

## Exercise on $W$ -boson production

Consider the production of a  $W^-$ -boson, which proceeds at LHC through the reaction

$$pp \rightarrow W^- + X, \quad (1)$$

where  $X$  is any allowed final state. At the parton level, this reaction proceeds to lowest order in perturbation theory through

$$\bar{u}d \rightarrow W^- \rightarrow l^- \bar{\nu}_l. \quad (2)$$

Calculate the cross section for  $W$ -boson production at LHC ( $\sqrt{s} = 14$  TeV) according to the factorization theorem as

$$\sigma_{pp \rightarrow W^- \rightarrow l^- \bar{\nu}_l} = \sum_{ij} \int dx_1 dx_2 f_i(x_1) f_j(x_2) \hat{\sigma}_{ij \rightarrow W^- \rightarrow l^- \bar{\nu}_l}(x_1, x_2, s), \quad (3)$$

For the parton distribution function you can assume for simplicity the following functional form

$$f_d(x) = \frac{0.2}{x}, \quad f_{\bar{u}}(x) = 2 \cdot f_d(x). \quad (4)$$

Compare your results for  $\sigma_{pp \rightarrow W^- \rightarrow l^- \bar{\nu}_l}$  with values from the literature.

**Hint:** Take all necessary ingredients and constants from the *Particle Data Booklet*, <http://pdg.lbl.gov> Eq. (39.18) in the PDG provides you with a formula for the parton cross section  $\hat{\sigma}_{ij \rightarrow W^-}$ .