice; non-pert. renormalization $\Lambda = 245 \pm 16 \pm 16 \text{ MeV}$

QCDSF Collab: $N_f = 2$ Lattice, pert. reno. $\Lambda = 261 \pm 17 \pm 26 \text{ MeV}$

NNLO	$\alpha_s(M_Z^2)$	expt	theory	Ref.
MRST03	0.1153	± 0.0020	± 0.0030	[2]
A02	0.1143	± 0.0014	± 0.0009	[3]
SY01(ep)	0.1166	± 0.0013		[8]
SY01(νN)	0.1153	± 0.0063		[8]
GRS	0.111			[10]
A06	0.1128	± 0.0015		[11]
BBG	0.1134	$+0.0019 / -0.0021$		[9]
N³LO	$\alpha_s(M_Z^2)$	expt	theory	Ref.
BBG	0.1141	$+0.0020 / -0.0022$		[9]

NNLO and N³LO

$\alpha_s(M_Z^2)$



J.B., H. Böttcher, A. Guffanti, 2006

4. The Needs : What would we like to know ?

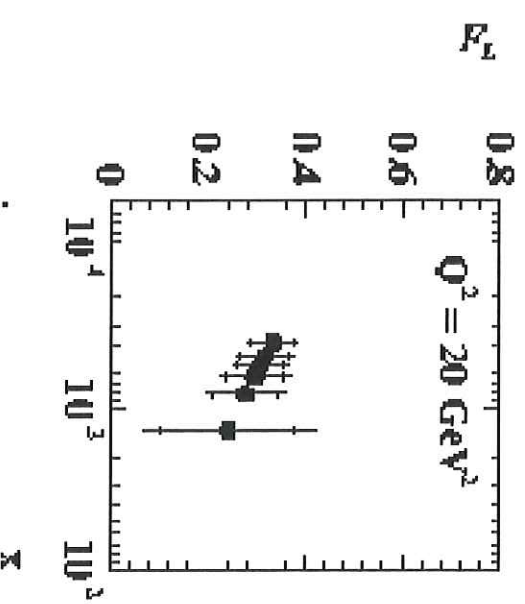
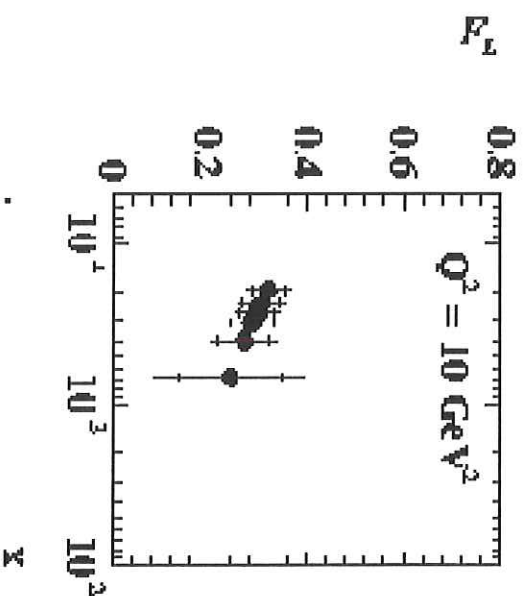
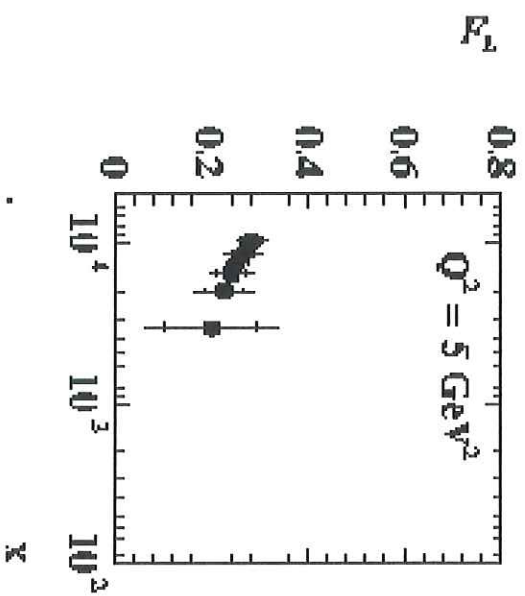
HERA:

- Collect high luminosity for $F_2(x, Q^2)$, $F_2^{c\bar{c}}(x, Q^2)$, $g_2^{c\bar{c}}(x, Q^2)$, and measure $h_1(x, Q^2)$.
- Measure : $F_L(x, Q^2)$. This is a key-question for HERA.

$$F_L(x, Q^2)$$

M. Klein, 2004: Projection for a possible measurement at HERA

⇒ of central importance to study the small x behaviour of the gluon distribution



4. Future Avenues : What would we like to know ?

HERA:

- Collect high luminosity for $F_2(x, Q^2)$, $F_2^{c\bar{c}}(x, Q^2)$, $g_2^{c\bar{c}}(x, Q^2)$, and measure $h_1(x, Q^2)$.
- Measure : $F_L(x, Q^2)$. This is a key-question for HERA.

RHIC & LHC:

- Improve constraints on gluon and sea-quarks: polarized and unpolarized. DIS PDF's \iff Collider PDF's

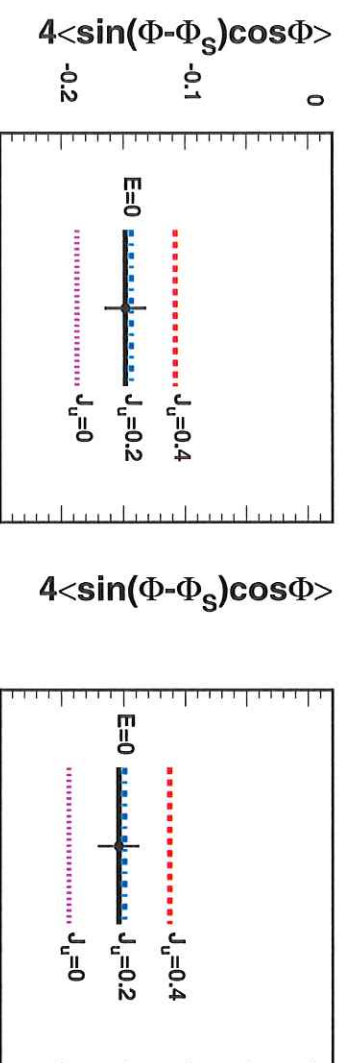
JLAB:

- High precision measurements in the large x domain at unpolarized and polarized targets; supplements HERA's high precision measurements at small x .

L_q from DVCS

- HERA and JLAB : Improve DVCS data

Theory widely developed, cf. rev. Belitsky & Radyushkin, 2005



Expected DVCS asymmetry $A_{UT}^{\sin(\phi-\phi_s)\cos\phi}$ with $b_u = 1, b_s = \infty, J_u = 0.4(0.2, 0.0)$, $J_d = 0.0$ in the Regge (left panel) and factorized (right panel) ansatz, at the average kinematics of the full measurement. $E = 0$ denotes zero effective contribution from the GPD E. The projected statistical error for 8M DIS events is shown. The systematic error is expected to not exceed the statistical one.

F. Elinghaus et al. 2005

The measurement of L_q off data is model-dependent at the moment.

Lattice calculations at low pion masses are needed to complete the picture

Graph Resummation and Saturation

Further study of proposed mechanisms needed: RHIC, LHC for nucleus-nucleus collisions.

ep scattering: partly different mechanisms

more studies would be welcome; link to higher twist contributions in gluon-dynamics

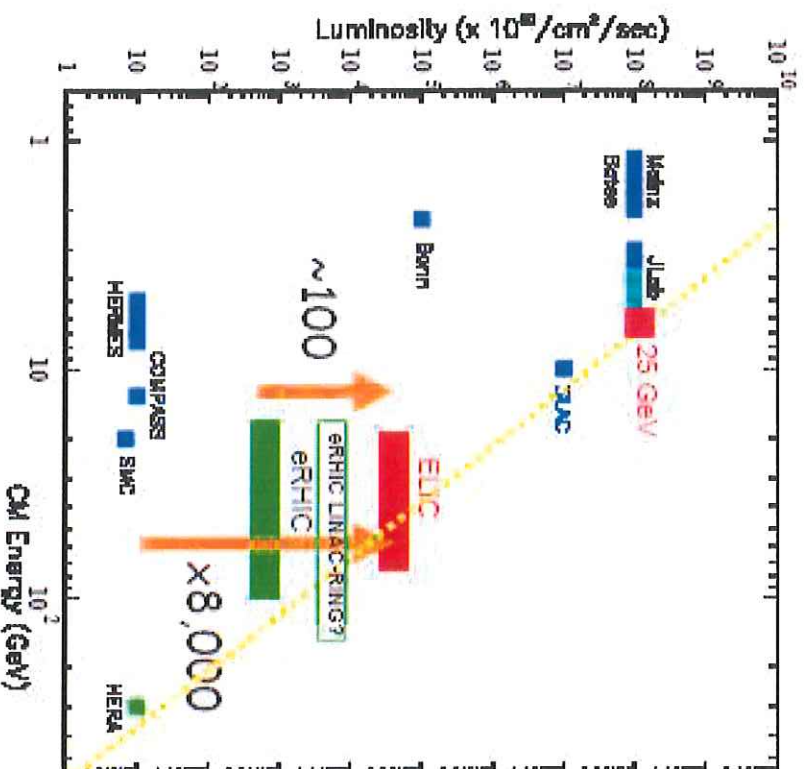
How do the non-perturbative and perturbative parts factorize ?

Conservation laws and interplay between the small x and medium x range behaviour

New DIS Machines

Where to go ?

- High energies : small x , large Q^2 desirable.
- High luminosities : ELIC: \sqrt{s} between CERN and HERA energies



R. Ent, 2004
 high precision physics
 polarized and unpolarized

Would be an important extension of the
 present programmes in many respects.

Enhancing Precision Further...

- What is the correct value of $\alpha_s(M_z^2)$? $\overline{\text{MS}}$ -analysis vs. scheme-invariant evolution helps. Compare non-singlet and singlet analysis; careful treatment of heavy flavor. (Theory & Experiment)
- Flavor Structure of Sea-Quarks: More studies needed. (All Experiments)
- Revisit polarized data upon arrival of the 3-loop anomalous dimensions; NLO heavy flavor contributions needed. (Theory)
- QCD at Twist 3: $g_2(x, Q^2)$, semi-exclusive Reactions, Transversity, diffraction in polarized scattering (HERMES, High Precision polarized experiments, JLAB, ELIC)
- Comparison with Lattice Results: α_s , Moments of Parton Distributions, Angular Momentum.

Enhancing Precision Further...

- Calculation of more hard scattering reactions at the 3-loop level: ILC, LHC
- Further perfection of the mathematical tools:
 - ⇒ Algorithmic simplification of Perturbation theory in higher orders.
- Even higher order corrections needed ?