

Measurement of the Angle $\phi_1(\beta)$ and $B\bar{B}$ Mixing (Recent results from BaBar and Belle)

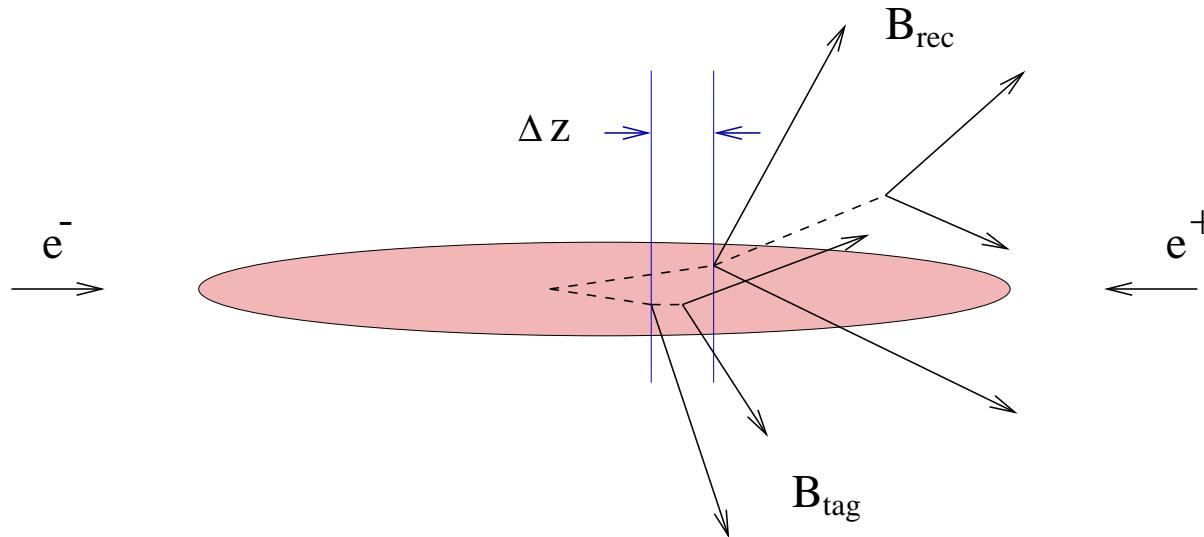
Kazuo Abe
KEK

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$$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$$

Charge-conjugation is conserved in $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$ decay. ($C = -1$)

Time structure stays $\psi(t) = |B^0\rangle |B^0\rangle - |\bar{B}^0\rangle |B^0\rangle$ at any t



BaBar: $9 \text{ GeV} \times 3.1 \text{ GeV} \rightarrow \Delta z \simeq 260 \mu\text{m}$

Belle: $8.5 \text{ GeV} \times 3 \text{ GeV} \rightarrow \Delta z \simeq 200 \mu\text{m}$

$$\Delta t = \Delta z / \gamma \beta c$$

Interaction region (KEKB):
 $2.3 \mu\text{m}(y) \times 100 \mu\text{m}(x) \times 7 \text{ mm}(z)$
much larger than Δz

Time-reference is given by the decay point of other B (Δt measurement).

Flavor of B_{rec} is opposite of B_{tag} at $\Delta z = 0$ (Flavor-tagging).

$B\bar{B}$ Mixing

- Mass and flavor eigenstates:

$$|B_1\rangle = p |B^0\rangle + q |\bar{B}^0\rangle$$

$$|B_2\rangle = p |B^0\rangle - q |\bar{B}^0\rangle$$

- Well-defined time dependence of (B_1, B_2)
 - Flavor-specific decays of (B^0, \bar{B}^0)
- } lead to $B^0\bar{B}^0$ oscillation

$$P^{\text{OF}} \propto \frac{e^{-|\Delta t/\tau_{B^0}|}}{4\tau_{B^0}} [1 + \cos(\Delta m_d \Delta t)], \quad P^{\text{SF}} \propto \frac{e^{-|\Delta t/\tau_{B^0}|}}{4\tau_{B^0}} [1 - \cos(\Delta m_d \Delta t)]$$

Lifetime distributions with $1 \pm \cos(\Delta m_d \Delta t)$ modulation.

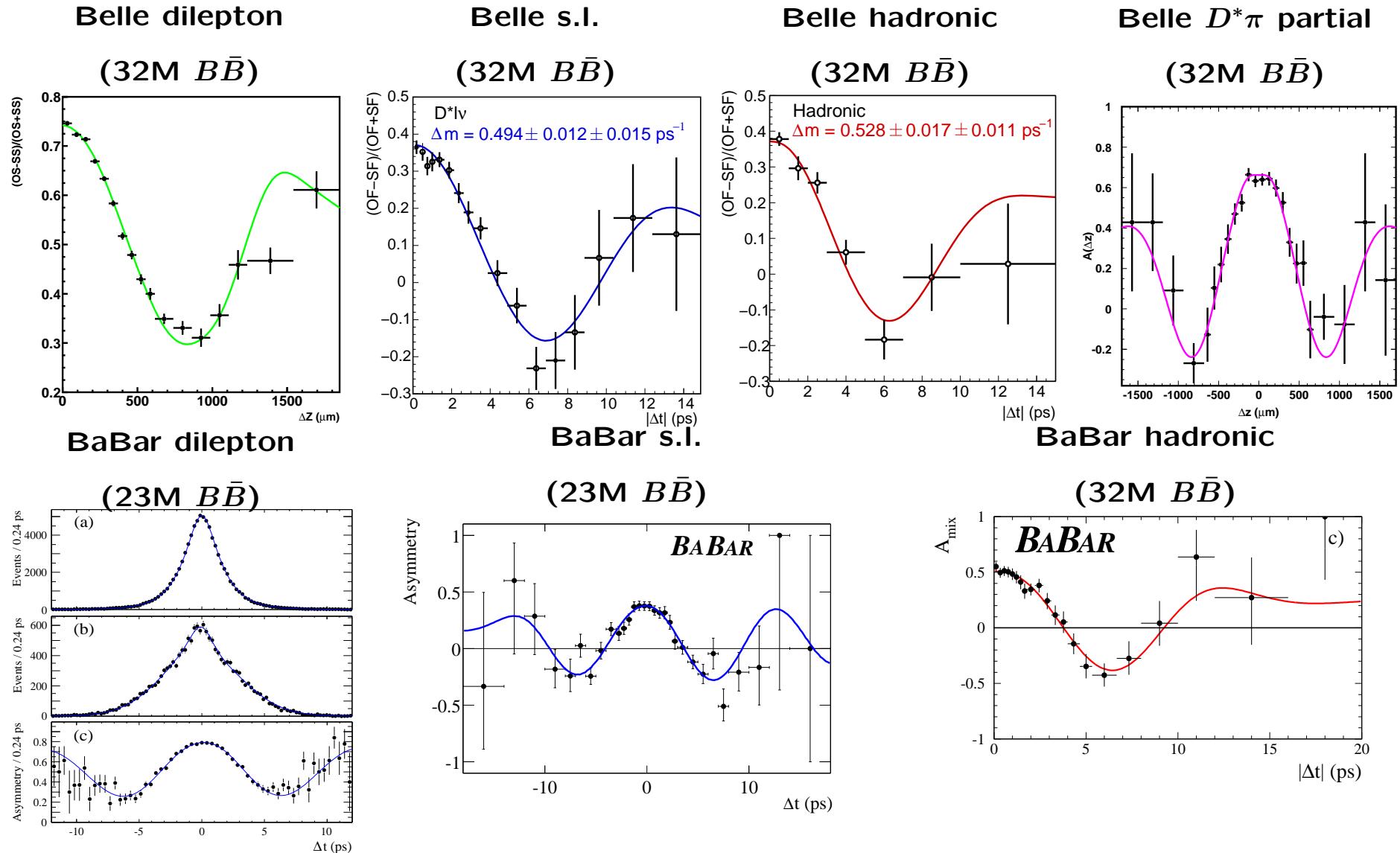
- $\underline{B}_{\text{rec}}$: $D^{(*)}\pi, D^{(*)}\rho, D^{(*)}l\nu, \dots$ (flavor-specific states)

dilepton: $B_{\text{rec}} = B_{\text{tag}} = \text{lepton only}$ (special case)

- B_{rec} for CP analysis: $J/\psi K_S, J/\psi K_L, \dots$ (CP-eigenstates)

Lifetime distributions with $1 \pm \sin 2\phi_1 \sin(\Delta m_d \Delta t)$ modulation.

(OF-SF)/(OF+SF) Asymmetries



Δm_d Results

- BaBar+Belle:

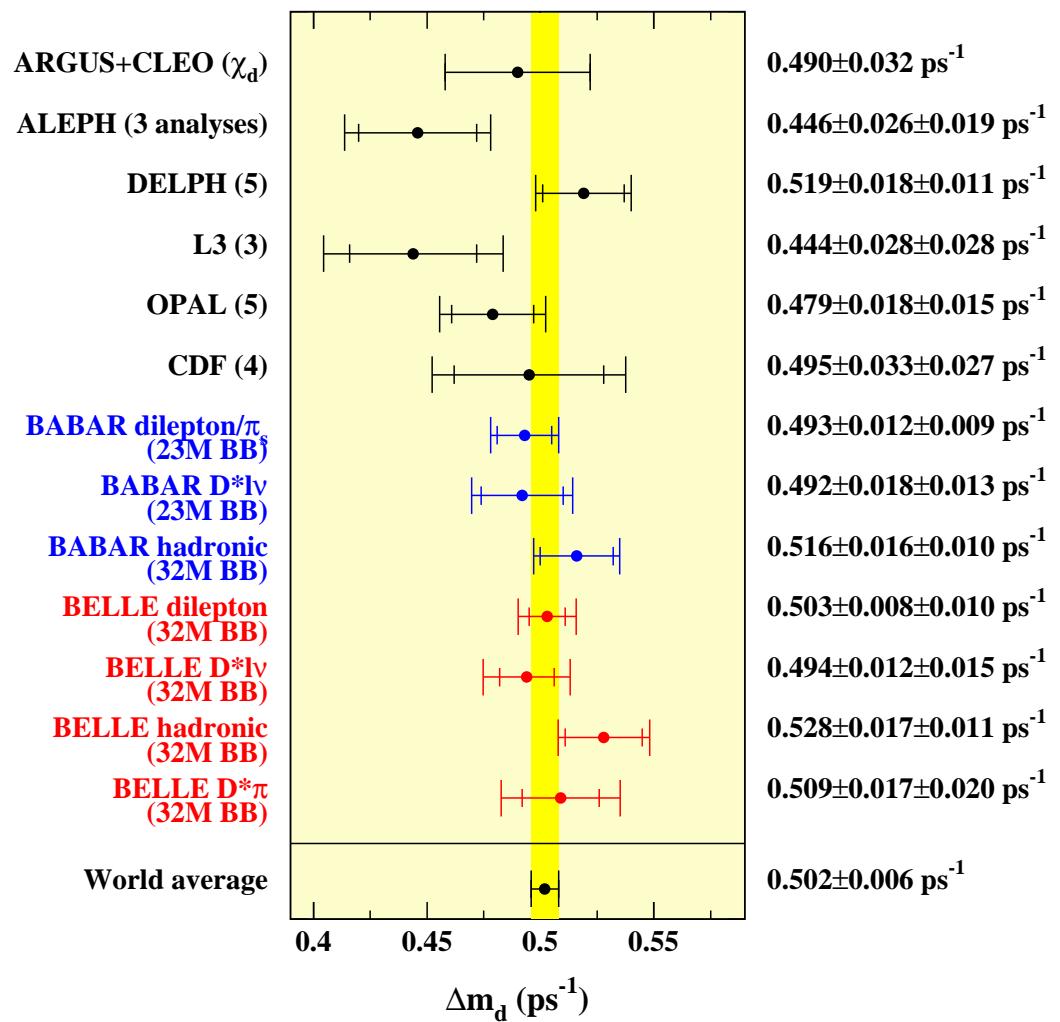
$$\Delta m_d = 0.504 \pm 0.007 \text{ ps}^{-1}$$

- World average:

$$\Delta m_d = 0.502 \pm 0.006 \text{ ps}^{-1}$$

- 1.2% accuracy

What is this good for?



$B\bar{B}$ Mixing in Standard Model

- Box-diagram is responsible for $B\bar{B}$ mixing.

$$\Delta m_d = m_H - m_L = 2|M_{12}|$$

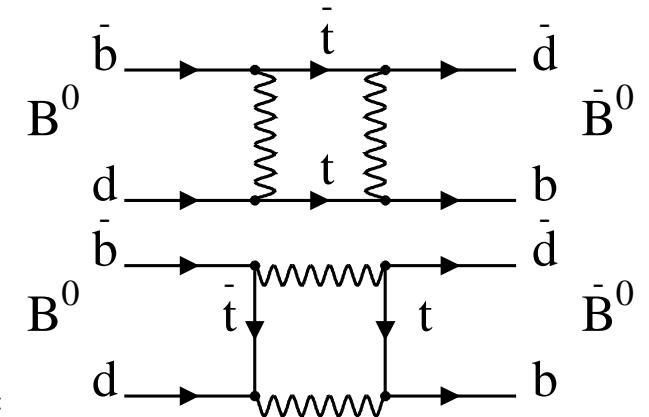
(redefine B_1, B_2 with B_H, B_L)

$$M_{12} = -\frac{G_F^2 m_W^2 \eta_B m_B B_B f_B^2}{12\pi^2} S_0 (m_t^2/m_W^2) (V_{td}^* V_{tb})^2$$

- $|V_{td}|$ extraction is dominated by $f_{B_d} \sqrt{B_{B_d}} = 230 \pm 40 \text{ MeV}$. Precise Δm_d does not help.
(Lattice QCD approach, Δm_s measurement)

- Mixing also has absorptive part: $\Delta\Gamma = \Gamma_L - \Gamma_H = 2|\Gamma_{12}|$
- $\Delta\Gamma$ is tiny: $\left| \frac{\Gamma_{12}}{M_{12}} \right| \sim \frac{\Delta\Gamma}{\Gamma} \simeq \frac{3\pi}{2} \frac{m_b^2}{m_W^2} \frac{1}{S_0(m_t^2/m_W^2)} \sim 5 \times 10^{-3} (\pm 30\%)$

Any deviation will be difficult to explain in SM. **Interesting**



$\Delta\Gamma$ Measurement

- Time-dependent decay rates must include non-zero $\Delta\Gamma$.
- Flavor-specific state ($B \rightarrow f(\bar{f})$):

$$[1 \pm \cos(\Delta m_d \Delta t)] \rightarrow [\cosh \frac{\Delta\Gamma_d \Delta t}{2} \pm \cos(\Delta m \Delta t)]$$

- CP eigenstate ($B^0 \rightarrow f_{CP}$, CP -even (CP -odd)):

$$[1 \pm \sin 2\phi_1 \sin(\Delta m_d \Delta t)]$$

$$\rightarrow [\cosh \frac{\Delta\Gamma_d \Delta t}{2} \mp \cos 2\phi_1 \sinh \frac{\Delta\Gamma_d \Delta t}{2} \pm \sin 2\phi_1 \sin(\Delta m \Delta t)]$$

CP Violation in $B\bar{B}$ Mixing

CP violation leads to $\rightarrow |q/p| \neq 1$

- $1 - |\frac{q}{p}|^2 \simeq Im\left(\frac{\Gamma_{12}}{M_{12}}\right) < 10^{-3}$

$$(|\Gamma_{12}/M_{12}| \sim 5 \times 10^{-3}, \quad \phi_{M_{12}} - \phi_{\Gamma_{12}} = \pi + O(m_c^2/m_b^2))$$

- $P_{++}^{\text{SF}} = |\frac{p}{q}|^2 \cdot P^{\text{SF}}$ $P_{--}^{\text{SF}} = |\frac{q}{p}|^2 \cdot P^{\text{SF}}$

P_{++}^{SF} and P_{--}^{SF} can be different \rightarrow charge asymmetry in SF events

- Possible new physics through $\phi_{M_{12}} - \phi_{\Gamma_{12}}$ at $O(10^{-3})$ level. Interesting

CPT Violation in $B\bar{B}$ Mixing

CPT violation leads to $p \neq p'$ and/or $q \neq q'$

- $|B_H\rangle = p |B^0\rangle + q |\overline{B^0}\rangle$, $|B_L\rangle = p' |B^0\rangle - q' |\overline{B^0}\rangle$

$$\frac{q}{p} = \tan(\frac{\theta}{2})e^{i\phi}, \quad \frac{q'}{p'} = \cot(\frac{\theta}{2})e^{i\phi} \quad (\theta \text{ can deviate from } 90^\circ)$$

- Time dependence of OF decay is modified:

$$1 + \cos(\Delta m_d \Delta t) \rightarrow$$

$$[1 + |\cos \theta|^2 + (1 - |\cos \theta|^2) \cos(\Delta m_d \Delta t) - 2 \operatorname{Im}(\cos \theta) \sin(\Delta m_d \Delta t)]$$

- P_{+-}^{OF} and P_{-+}^{OF} can be different → time-dependent asymmetry in OF events
- Quantum Mechanics test, exotics. Something to continue looking for

$\Delta\Gamma/\Gamma, |q/p|, \cos\theta(z)$ Results

BaBar: Fully reconstructed hadronic events (88M $B\bar{B}$)

$$\begin{aligned} \text{sgn}(\text{Re}\lambda_{CP})\Delta\Gamma/\Gamma &= -0.008 \pm 0.037 \pm 0.018 \quad (\text{sgn}(\text{Re}\lambda_{CP}) = +1 \text{ in SM}) \\ |q/p| &= 1.029 \pm 0.013 \pm 0.011 \\ \text{Re}\lambda_{CP}/|\lambda_{CP}| \text{Re}z &= 0.014 \pm 0.035 \pm 0.034 \quad (\text{Re}\lambda_{CP}/|\lambda_{CP}| \simeq 0.672 \pm 0.068) \\ \text{Im}z &= 0.038 \pm 0.029 \pm 0.025 \end{aligned}$$

BaBar: dilepton events (23M $B\bar{B}$)

$$|q/p| = 0.998 \pm 0.005 \pm 0.007$$

Belle: dilepton events (32M $B\bar{B}$)

$$\begin{aligned} \text{Im}(\cos\theta) &= 0.03 \pm 0.01 \pm 0.03 \\ \text{Re}(\cos\theta) &= 0.00 \pm 0.12 \pm 0.01 \end{aligned}$$

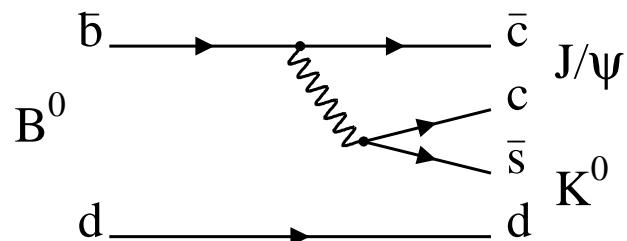
- $\delta(\Delta\Gamma/\Gamma) \sim 0.05$ (10^{-2} in SM),
 $\delta(|q/p|) \sim 0.01$ ($\sim 10^{-3}$ in SM),
 $\delta(\text{Im}(\cos\theta)) \sim 0.03$, $\delta(\text{Re}(\cos\theta)) \sim 0.07$.

sin 2 ϕ_1 from $J/\psi K_S$ and other $b \rightarrow c\bar{c}s$ decays

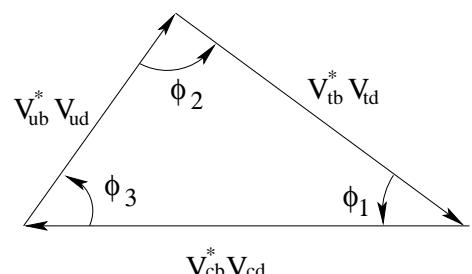
Asymmetry between $(B^0 \rightarrow f)$ and $(\bar{B}^0 \rightarrow \bar{f})$ for final state $f = \bar{f} = f_{CP}$:

$$a_f(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f) - \Gamma(B^0(t) \rightarrow f)}{\Gamma(\bar{B}^0(t) \rightarrow f) + \Gamma(B^0(t) \rightarrow f)} = \frac{2Im\lambda_f}{|\lambda_f|^2 + 1} \sin(\Delta mt) + \frac{|\lambda_f|^2 - 1}{|\lambda_f|^2 + 1} \cos(\Delta mt)$$

$Im\lambda_f \neq 0 \rightarrow$ Mixing-assisted CP violation, $|\lambda_f| \neq 1 \rightarrow$ Direct CP violation



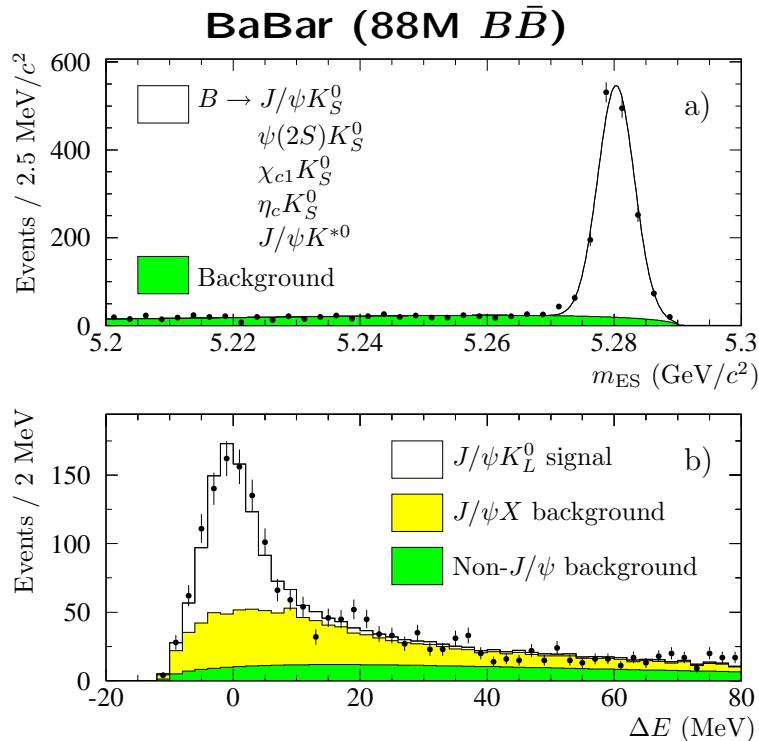
$$\begin{aligned}\lambda_f &= \frac{q \langle f | H | \bar{B}^0 \rangle}{p \langle f | H | B^0 \rangle} \\ \frac{q}{p} &= \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \rightarrow e^{-2i\phi_1} \text{ (Standard Model)}\end{aligned}$$



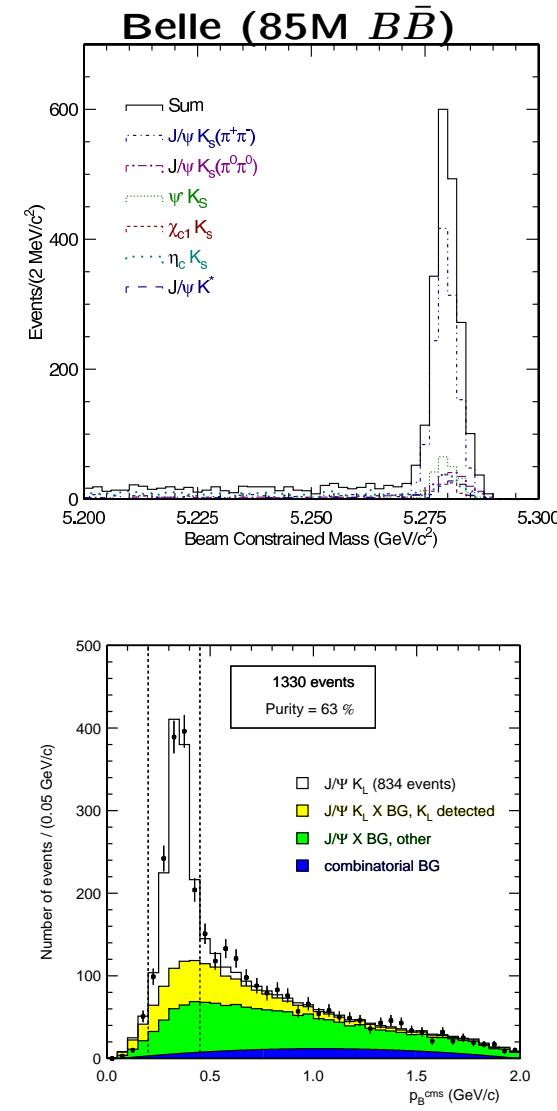
$$\begin{aligned}\lambda(J/\psi K_S) &= \frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \cdot \eta_{J/\psi K_S} \cdot \left(\frac{V_{cb} V_{cs}^*}{V_{cb}^* V_{cs}} \right) \cdot \left(\frac{V_{cd}^* V_{cs}}{V_{cs}^* V_{cd}} \right) \\ &\rightarrow Im\lambda(J/\psi K_S) = \sin 2\phi_1 \quad (-\sin 2\phi_1 \text{ for } J/\psi K_L)\end{aligned}$$

(sign of $\sin 2\phi_1$ depends on CP of final state η_f)

Selection of $J/\psi K_S$ and other $b \rightarrow c\bar{c}s$ Events



- Signal peaks at M_B in beam-energy constrained B mass distributions.
- No K_L energy measurement.
Calculated $\Delta E = E_{J/\psi K_L} - E_{\text{beam}}$ (peaks at 0 MeV) or p_B^* (peaks at 340 MeV/c).



Extraction of $\sin 2\phi_1$

- Tag the flavor of each candidate event. Categorize according to the quality of tagging.
- Determine mistag fraction from the data (assuming Δm_d is known).

$$(N_{OF} - N_{SF})/(N_{OF} + N_{SF}) = (1 - 2w) \cos(\Delta m_d \Delta t)$$

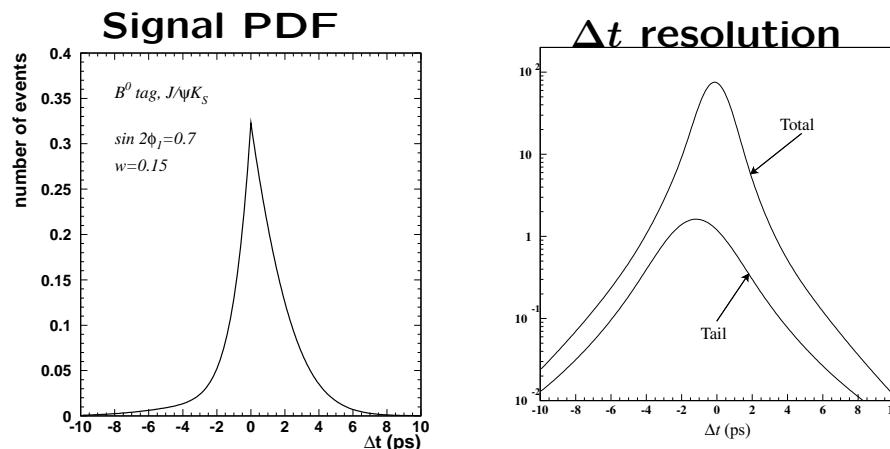
BaBar				
category	$\epsilon(\%)$	$w(\%)$	$\Delta w(\%)$	$\epsilon_{\text{eff}}(\%)$
lepton	$9.1 \pm .2$	$3.3 \pm .6$	-1.5 ± 1.1	$7.9 \pm .3$
kaon I	$16.7 \pm .2$	$10.0 \pm .7$	-1.3 ± 1.1	$10.7 \pm .4$
kaon II	$19.8 \pm .3$	$20.9 \pm .8$	-4.4 ± 1.2	$6.7 \pm .4$
inclusive	$20.0 \pm .3$	$31.5 \pm .9$	-2.4 ± 1.3	$2.7 \pm .3$
all	$65.6 \pm .5$			$28.1 \pm .7$

$$(\Delta w = w(B^0) - w(\bar{B}^0), \epsilon_{\text{eff}} = \epsilon(1 - 2w)^2)$$

Belle			
cat.	$\epsilon(\%)$	$w(\%)$	$\epsilon_{\text{eff}}(\%)$
1	39.8	$45.8 \pm .6$	$0.3 \pm .1$
2	14.6	$33.6 \pm .9$	$1.6 \pm .2$
3	10.4	$22.8 \pm 1.$	$3.1 \pm .2$
4	12.2	$16.0 \pm .9$	$5.6 \pm .3$
5	9.4	$11.2 \pm .9$	$5.6 \pm .3$
6	13.6	$2.0 \pm .6$	$12.6 \pm .4$
all	100.0		$28.8 \pm .6$

- Fit Δt distribution. Maximize $L = \prod_i P_i$ ($i \dots$ each candidate event)

$$P_i = \int [f_{\text{sig}} P_{\text{sig}}(\Delta t') R_{\text{sig}}(\Delta t - \Delta t') + (1 - f_{\text{sig}}) P_{\text{bkg}}(\Delta t') R_{\text{bkg}}(\Delta t - \Delta t')] d\Delta t'$$

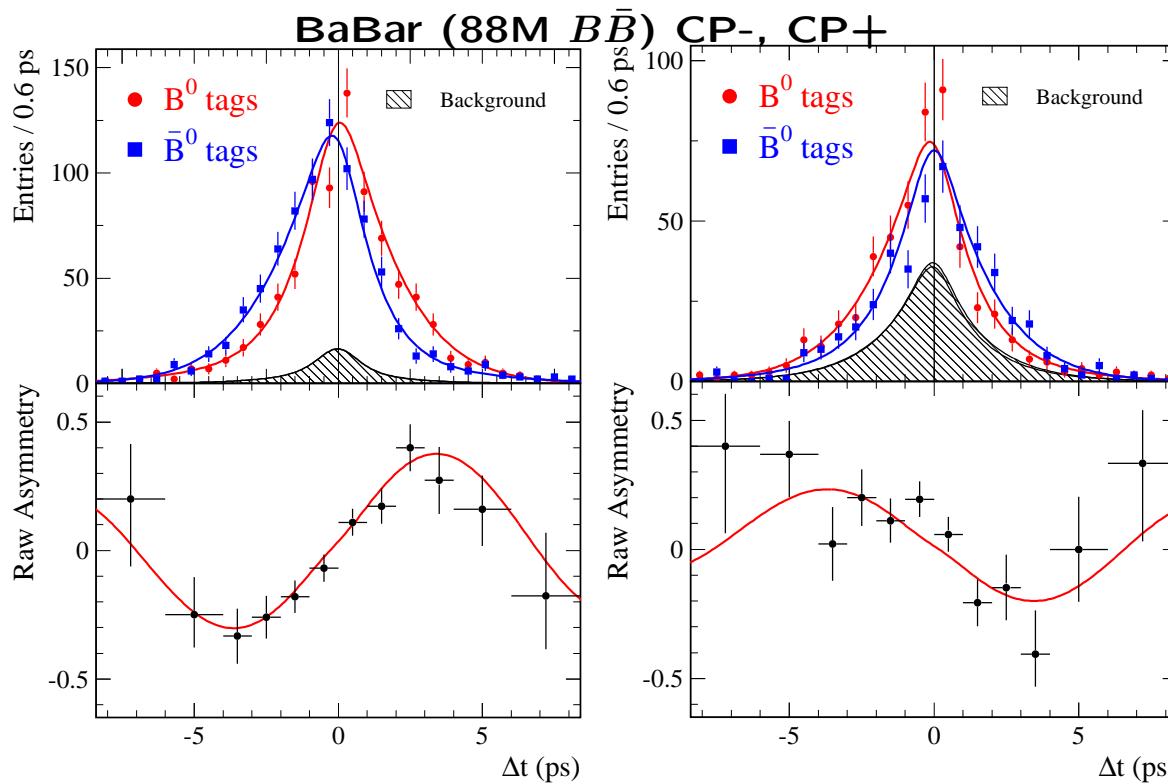


f_{sig} : signal fraction of candidate event

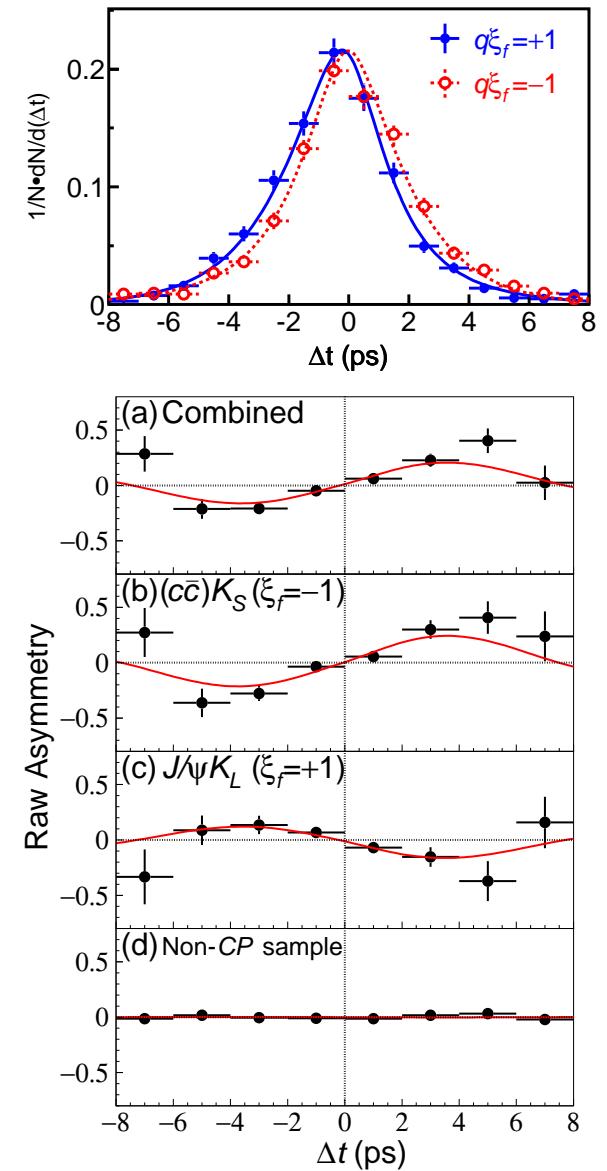
$P_{\text{sig}}, P_{\text{bkg}}$: t probability density function

$R_{\text{sig}}, R_{\text{bkg}}$: Δt resolution

Δt Distributions



Belle (85M $B\bar{B}$) Combined



$\sin 2\phi_1$ Results: $J/\psi K_S$ and other $b \rightarrow c\bar{c}s$ decays

BaBar (88M $B\bar{B}$)

$$\sin 2\beta = 0.741 \pm 0.067 \pm 0.034$$

$$|\lambda| = 0.948 \pm 0.051 \pm 0.030$$

Belle (85M $B\bar{B}$)

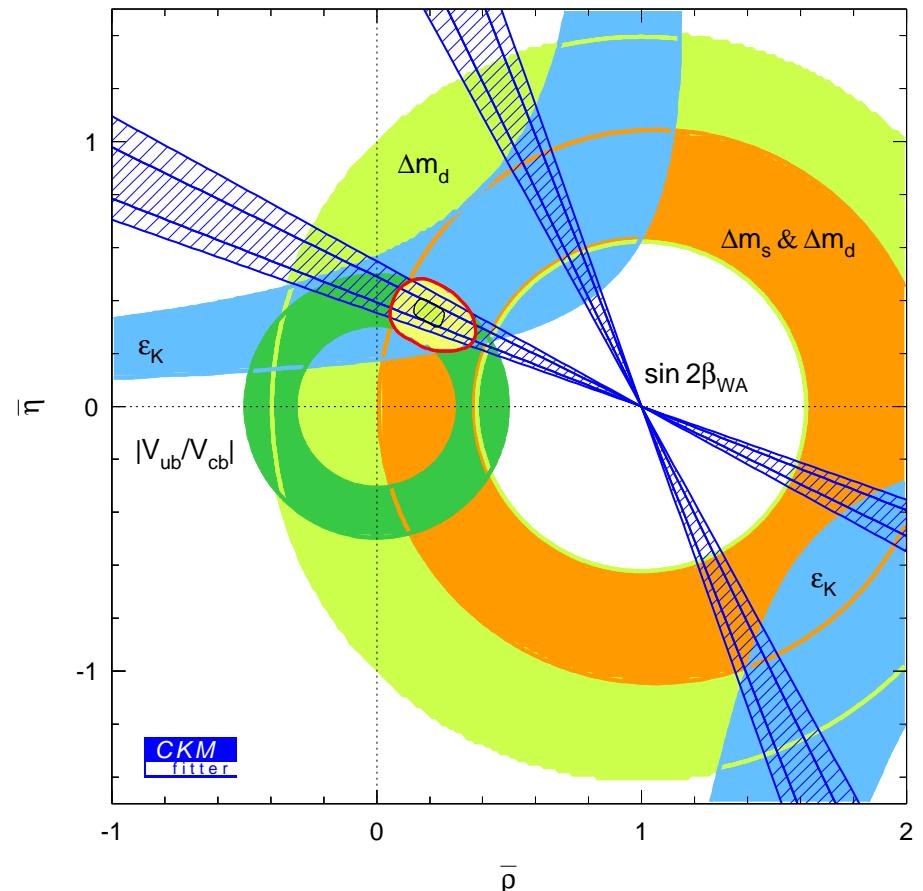
$$\sin 2\phi_1 = 0.719 \pm 0.074 \pm 0.035$$

$$|\lambda| = 0.950 \pm 0.049 \pm 0.025$$

BaBar and Belle combined

$$\sin 2\phi_1 = 0.734 \pm 0.055$$

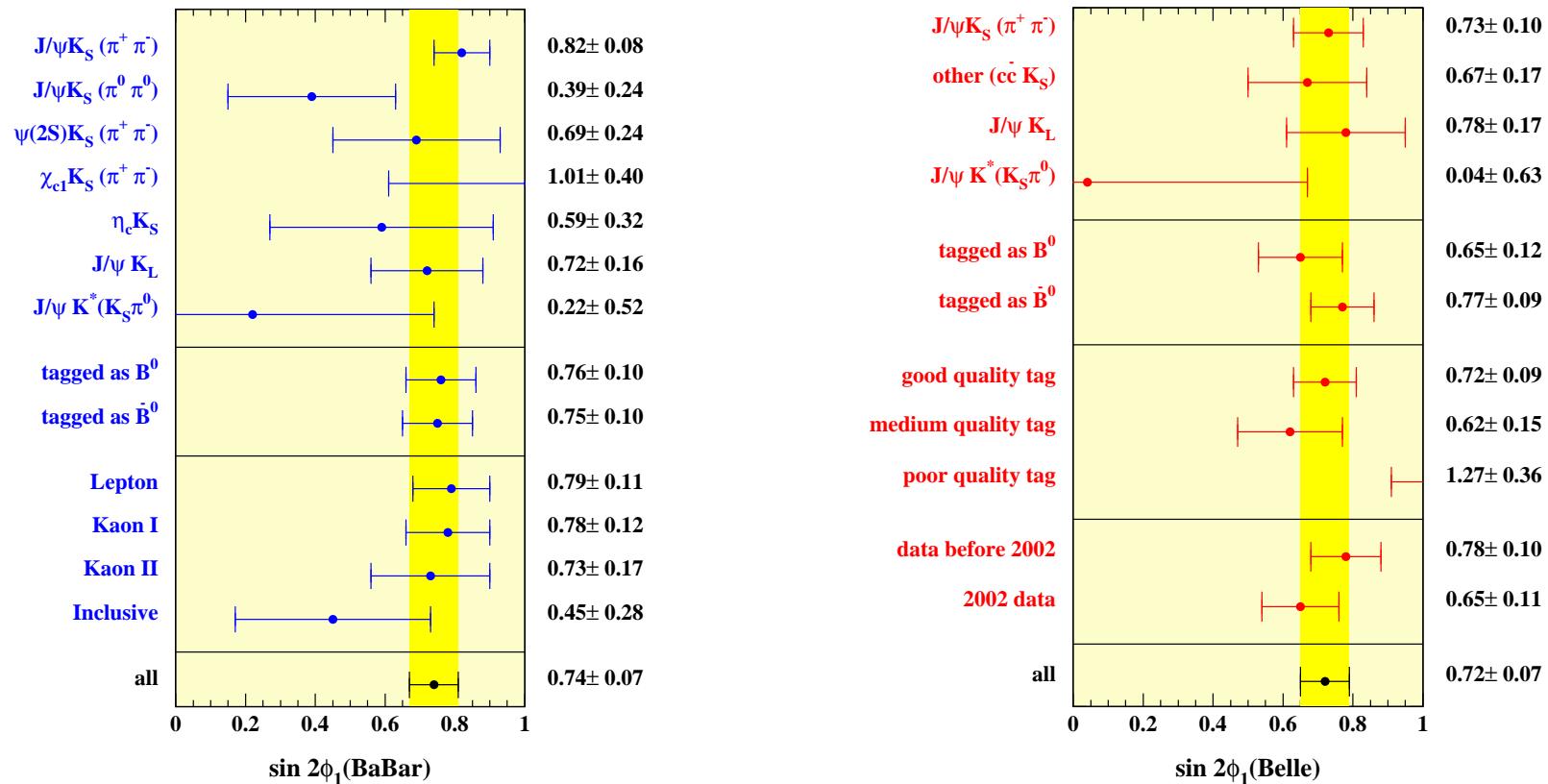
Good agreement with CKM fit.



Red (black): 90% (5%) CL contour
without $\sin 2\phi_1$

Shaded: 1σ , 2σ regions for $\sin 2\phi_1$

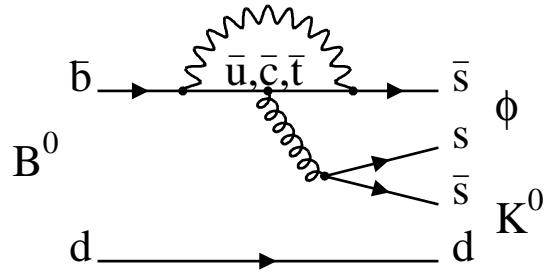
Consistency among Subsamples



All $b \rightarrow c\bar{c}s$ modes point to the same $\sin 2\phi_1$ within the present precision.
How about the modes from other diagrams ?

sin $2\phi_1$ from ϕK_S

Only $b \rightarrow s s \bar{s}$ penguin contribution in SM.



Leading term: $V_{cb}V_{cs}^*(P_c - P_t) = A\lambda^2(P_c - P_t)$

Next term: $V_{ub}V_{us}^*(P_u - P_t) = A\lambda^4(\rho - i\eta)(P_u - P_t)$

(penguin amplitudes: $P_t \gg P_c \gg P_u$)

- Leading term has the same CKM factor as $b \rightarrow c \bar{c} s$.
- Next term has a different phase, but suppressed by $\lambda^2 \simeq 5\%$.
- $\eta_{\phi K_s} = -1 \rightarrow Im\lambda \simeq \sin 2\phi_1$ in SM.

- Allow room for new physics. Parameterize Δt distributions by

$$a_f(\Delta t) = S_f \sin(\Delta m_d \Delta t) + A_f \cos(\Delta m_d \Delta t)$$

$$S_f = \frac{2Im\lambda_f}{|\lambda_f|^2+1} \simeq -\eta_f \sin 2\phi_1 \text{ in SM} \quad A_f = -C_f = \frac{|\lambda_f|^2-1}{|\lambda_f|^2+1} \simeq 0 \text{ in SM.}$$

- Deviation is an indication of new physics in penguin loop (not in mixing).

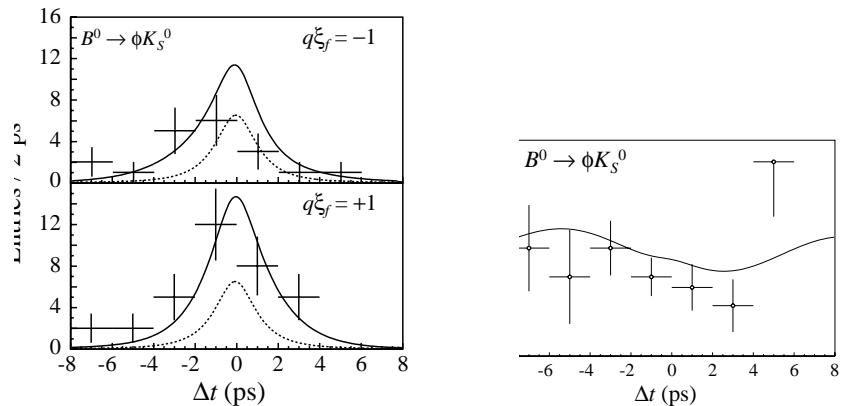
sin 2 ϕ_1 from ϕK_S : Results

BaBar (84M $B\bar{B}$)

$$S_{\phi K_S} = -0.18 \pm 0.51 \pm 0.07$$

$$A_{\phi K_S} = +0.80 \pm 0.38 \pm 0.12$$

Belle (85M $B\bar{B}$)

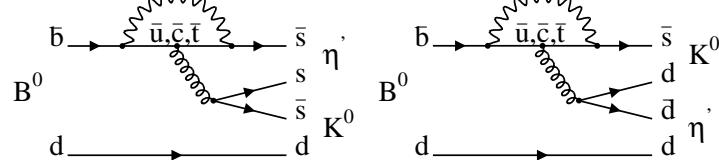


$$S_{\phi K_S} = -0.73 \pm 0.64 \pm 0.22$$

$$A_{\phi K_S} = -0.56 \pm 0.41 \pm 0.16$$

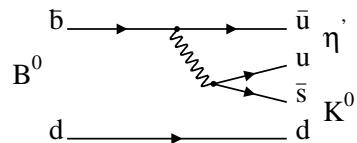
sin 2 ϕ_1 from $\eta' K_S$

**Additional $b \rightarrow s d \bar{d}$ penguin
and $b \rightarrow u$ tree**



$$V_{cb} V_{cs}^* (P_c - P_t) = A \lambda^2 (P_c - P_t)$$

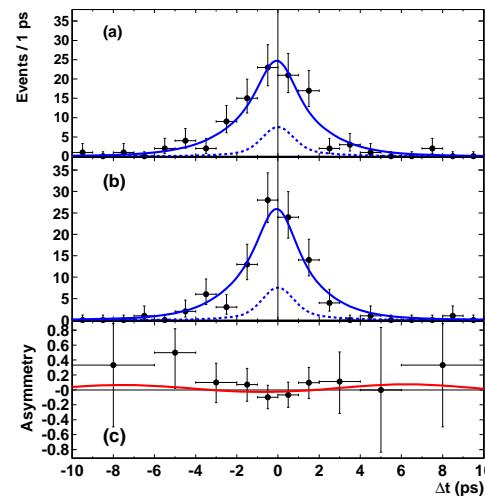
$$V_{ub} V_{us}^* (P_u - P_t) = A \lambda^4 (\rho - i\eta) (P_u - P_t)$$



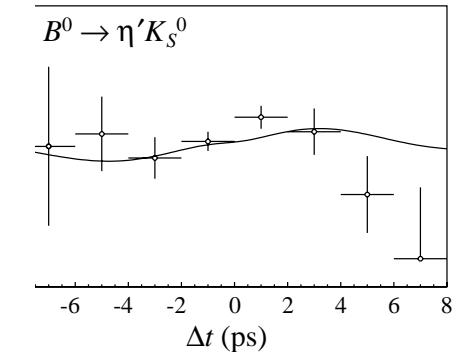
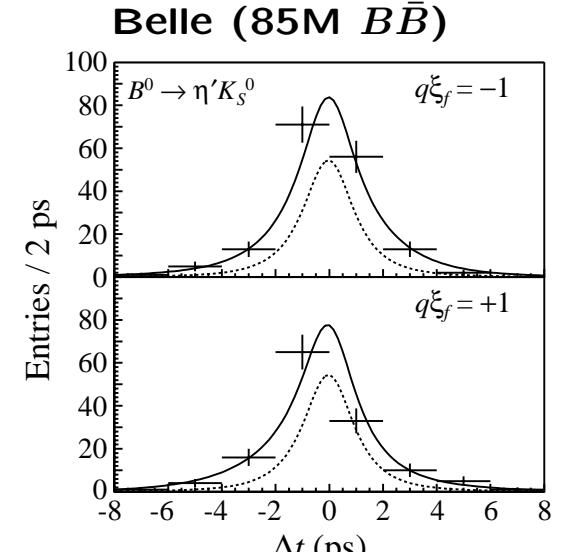
$$V_{ub} V_{us}^* = A \lambda^4 (\rho - i\eta)$$

**Additional 5% $b \rightarrow u$ tree
effect compared with ϕK_S .**

$$\eta_{\eta' K_S} = -1 \rightarrow S_f \simeq \sin 2\phi_1.$$

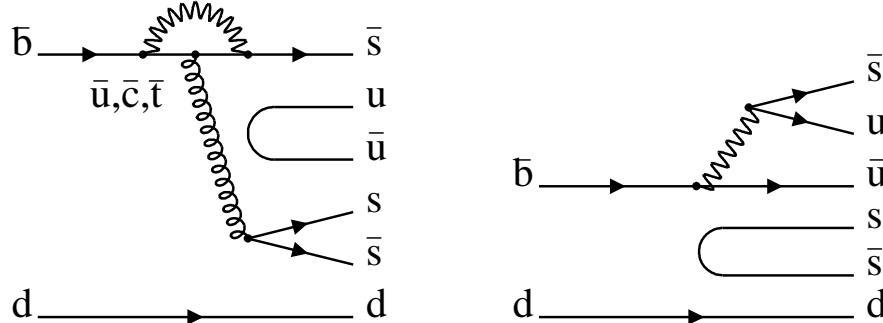


$$S_{\eta' K_S} = +0.02 \pm 0.34 \pm 0.03 \\ A_{\eta' K_S} = -0.10 \pm 0.23 \pm 0.03$$



$$S_{\eta' K_S} = +0.71 \pm 0.37^{+0.05}_{-0.06} \\ A_{\eta' K_S} = +0.26 \pm 0.22 \pm 0.03$$

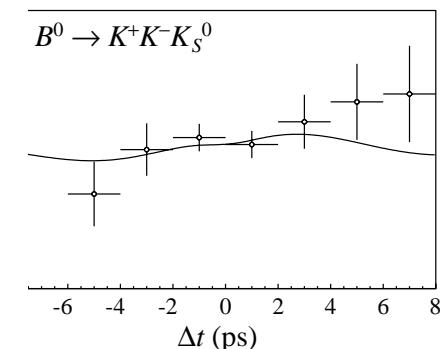
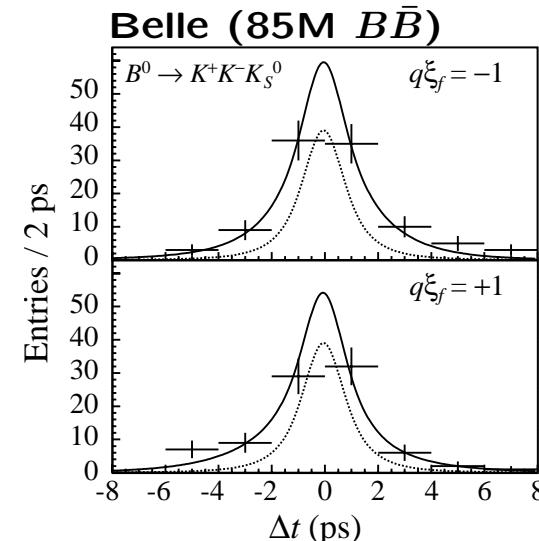
sin 2 ϕ_1 from $K^+K^-K_S$



- $b \rightarrow s\bar{s}\bar{s}$ penguin and $b \rightarrow u\bar{u}$ tree can contribute.
- Three body final state: mixture of CP+ and CP-.

Belle analyses show $b \rightarrow u\bar{u}$ tree is negligible and $\eta_{K^+K^-K_S} \simeq +1$.

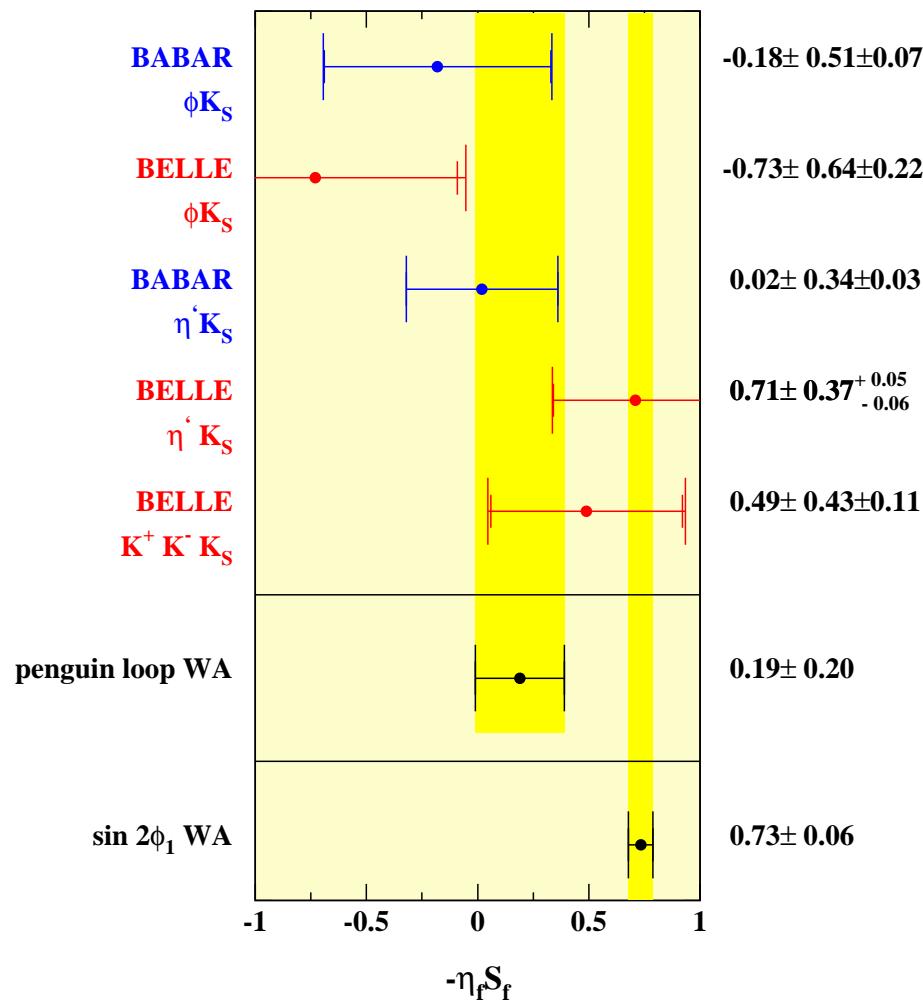
$$S_f \simeq -\sin 2\phi_1.$$



$$S_{K^+K^-K_S} = -0.49 \pm 0.43 \pm 0.11$$

$$A_{K^+K^-K_S} = -0.40 \pm 0.33 \pm 0.10$$

$-\eta_f S_f$ for Penguin Loops ($= \sin 2\phi_1$ in SM)

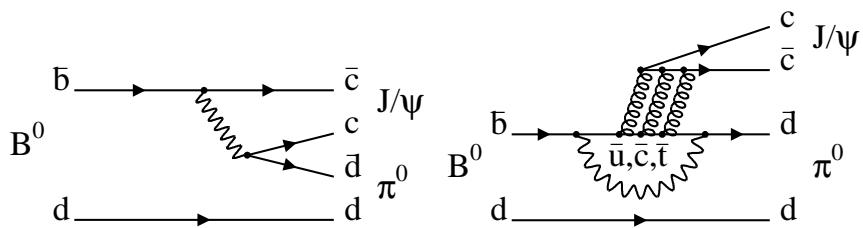


Hint of anomaly?

New physics search in B meson decays is now a reality.

$\sin 2\phi_1$ from $J/\psi \pi^0$?

Tree and penguin are comparable



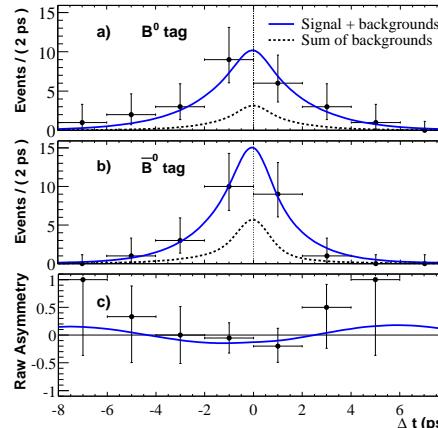
$$V_{cb} V_{cd}^* = -A \lambda^3$$

$$V_{cb} V_{cd}^*(P_c - P_t) = -A \lambda^3 (P_c - P_t)$$

$$V_{ub} V_{ud}^*(P_u - P_t) = A \lambda^3 (\rho - i\eta) (P_u - P_t)$$

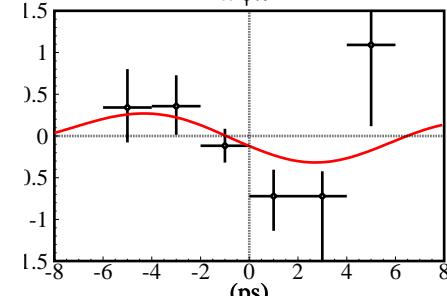
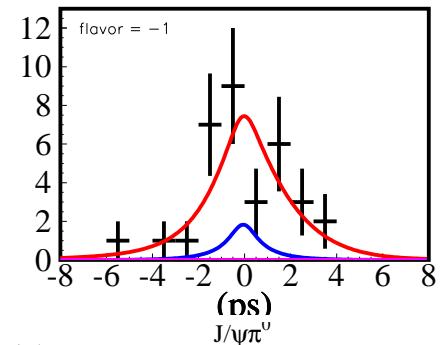
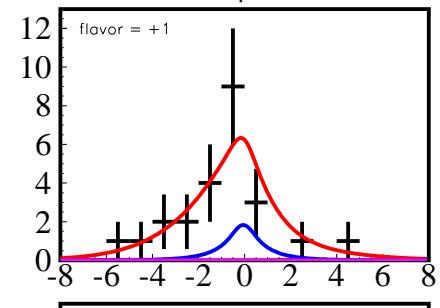
- CKM factor of tree same as $J/\psi K^0$ ($K^0 \rightarrow K_S$).
- $\eta_{J/\psi \pi^0} = +1 \rightarrow S_f \simeq -\sin 2\phi_1$ (If no penguin)
- If a deviation is seen, penguin should be the first suspect.

BaBar (88M $B\bar{B}$)



$$\begin{aligned} S_{J/\psi \pi^0} &= \\ &+0.05 \pm 0.49 \pm 0.16 \\ A_{J/\psi \pi^0} &= \\ &-0.38 \pm 0.41 \pm 0.09 \end{aligned}$$

Belle (85M $B\bar{B}$)

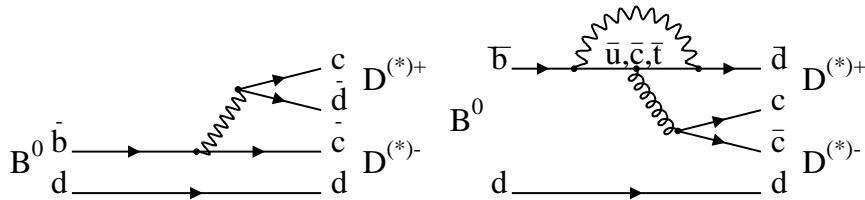


$$\begin{aligned} S_{J/\psi \pi^0} &= \\ &-0.93 \pm 0.49 \pm 0.08 \end{aligned}$$

$$\begin{aligned} A_{J/\psi \pi^0} &= \\ &-0.25 \pm 0.39 \pm 0.06 \end{aligned}$$

$\sin 2\phi_1$ from $D^{*+}D^{*-}$ and $D^{*+}D^-$?

Similar “penguin pollution” as $J/\psi\pi^0$



$$V_{cb}V_{cd}^* = -A\lambda^3$$

$$V_{cb}V_{cd}^*(P_c - P_u) = -A\lambda^3(P_c - P_u)$$

$$V_{tb}V_{td}^*(P_t - P_u) = A\lambda^3(1 - \rho + i\eta)(P_t - P_u)$$

- $D^{*+}D^{*-}$: mix of CP+ and CP-

BaBar angular analysis

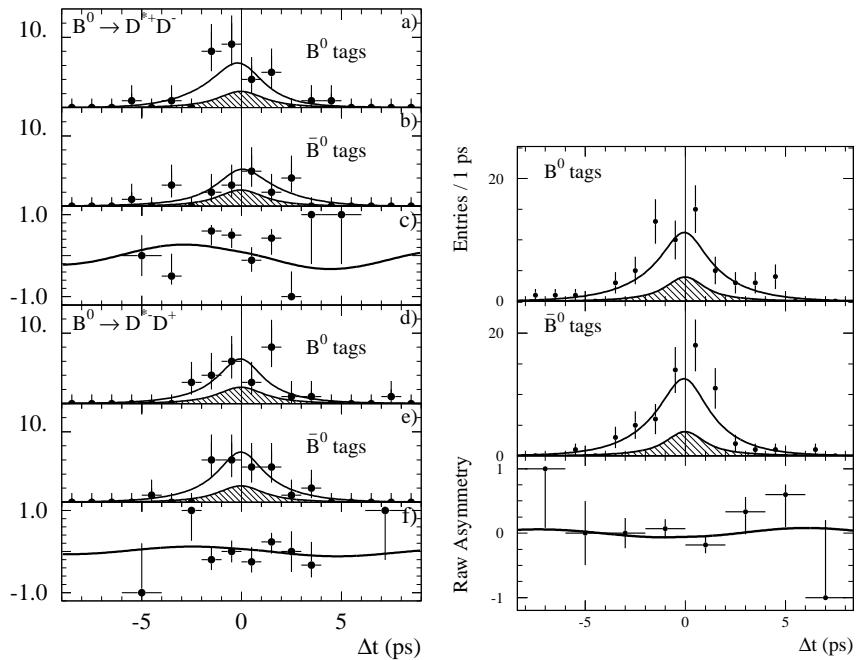
$$\eta_{D^{*+}D^{*-}} \simeq +1$$

$$S_f \simeq -\sin 2\phi_1 \text{ (if no penguin)}$$

- $D^{*+}D^-$: Mixing-induced CPV measurement using non-CP final states.

$$S_f \simeq -\sin 2\phi_1 \text{ (if no penguin)}$$

BaBar (88M $B\bar{B}$), D^*D and D^*D^* (right)



$$S_{D^*D}^\pm = -0.24 \pm 0.69 \pm 0.12$$

$$S_{D^*D}^\mp = -0.82 \pm 0.75 \pm 0.14$$

$$A_{D^*D}^\pm = +0.22 \pm 0.37 \pm 0.10$$

$$A_{D^*D}^\mp = +0.47 \pm 0.40 \pm 0.12$$

For CP+ component:

$$Im\lambda_{f+}(D^*D^*) = 0.05 \pm 0.29 \pm 0.10$$

$$|\lambda_{f+}(D^*D^*)| = 0.75 \pm 0.19 \pm 0.02$$

Summary

- Precision of Δm_d reached 1.2%.
 - New physics effects in $B\bar{B}$ mixing vigorously explored.
 $\delta(\Delta\Gamma/\Gamma) \sim 0.05$ ($< 10^{-2}$ in SM), $\delta(|q/p|) \sim 0.01$ (10^{-3} in SM),
 $Re(\cos\theta) \sim 0.07$, $Im(\cos\theta) \sim 0.03$.
 - Important test ground for Δt measurement and flavor tagging.
- Precision of $\sin 2\phi_1$ reached 8%. Good agreement between BaBar and Belle.
 - Statistical error still dominates.
 - Good agreement with global CKM fit (without $\sin 2\phi_1$).
 - $|\lambda|$ is consistent with 1 in $b \rightarrow c\bar{c}s$ decays as expected in SM.
- New physics search by “ $\sin 2\phi_1$ ” measurements in penguin loops is well under way.
 - $\delta S_{\phi K_S} \sim \pm 0.6$, $\delta S_{\eta' K_S} \sim \pm 0.4$, $\delta S_{(K^+ K^- K_S)} \sim \pm 0.4$.
 - “ $\sin 2\phi_1$ ” (penguin) $= 0.19 \pm 0.20$ ($\sin 2\phi_1 = 0.734 \pm 0.055$). Very exciting.
- “ $\sin 2\phi_1$ ” measurements in “penguin polluted” decays were also pushed to find useful information.

Backup: References

	BaBar	Belle
Δm_d	dilepton hadronic semileptonic $D^*\pi$ partial r	PRL 88, 221803 (2002) PRL 88, 221802 (2002) hep-ex/0212017 PRD 67, 092004 (2003)
$\Delta\Gamma/\Gamma$	hep-ex/0303043	
CPV	hep-ex/0303043 PRL 88, 231801 (2002)	
$CPTV$	hep-ex/0303043	PRD 67, 052004 (2003)
$\sin 2\phi_1$	PRL 89, 201802 (2002)	PRD 66, 071102 (2002)
$S_{\phi K_S}$	Moriond (March 2003)	PRD 67, 031102(R) (2003)
$S_{\eta' K_S}$	hep-ex/0303046	above
$S_{K^+ K^- K_S}$		above
$S_{J/\psi \pi^0}$	hep-ex/0303018	Belle-CONF-0201
$S_{D^* D}$	hep-ex/0303004	
$S_{D^* D^*}$	FPCP (June 2003)	

Backup: Parameters of CP Fit

Parameterization	BaBar	Belle
Signal PDF	$\sin 2\beta$ (1)	$\sin 2\phi_1$ (1)
Signal mistag frac.	w , Δw for 4 cat. (8)	w for 6 cat. (6)
Background mistag frac.	w , Δw for 4 cat. (8)	(0)
Signal Δt resolution	(9)	(13)
Background Δt resolution	(9)	(11)
Fitting method	Use B_{CP} and B_{flav} events Minimize $L_{CP} + L_{\text{mix}}$ Fit with 35 parameters	Use B_{CP} events only Maximize L_{CP} Fit with $\sin 2\phi_1$ only Others from data and MC

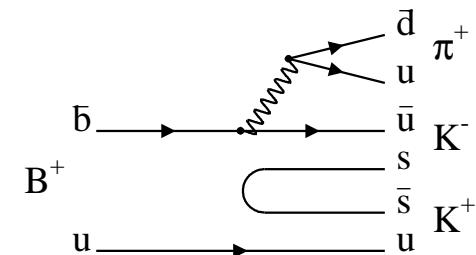
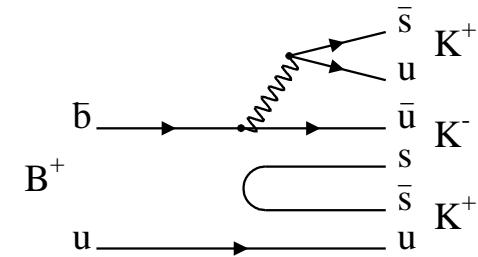
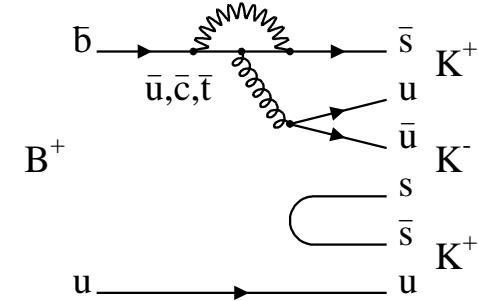
Backup slide: $b \rightarrow u$ tree contribution to KKK final state

- KKK is dominated by $b \rightarrow s$ penguin.
- $KK\pi$ is dominated by $b \rightarrow u$ tree.
- $b \rightarrow u$ tree contribution to KKK :
- $F = \left| \frac{A_{b \rightarrow u}^{KKK}}{A_{\text{total}}^{KKK}} \right| = \frac{B(B^+ \rightarrow K^+ K^- \pi^+)}{B(B^+ \rightarrow K^+ K^+ K^-)} \times \left(\frac{f_K}{f_\pi} \right) \times \tan^2 \theta_C$

$$F = 0.022 \pm 0.005 \quad (B^+)$$

$$F = 0.023 \pm 0.013 \quad (B^0)$$

- $b \rightarrow u$ tree contribution is 10 - 15% in amplitude.



Backup slide: CP content in $K_S^0 K^+ K^-$ state

- Isospin symmetry:
- $B(B^0 \rightarrow K^0 K^+ K^-) = B(B^+ \rightarrow K^+ K^0 \bar{K}^0) \times \frac{\tau_{B^0}}{\tau_{B^+}}$
- $K^0 \bar{K}^0$ must be symmetric (Bose statistics):
- $|K^+ K^0 \bar{K}^0\rangle = \alpha \frac{|K^+ K_S K_S\rangle + |K^+ K_L K_L\rangle}{\sqrt{2}} + \beta |K^+ K_S K_L\rangle$
($\alpha, \beta \cdot \cdot$ relative orbital angular momentum even, odd)
- $\alpha^2 = 2 \frac{B(B^+ \rightarrow K^+ K_S K_S)}{B(B^0 \rightarrow K^0 K^+ K^-)} \times \frac{\tau_{B^0}}{\tau_{B^+}}$

α gives CP even component of $K_S K^+ K^-$.

- Belle result (after removing ϕK_S events):

$$\alpha^2 = 1.04 \pm 0.19 \pm 0.06$$

Backup slide: Contributing terms for CP mode decays

mode	leading term	next term
$J/\psi K_S$	$V_{cb}V_{cs}^* = A\lambda^2$	$V_{ub}V_{us}^*(P_u - P_t) = A\lambda^4(\rho - i\eta)(P_u - P_t)$
	$V_{cb}V_{cs}^*(P_c - P_t) = A\lambda^2(P_c - P_t)$	
ϕK_S	$V_{cb}V_{cs}^*(P_c - P_t) = A\lambda^2(P_c - P_t)$	$V_{ub}V_{us}^*(P_u - P_t) = A\lambda^4(\rho - i\eta)(P_u - P_t)$
		$V_{ub}V_{us}^* = A\lambda^4(\rho - i\eta)$
$J/\psi \pi^0$	$V_{cb}V_{cd}^* = -A\lambda^3$	
	$V_{cb}V_{cd}^*(P_c - P_u) = -A\lambda^3(P_c - P_u)$	
	$V_{tb}V_{td}^*(P_t - P_u) = A\lambda^3(1 - \rho + i\eta)(P_t - P_u)$	

